

$b \rightarrow s\nu\bar{\nu}$  decays in the MSSM with general  
flavor mixing

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based on work with F. Borzumati (NCU, Taiwan)

- $b \rightarrow s\nu\bar{\nu}$  decays
- SUSY and Higgs contributions
  - $\tan\beta$  -enhanced one-loop flavor violations
  - correlation with  $b \rightarrow s\gamma$
- each sector
  - gluino-squark loops
  - chargino-squark loops
  - $(H^\pm, q)$  loops and other B processes

# Introduction

FCNC processes are very important to probe the physics beyond the SM

- \* No tree-level SM contributions
- ⇒ contributions from new physics are relatively enhanced

FCNC in  $B$  physics

$B_{d,s}-\bar{B}_{d,s}$  mixings,  $b \rightarrow s\gamma$ ,  $b \rightarrow sl^+l^-$ ,  $B_{s,d} \rightarrow \mu^+\mu^-$ , ...

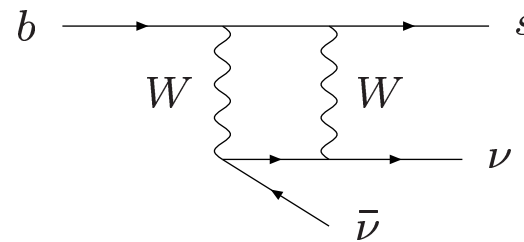
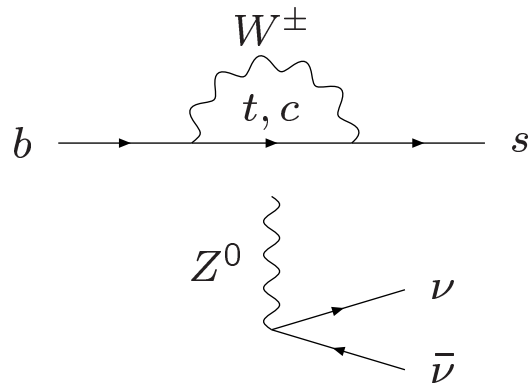
Here we consider the decays  $b \rightarrow s\nu\bar{\nu}$  in the MSSM (minimal supersymmetric standard model), especially for general squark flavor mixing and at large  $\tan\beta = \langle H_U \rangle / \langle H_D \rangle \gg 1$ .

$b \rightarrow s\nu\bar{\nu}$  ( $\bar{B} \rightarrow X_s\nu\bar{\nu}$ ) decays ( $B^- \rightarrow K^{(*)-}\nu\bar{\nu}, \dots$ )

Generated by Z-penguin and box diagrams.

SM contributions

$$\sim K_{ts}^* K_{tb} (\bar{s}_L \gamma^\mu b_L) (\bar{\nu} \gamma_\mu \nu)$$



- \* Inclusive branching ratio  $\text{BR}(\bar{B} \rightarrow X_s\nu\bar{\nu})$ :  
 small uncertainty from hadronic/nonperturbative corr.  
 by hard GIM cancellation/dominance of top loops  
 $\Rightarrow$  **theoretically clean prediction** “Golden mode”

## Experimental search for $b \rightarrow s\nu\bar{\nu}$

Search for  $B \rightarrow (K, K^*, \dots) + E_{\text{missing}}$  : not observed yet

Upper limits:

$$\text{Br}(\bar{B} \rightarrow X_s + E_{\text{miss}}) < 6.4 \times 10^{-4} \text{ (ALEPH, 2001)}$$

$$\text{Br}(B^- \rightarrow K^- + E_{\text{miss}}) < 3.6 \times 10^{-5} \text{ (Belle, 2005)}$$

Still much larger than the SM predictions (sum of  $\nu = \nu_{e,\mu,\tau}$ )

$$\text{Br}(\bar{B} \rightarrow X_s\nu\bar{\nu})_{SM} \sim (3.7 \pm 0.2) \times 10^{-5} \text{ (Bobeth et al, 2005)}$$

$$\text{Br}(B^- \rightarrow K^-\nu\bar{\nu})_{SM} = (3.8 \pm \frac{1.2}{0.6}) \times 10^{-6} \text{ (Buchalla et al, 2001)}$$

A target at Super B factory

Comparison with  $s \rightarrow d\nu\bar{\nu}$

$$\mathcal{A}(b \rightarrow s\nu\bar{\nu}) \propto K_{ts}^* K_{tb} \sim \lambda^2 \gg \mathcal{A}(s \rightarrow d\nu\bar{\nu}) \propto K_{td}^* K_{ts} \sim \lambda^5$$

Larger amplitude, but harder to detect

Cf.

$$\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu})_{SM} = (8.0 \pm 1.1) \times 10^{-11}$$

$$\text{Br}(K_L^0 \rightarrow \pi \nu\bar{\nu})_{SM} = (2.8 \pm 0.4) \times 10^{-11} \text{ (Buras et al, 2006)}$$

$$\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu})_{exp} = (1.5 \pm \frac{1.3}{0.9}) \times 10^{-10} \text{ (E949, 2004)}$$

Observed

# MSSM (minimal supersymmetric standard model)

A very promising extension of the Standard model

All particles in SM form “supermultiplets” with their **SUSY partners(SUSY particles)**, which have the same gauge charges and different spins by 1/2.

\* Having two Higgs doublets

$$H_D = (H_D^0, H_D^-), \quad H_U = (H_U^+, H_U^0),$$

$$\langle H_D^0 \rangle^2 + \langle H_U^0 \rangle^2 = 2m_W^2/g_2^2, \quad \langle H_U^0 \rangle / \langle H_D^0 \rangle \equiv \tan \beta$$

$$\langle H_D \rangle \rightarrow m_d, m_l \quad \langle H_U \rangle \rightarrow m_u \quad (\text{at tree level})$$

### Chiral supermultiplets

fermion ( $s = 1/2$ )		scalar ( $s = 0$ )	
$q_L = (u_L, d_L)$	quarks	$\tilde{q}_L = (\tilde{u}_L, \tilde{d}_L)$	squarks
$u_R, d_R$		$\tilde{u}_R, \tilde{d}_R$	
$l_L = (\nu_L, e_L)$	leptons	$\tilde{l}_L = (\tilde{\nu}_L, \tilde{e}_L)$	sleptons
$e_R$		$\tilde{e}_R$	
$\tilde{H}_D, \tilde{H}_U$	higgsino	$H_D, H_U$	Higgs bosons

### Vector supermultiplets

fermion ( $s = 1/2$ )		gauge boson ( $s = 1$ )	
$\tilde{g}$	gluino	$g_\mu$	SU(3) boson (gluon)
$\tilde{W}$	wino	$W_\mu$	SU(2) boson
$\tilde{B}$	bino	$B_\mu$	U(1) boson

$$(\tilde{W}^\pm, \tilde{H}^\pm) \rightarrow \tilde{\chi}_{1,2}^\pm (\text{charginos}), \quad (\tilde{B}, \tilde{W}^0, \tilde{H}_D^0, \tilde{H}_U^0) \rightarrow \tilde{\chi}_{1-4}^0 (\text{neutralinos}),$$

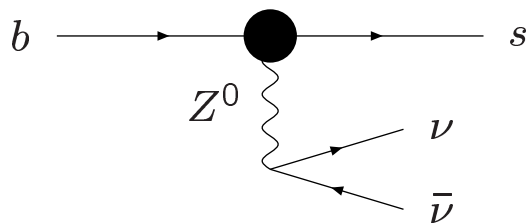
$$(\tilde{q}_L, \tilde{q}_R) \rightarrow \tilde{q}_{1-6}$$

# SUSY/Higgs contributions to $b \rightarrow s\nu\bar{\nu}$

Bertolini et al; Grossman et al; Buchalla et al; ...

(1)  $Z^0$ -penguin diagrams by effective  $(Z_\mu\bar{s}_L\gamma^\mu b_L, Z_\mu\bar{s}_R\gamma^\mu b_R)$  vertex (quark-Higgs, squark-ino)

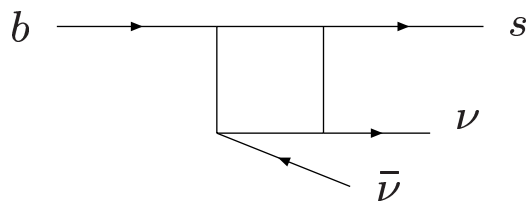
main parts of SUSY/Higgs contributions



Need flavor changing and SU(2) breaking in the loops

(2) Box diagrams

usually small for SUSY loops



Effective Hamiltonian for  $b \rightarrow s\nu\bar{\nu}$

$$H_{\text{eff}} = -\frac{2G_f\alpha}{\sqrt{2}\pi}K_{ts}^*K_{tb}[C_\nu\mathcal{O}_L + C'_\nu\mathcal{O}_R],$$

$$\mathcal{O}_L = (\bar{s}_L\gamma^\mu b_L)(\bar{\nu}_L\gamma_\mu\nu_L), \quad \mathcal{O}_R = (\bar{s}_R\gamma^\mu b_R)(\bar{\nu}_L\gamma_\mu\nu_L)$$

$$C_\nu = C_\nu(\text{SM}) + C_\nu(\text{new}), C'_\nu = C'_\nu(\text{new}) \quad (C_\nu(\text{SM}) \simeq -6.6)$$

Inclusive branching ratio

$$\sum_\nu \text{Br}(B \rightarrow X_s\nu\bar{\nu}) \sim \frac{N_\nu\alpha^2}{4\pi^2}\text{Br}(B \rightarrow X_{ce}\bar{\nu}_e)\frac{|K_{tb}K_{ts}^*|^2}{|K_{cb}|^2}(|C_\nu|^2 + |C'_\nu|^2)$$

(+ QCD corr.)

# Flavor mixing in squark sector

Squark mass matrix in the “super-CKM” basis  $(\tilde{q}_{Li}, \tilde{q}_{Ri})$   
( $i = 1 - 3, q = (u, c, t; d, s, b)$ )

$$M_{\tilde{q}}^2 = \begin{pmatrix} M_{\tilde{q}LL}^2 & (M_{\tilde{q}RL}^2)^\dagger \\ M_{\tilde{q}RL}^2 & M_{\tilde{q}RR}^2 \end{pmatrix},$$
$$(M_{\tilde{q}LL}^2) = m_{\tilde{q}LL}^2 + (m_q^{(0)})^\dagger (m_q^{(0)}) + D_{qL} I,$$
$$(M_{\tilde{q}RR}^2) = m_{\tilde{q}RR}^2 + (m_q^{(0)}) (m_q^{(0)})^\dagger + D_{qR} I,$$
$$(M_{\tilde{q}RL}^2) = (m_{\tilde{q}RL}^2) - (\tan \beta)^{-2I_q} \mu m_q^{(0)}$$

Off-diagonal parts of  $M_{\tilde{q}LL,RR,RL}^2$  may generate potentially large FCNC.  
here assume only 2 – 3 mixings

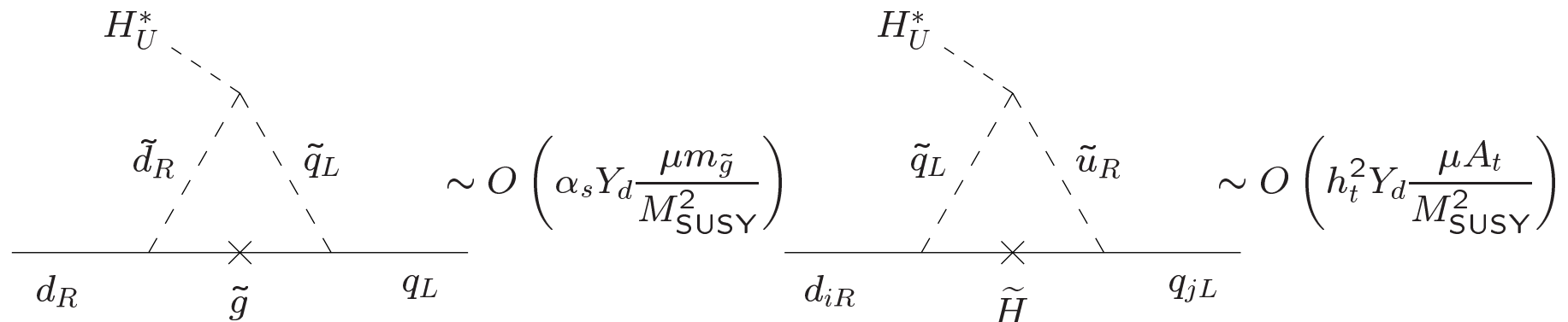
# tan $\beta$ -enhanced one-loop quark flavor violation

Effective interactions of  $d_{iR} = (d, s, b)_R$  to two Higgs doublets, after SUSY particles are integrated out

$$\mathcal{L}_{\text{int}} = -(Y_1^d)_{ij} \bar{d}_{iR} q_{jL} H_D - (\Delta Y_2^d)_{ij} \bar{d}_{iR} q_{jL} H_U^c$$

$H_U \sim h^0$  (SM – like),  $H_D \sim (H^0, A^0, H^\pm)$  at  $\tan \beta \gg 1$

$\Delta Y_2^d = 0$  at tree-level by SUSY (No FCNC in  $H-q$  interaction), but induced by SUSY loops with soft SUSY breaking.



## $O(\tan \beta)$ corrections to $H - q$ couplings

Hempfling; Hall et al.; Carena et al.; Blazek et al.; Babu, Kolda; Foster, Okumura, Roszkowski; ...

$$m_d(\text{SM})_{ij} = \frac{\bar{v}}{\sqrt{2}} \cos \beta [Y_1^d + \tan \beta \Delta Y_2^d]_{ij} \quad \text{diagonal (superCKM basis)}$$

$\Updownarrow$

$$(\text{bare mass})(m_d^{(0)})_{ij} = \frac{\bar{v}}{\sqrt{2}} \cos \beta (Y_1^d)_{ij} \quad \text{in } M_{\tilde{d}RL}: \text{ nondiagonal}$$

$$g(H^0 \bar{d}_{iR} d_{jL}, \tilde{H}_D^0 \tilde{d}_{iR}^* d_{jL})^{\text{eff}} \simeq (Y_1^d)_{ij} \quad \text{nondiagonal}$$

$$g(H^- \bar{d}_{iR} u_{jL}, \tilde{H}_D^- \tilde{d}_{iR}^* u_{jL})^{\text{eff}} \simeq (Y_1^d)_{il} K_{jl}^*, \quad \text{not prop. to } K_{ji}^*$$

$\tan \beta$ -enhanced one-loop flavor-changing couplings of  $(H, \tilde{H})$  to (s)quarks, not governed by CKM matrix, are generated.

New source for FCNC

# SUSY/Higgs contributions in MSSM

## (1) Gluino-squark loops

generated by  $\tilde{b} - \tilde{s}$  and  $\tilde{q}_L - \tilde{q}_R$  mixings in the loops **enhanced by  $\tan \beta \gg 1$  and squark flavor mixings**

## (2) Chargino-squark loops

Important for small/moderate  $\tan \beta$ :  
Main subject in previous studies

## (3) ( $H^\pm$ , $t$ ) loops

$\Delta C_\nu (b_L \rightarrow s_L)$ :  $O(m_t^2 / \tan^2 \beta)$ , only relevant for  $\tan \beta \sim 1$   
 $\Delta C'_\nu (b_R \rightarrow s_R)$ :  $O(m_b m_s \tan^2 \beta)$  in “minimal flavor violation”  
relevant for  $\tan \beta \gg 1$  and with **flavor mixing of  $\tilde{s}_R$**

## Correlations to $b \rightarrow s\gamma$

$b \rightarrow s\gamma$ :

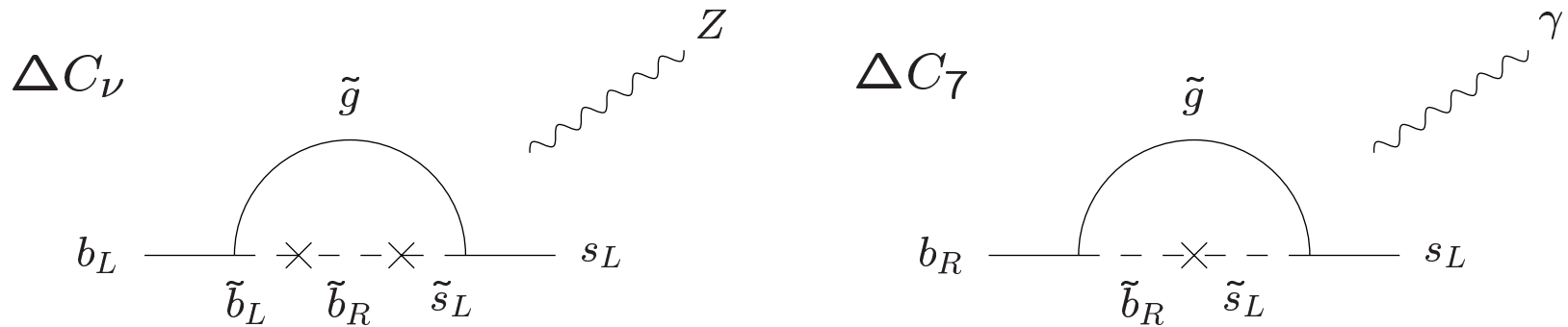
enhanced by the  $SU(2) \times U(1)$  breakings and  $3 \rightarrow 2$  flavor changing in the loops (same as  $b \rightarrow s\nu\bar{\nu}$ )

$\Rightarrow$  experimental bound on  $b \rightarrow s\gamma$  might give constraints on the SUSY/Higgs contributions to  $b \rightarrow s\nu\bar{\nu}$ .

Very rough estimation of the constraints:

Requiring Wilson coeff.  $(\Delta C_7, \Delta C'_7)(\mu_W)$  for  $b \rightarrow s\gamma$  from each SUSY/Higgs sector to be not larger than  $C_7(\text{SM}, \mu_W) \sim -0.2$

(1) Gluino-squark contribution to  $(C_\nu, C'_\nu)$



Both scale with  $\tilde{b}_R - \tilde{s}_L$  mixing  $\propto \tan \beta$

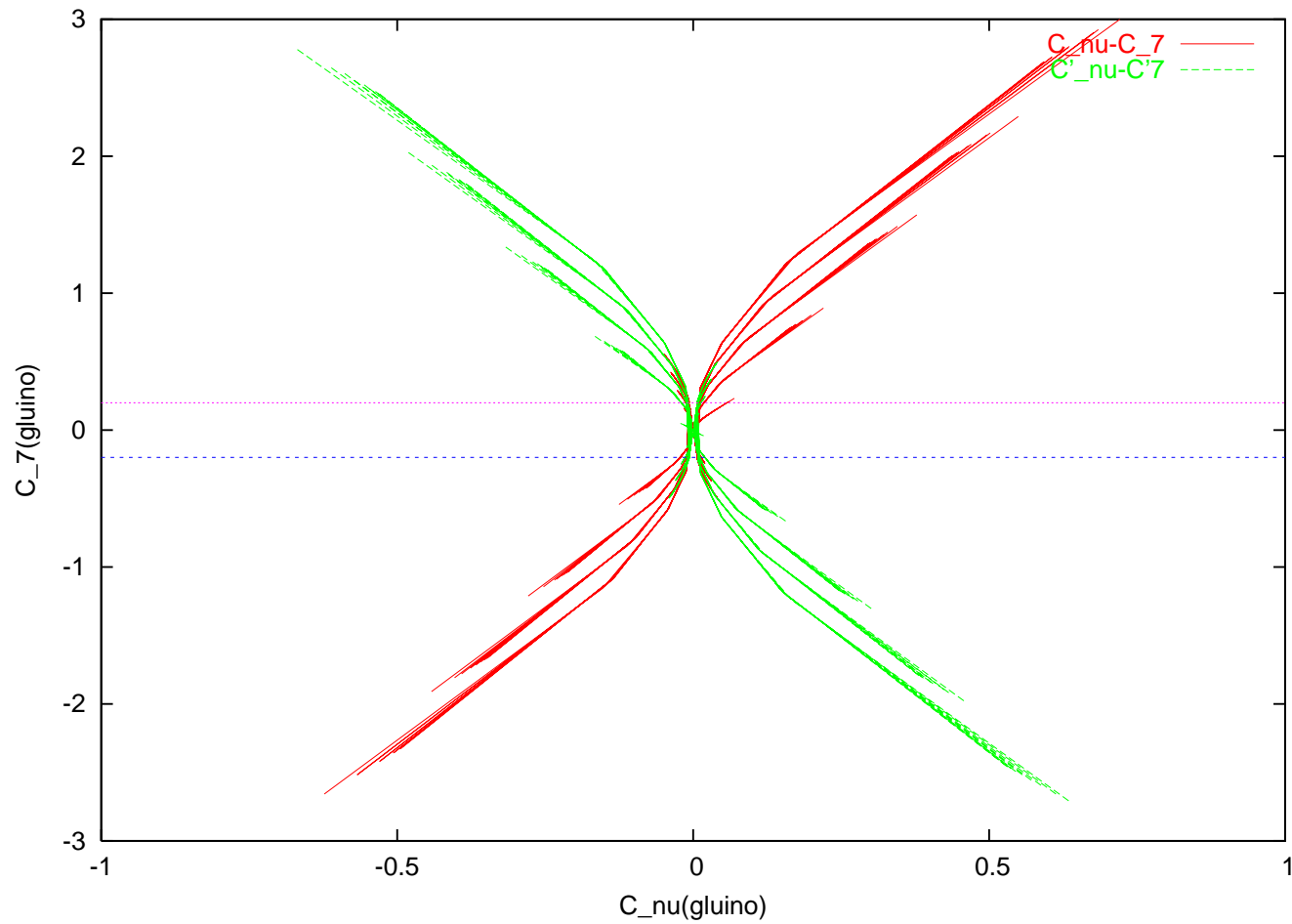
(loop-induced or multi-insertion)

Requiring  $|\Delta C_7(\tilde{g})| < |C_7(\text{SM}, \mu_W)| \sim 0.2$  constrains  $\Delta C_\nu(\tilde{g})$  much smaller than  $C_\nu(\text{SM}) = -6.6$ .

Gluino contributions cannot be large, even at  $\tan \beta \gg 1$

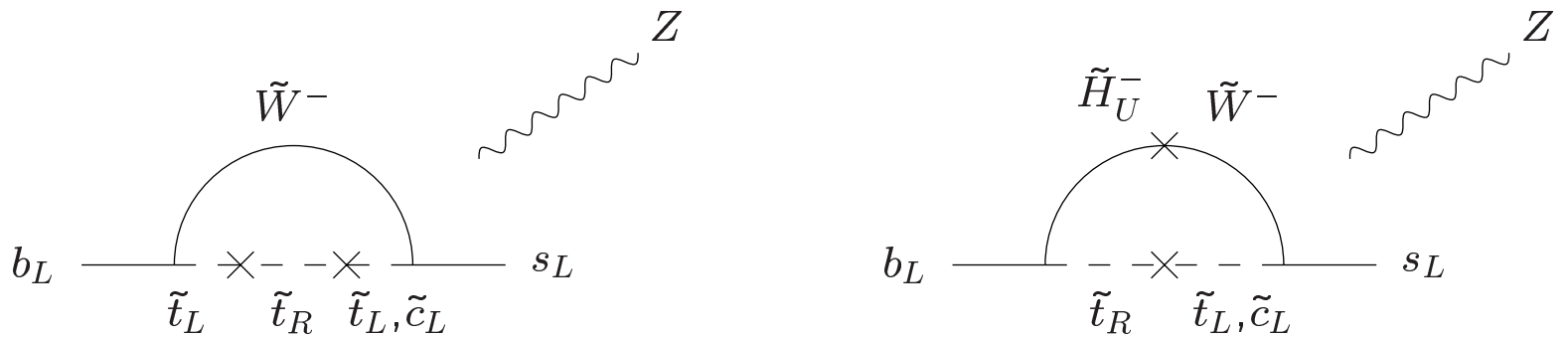
# $\Delta C_\nu - \Delta C_7$ corr. (gluino-squark loops)

$\tan \beta = 50$ ,  $M_{\tilde{q}} = 500$  GeV,  $m_{\tilde{g}} = 600$  GeV,  $\mu = [-500, 500]$  GeV,  $(\delta_{LL,RR}^d)_{23} = [-0.2, 0.2]$



## (2) Chargino-squark contributions

main parts

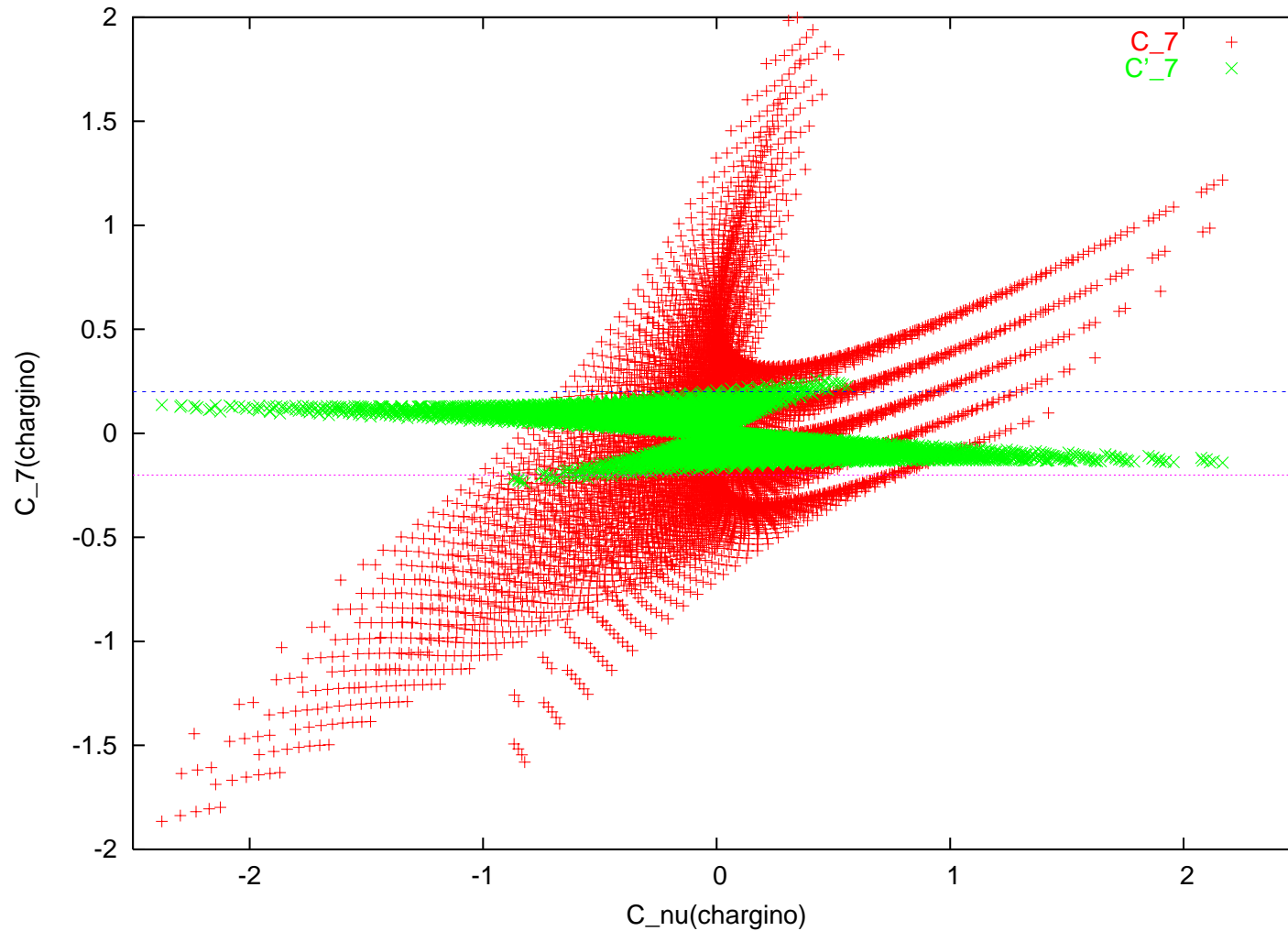


$\Delta C_\nu$  increases with  $(A_u)_{33}$  ( $\tilde{t}_R - \tilde{t}_L$ ) and  $(A_u)_{32}$  ( $\tilde{t}_R - \tilde{c}_L$ ) mixings

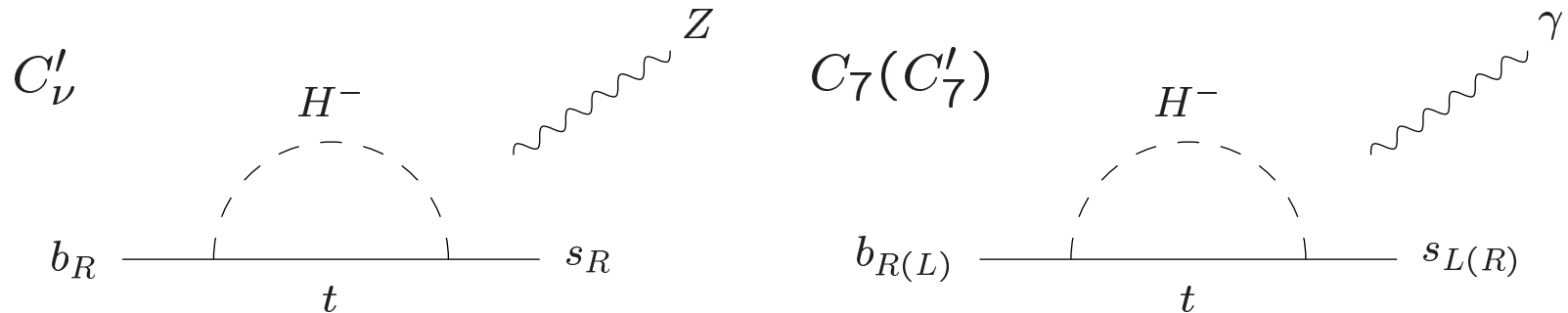
$$(m_{\tilde{u}_{RL}})_{33,32} \equiv m_t (A_u)_{33,32}$$

$\Delta C_7(\tilde{\chi}^\pm)$  also increases with  $(A_u)_{33,32}$  as well as with  $\tan \beta$ , but Possible to have sizable  $\Delta C_\nu(\tilde{\chi}^\pm)$  while  $\Delta C_7(\tilde{\chi}^\pm) \sim 0$  due to their different dependences on  $((A_u)_{33}, (A_u)_{32})$

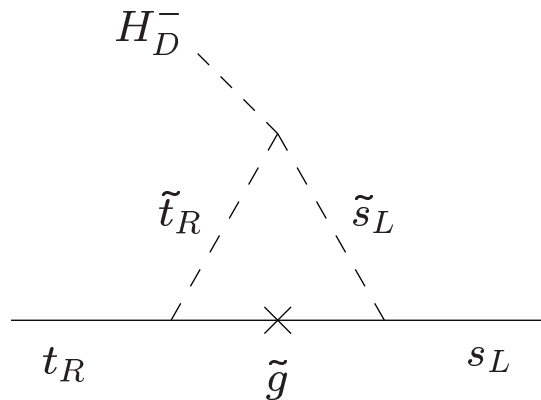
$[\tan \beta = 50, M_{\tilde{q}} = 500 \text{ GeV}, M_2 = 300 \text{ GeV}, \mu = 550 \text{ GeV}, m_{\tilde{l}} = 400 \text{ GeV},$   
 $(\delta_{LL}^u)_{23} = [-0.2, 0.2], (\delta_{RR}^u)_{23} = 0 ]$  cf.  $C_\nu(SM) = -6.6$



$H^\pm$  contributions for  $\tan \beta \gg 1$   
 (by loop-generated effective  $H - s_R$  couplings)



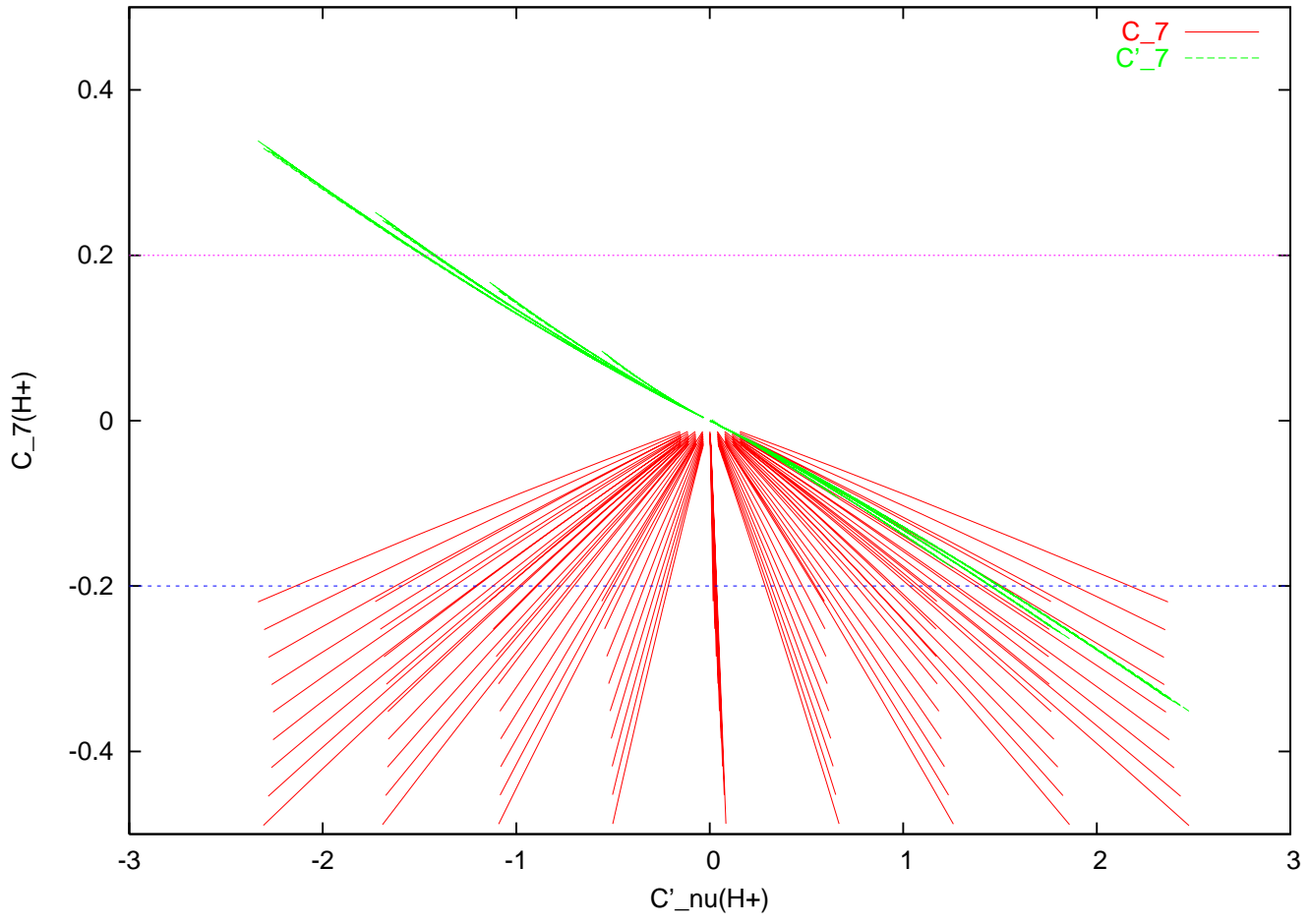
Correlation between  $C'_\nu(H^\pm)$  and  $C_7(H^\pm)$ : severely affected by  $O(\tan \beta)$  vertex corrections to the  $t_R - s_L - H^\pm$  coupling in  $C_7(H^\pm)$ .



$$= h_t \Delta_t \sim O\left(\alpha_s h_t \frac{\mu m_{\tilde{g}}}{M_{\text{SUSY}}^2}\right)$$

Remove  $\cot \beta$  and  $K_{ts}$  suppression of tree-level coupl.  $\sim K_{ts} \frac{\sqrt{2}}{v} m_t \cot \beta$

$[\tan \beta = 50, M_{\tilde{q}} = 1000 \text{ GeV}, M_3 = 1200 \text{ GeV}, \mu = -500 \text{ GeV}, (A_u)_{33} = 500 \text{ GeV}, \delta_{LL,RR}^d = [-0.2, 0.2], m_{H^\pm} = [200, 2000] \text{ GeV}]$   
 cf.  $C_\nu(SM) = -6.6$



## Other FCNC constraints on $C'_\nu(H^\pm)$

Effective  $H^+\bar{s}_R t_L$  coupling is associated with  $(H^0, A^0)\bar{s}_R b_L$  by SU(2) symmetry.

Large “tree-level” contributions to  $B_s - \bar{B}_s$  mixing and  $B_s \rightarrow \mu^+\mu^-$  are induced by Higgs penguin.



$$\Delta M_{B_s}(H^+) < \Delta M_{B_s}(SM) \rightarrow |(Y_1^d)_{32}(Y_1^d)_{23}^*| < 8 \times 10^{-6} (m_A/500 \text{ GeV})^2$$

$$\text{Br}(B_s \rightarrow \mu^+\mu^-) < 8 \times 10^{-8} \text{ (CDF, 2006)}$$

$$\rightarrow |(Y_1^d)_{32} - (Y_d^1)_{23}^*| < 0.4 \cos \beta (m_A/500 \text{ GeV})^2$$

$$\Rightarrow |C'_\nu(H^+)| < 0.1 \text{ for } \tan \beta = 50, m_A < 500 \text{ GeV}$$

# Conclusions

\* In the MSSM with large  $\tan\beta$  and general flavor mixings for squarks, the gluino and  $H^\pm$  loops may give potentially sizable contributions, similar to the chargino contribution, through the  $b \rightarrow s\nu\bar{\nu}$  decays by  $bsZ$  penguin.

\* However, their magnitudes are strongly constrained by other FCNC processes of the b mesons,  $b \rightarrow s\gamma$ ,  $B_s - \bar{B}_s$  mixing,  $B_s \rightarrow \mu^+\mu^- \dots$

\* Requiring  $\Delta C_7(\text{gluino}) < C_7(\text{SM})$  and (Higgs penguin)  $<$  (Experimental deviation from SM) for  $B_s - \bar{B}_s$  mixing and  $B_s \rightarrow \mu^+\mu^-$  give strong constraints  $\Delta C_\nu^{(')}(\tilde{g}, H^\pm) \ll C_\nu(\text{SM})$ .