



University
ofGlasgow

Beyond DUNE and Hyper-Kamiokande: neutrino facilities from muon decay

Seminar, Kyoto University

29 November 2018

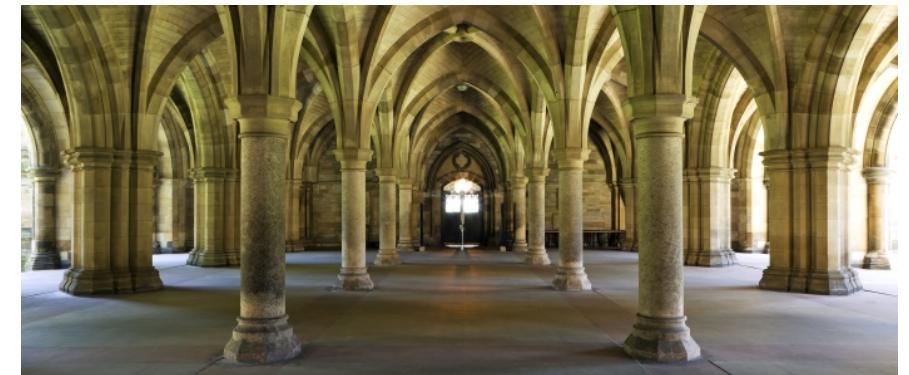
Paul Soler
University of Glasgow

University of Glasgow

- ❑ Nijo Castle: 1626



- ❑ University of Glasgow: 1451
4th oldest English-speaking university



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1. Physics Motivation

Neutrino mixing

- Weak eigenstates and mass eigenstates different:
Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \Rightarrow U = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix}$$

where $c_{ij} = \cos \theta_{ij}$, and $s_{ij} = \sin \theta_{ij}$

- Three mixing angles and one CP violating phase

$$U_{PMNS} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

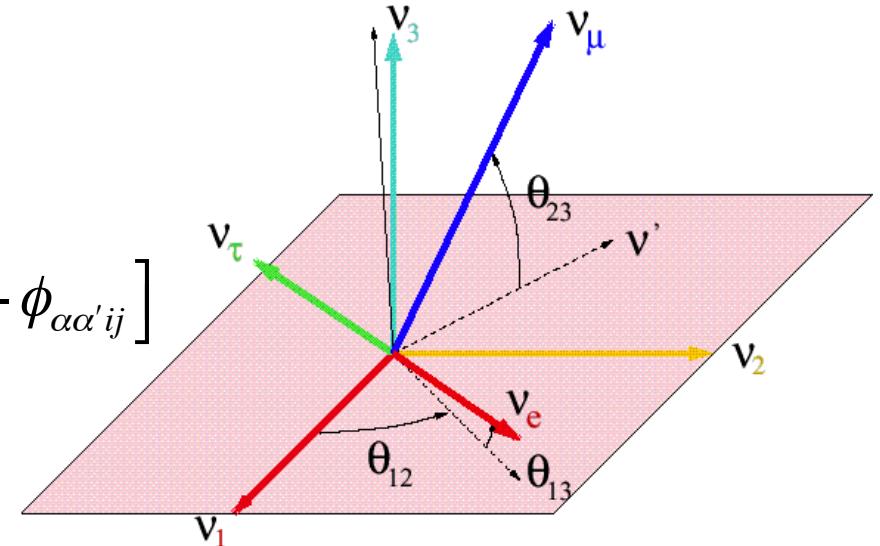
$$|\nu_\alpha\rangle = \sum_i U_{\alpha i} |\nu_i\rangle \text{ where } \alpha = e, \mu, \tau \text{ and } i = 1, 2, 3$$

Neutrino oscillations

- Three rotations in weak and mass eigenstate space

$$|\nu_\alpha(t)\rangle = e^{i\vec{p}\cdot\vec{r}} \sum_i e^{-iE_i t} U_{\alpha i} |\nu_i\rangle$$

$$P_{\nu_\alpha \rightarrow \nu_{\alpha'}}(t) = |\langle \nu_{\alpha'} | \nu_\alpha(t) \rangle|^2 = \\ \sum_{i,j} |U_{\alpha i} U_{\alpha' i}^* U_{\alpha j}^* U_{\alpha' j}| \cos[(E_i - E_j)t - \phi_{\alpha\alpha' ij}]$$



$$P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)}(x) = s_{23}^2 \sin^2 2\theta_{13} \sin^2 \left[\frac{\Delta m_{13}^2}{4E} x \right] + c_{23}^2 \sin^2 2\theta_{12} \sin^2 \left[\frac{\Delta m_{12}^2}{4E} x \right] + \\ + \tilde{J} \cos \left[\pm \delta - \frac{\Delta m_{13}^2}{4E} x \right] \left(\frac{\Delta m_{12}^2}{4E} x \right) \sin \left[\frac{\Delta m_{13}^2}{4E} x \right] \quad \text{with } \tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$$

Includes CP violation: neutrino/antineutrino oscillation difference if $\delta \neq 0$

Neutrino oscillations in matter

- ❑ Resonant neutrino oscillation in matter: MSW effect
 - Discriminates between normal and inverted mass hierarchy

$$P_{\nu_e \nu_\mu (\bar{\nu}_e \bar{\nu}_\mu)}(x) = P_1 + P_2 + P_3 + P_4$$

$$P_1 = s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{13}}{B_\mp} \right)^2 \sin^2 \left[\frac{B_\mp}{2} x \right]$$

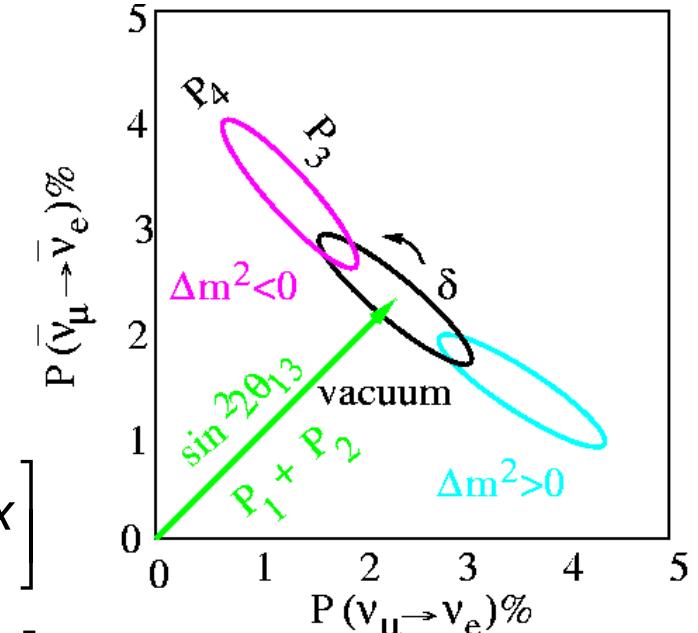
$$P_2 = c_{23}^2 \sin^2 2\theta_{12} \left(\frac{\Delta_{12}}{A} \right)^2 \sin^2 \left[\frac{A}{2} x \right]$$

$$P_3 = \tilde{J} \cos \delta \cos \left[\frac{\Delta_{13}}{2} x \right] \left(\frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\mp} \right) \sin \left[\frac{A}{2} x \right] \sin \left[\frac{B_\mp}{2} x \right]$$

$$P_4 = \pm \tilde{J} \sin \delta \sin \left[\frac{\Delta_{13}}{2} x \right] \left(\frac{\Delta_{12}}{A} \frac{\Delta_{13}}{B_\mp} \right) \sin \left[\frac{A}{2} x \right] \sin \left[\frac{B_\mp}{2} x \right]$$

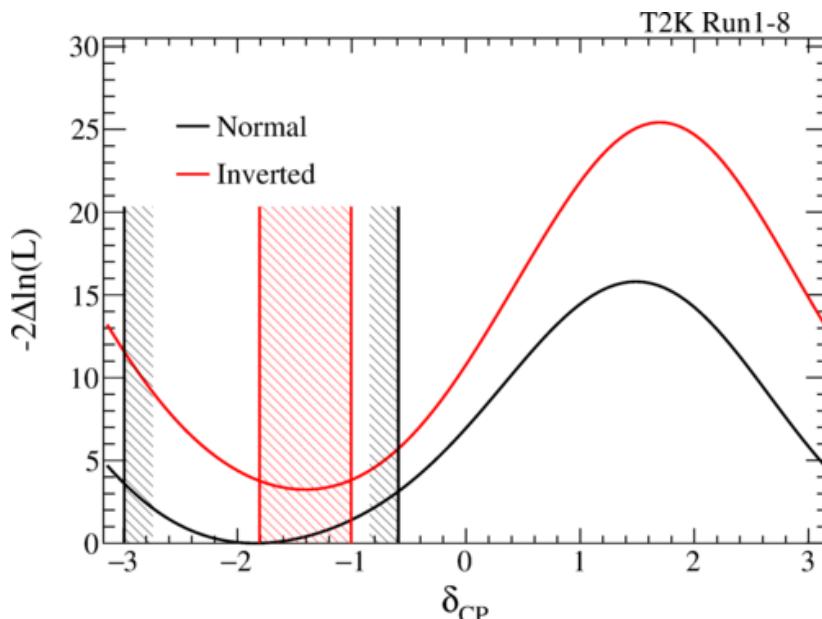
$$\Delta_{ij} \equiv \frac{\Delta m_{ij}^2}{2E} \quad A \equiv \sqrt{2G_F n_e} \quad \tilde{J} \equiv c_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$$

with $B_\mp \equiv \sqrt{(\Delta_{13} \cos 2\theta_{13} \mp A)^2 + \Delta_{13}^2 \sin^2 2\theta_{13}} \approx |\Delta_{13} \mp A|$

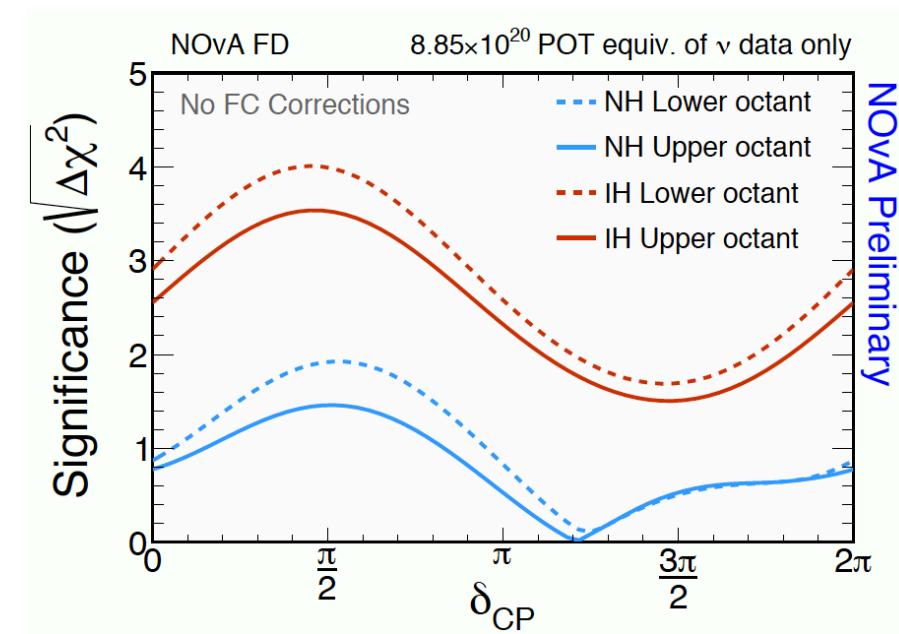


Next generation long-baseline experiments

- ❑ Main physics goals of long-baseline neutrino experiments are to observe CP violation in neutrinos and to determine neutrino mass ordering
- ❑ Both T2K and NOvA are exhibiting hints of CP violation in the neutrino sector at $\sim 2\sigma$ level



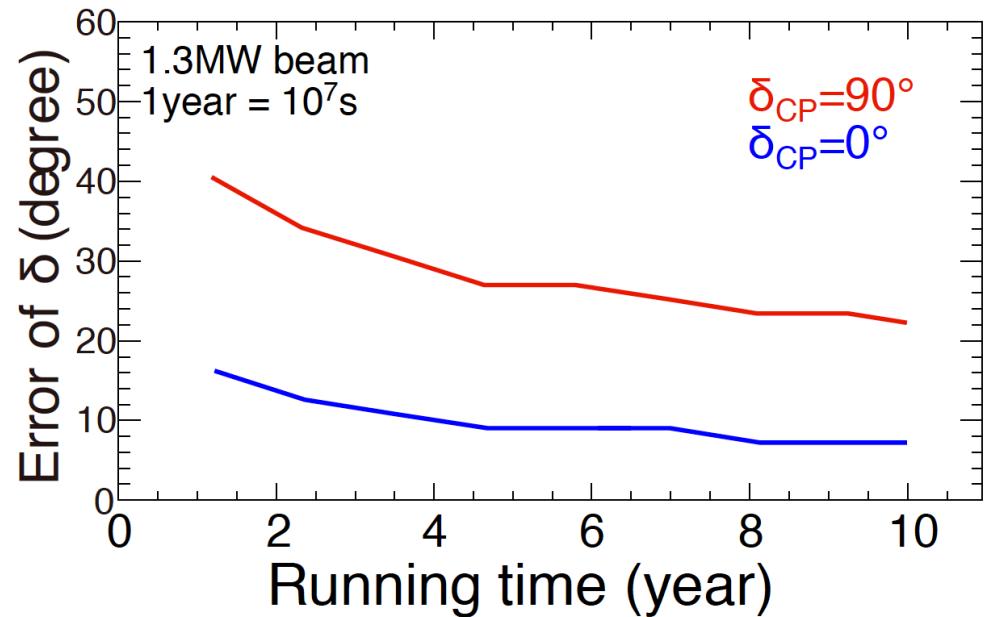
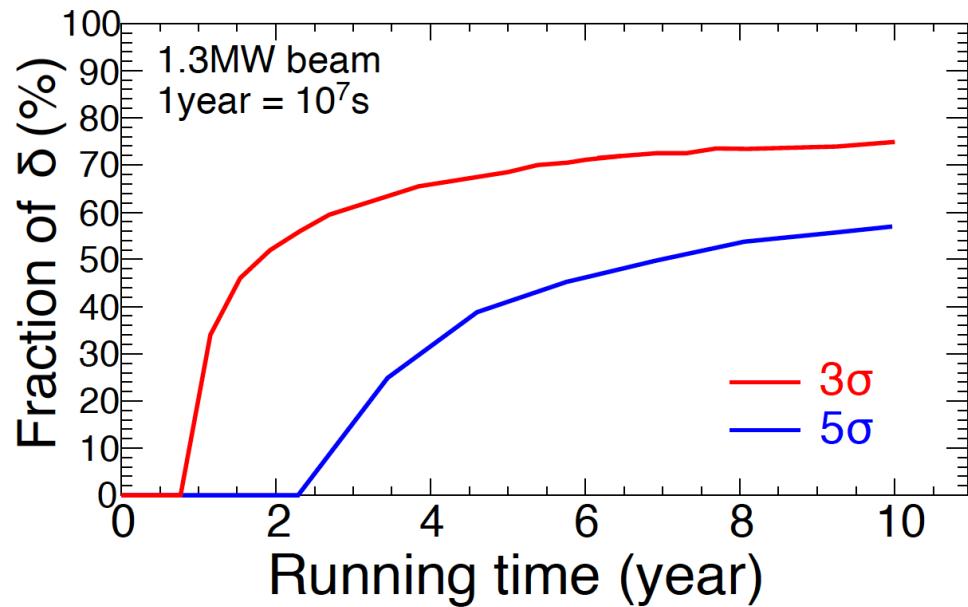
PRL, 121, 171802 (2018)



Neutrino 2018

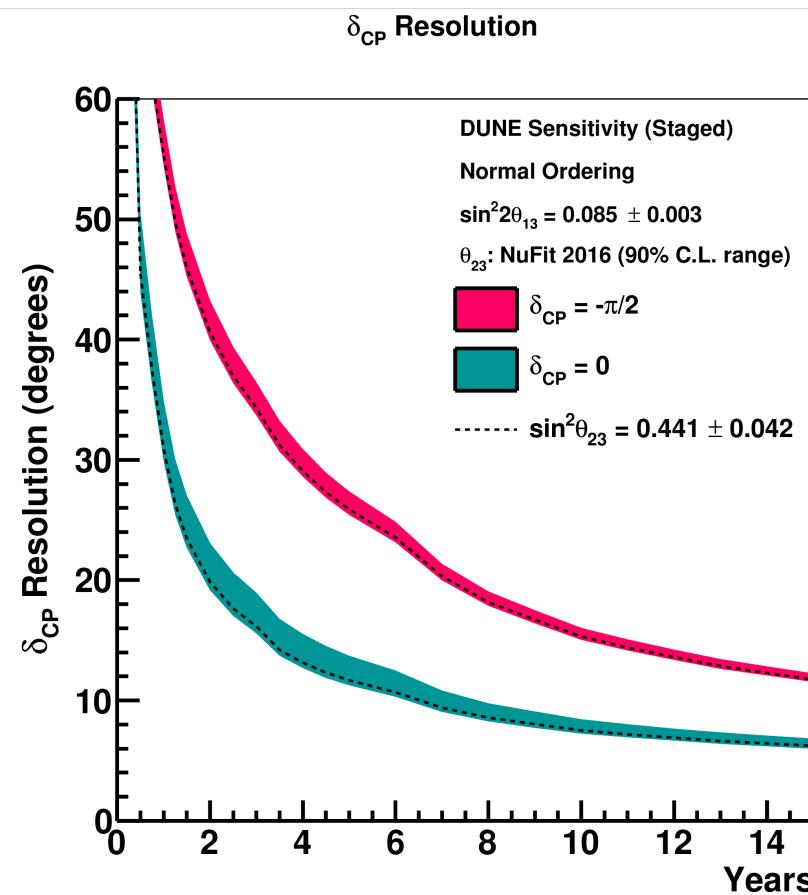
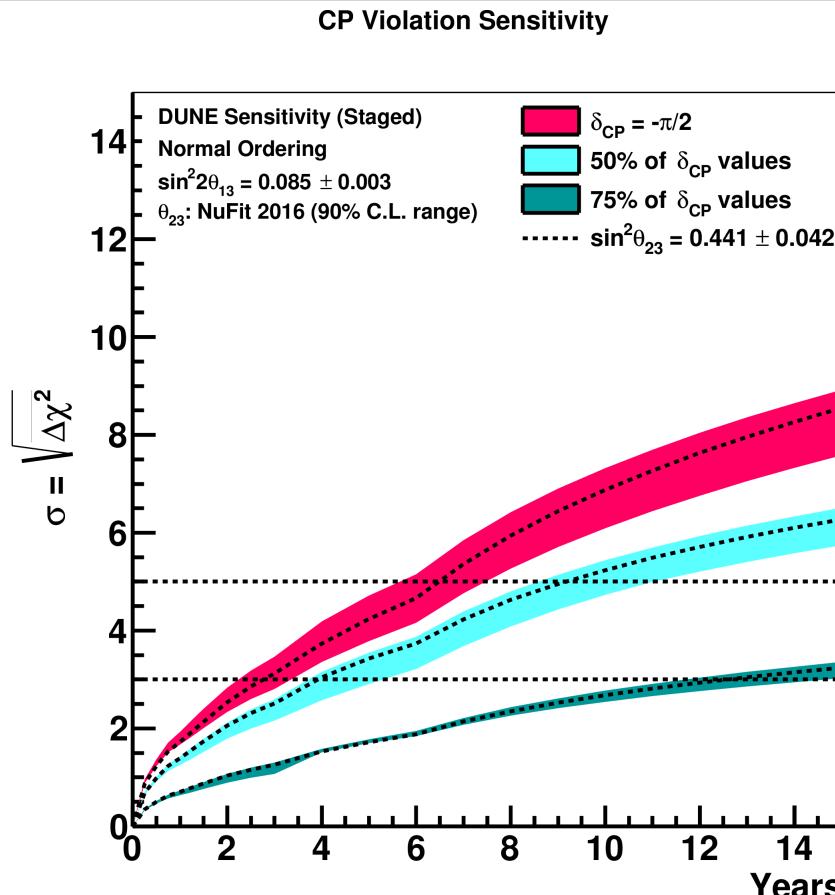
Next generation long-baseline experiments

- ❑ Require next generation experiments for 5σ results
- ❑ Hyper-K Design Report: [arXiv:1805.04163](https://arxiv.org/abs/1805.04163)
 - CP-violation accuracy: $\Delta\delta_{CP} \sim 23^\circ$ after 10 years for $\delta_{CP} = \pm 90^\circ$



Next generation long-baseline experiments

- ❑ Require next generation experiments for 5σ results
- ❑ DUNE Interim Design Report: [arXiv:1807.10334](https://arxiv.org/abs/1807.10334)
 - CP-violation accuracy: $\Delta\delta_{CP} \sim 15^\circ$ after 10 years for $\delta_{CP} = \pm 90^\circ$



Is discovering CP violation sufficient?

- ❑ Is discovering CP violation and determining the mass ordering sufficient or do we need more precision?
- ❑ We want to test the Standard Neutrino Model, the three-neutrino paradigm and search for new physics
- ❑ Compare PMNS mixing matrix to models:

$$U_{PMNS} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

where $c_{ij} = \cos \theta_{ij}$ and $s_{ij} = \sin \theta_{ij}$

$$U_{PMNS} = \begin{pmatrix} \sqrt{2/3} & 1/\sqrt{3} & 0 \\ -1/\sqrt{6} & 1/\sqrt{3} & 1/\sqrt{2} \\ 1/\sqrt{6} & -1/\sqrt{3} & 1/\sqrt{2} \end{pmatrix}$$

$\theta_{12} = \sin^{-1}(1/\sqrt{3}) \sim 35.3^\circ$, $\theta_{23} = 45^\circ$, $\theta_{13} = 0$, $\delta = 0$

Harrison, Perkins, Scott PLB 530 (2002), 167

Tri-bimaximal mixing: suggestive of a broken flavour symmetry

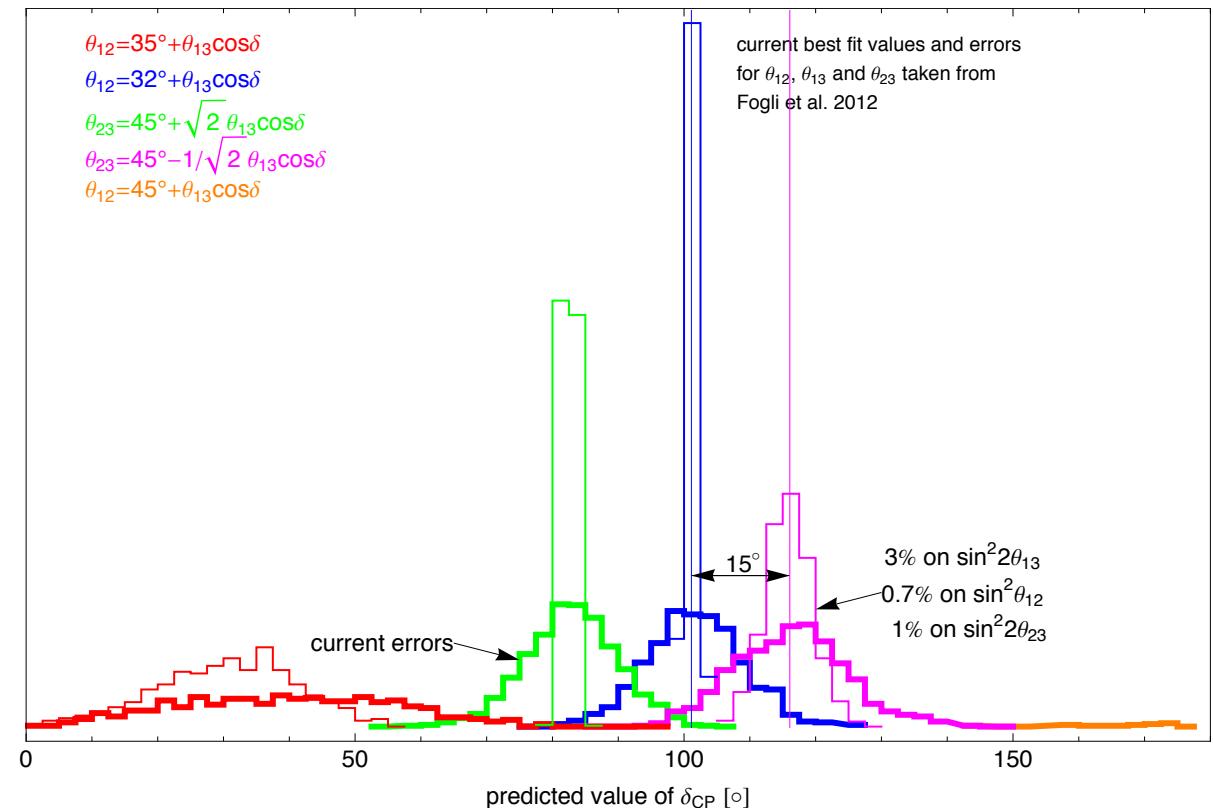
Is discovering CP violation sufficient?

- ❑ What precision is required to search for mechanism behind the generation of neutrino masses?
 - In quark sector, precision around 5°
 - Flavour sum rules:
Accuracy required $\sim 5^\circ$

ie. deviation of mixing angles from tri-bimaximal mixing:

$$\theta_{12} - \theta_{13} \cos \delta = \sin^{-1} \left(\frac{1}{\sqrt{3}} \right)$$

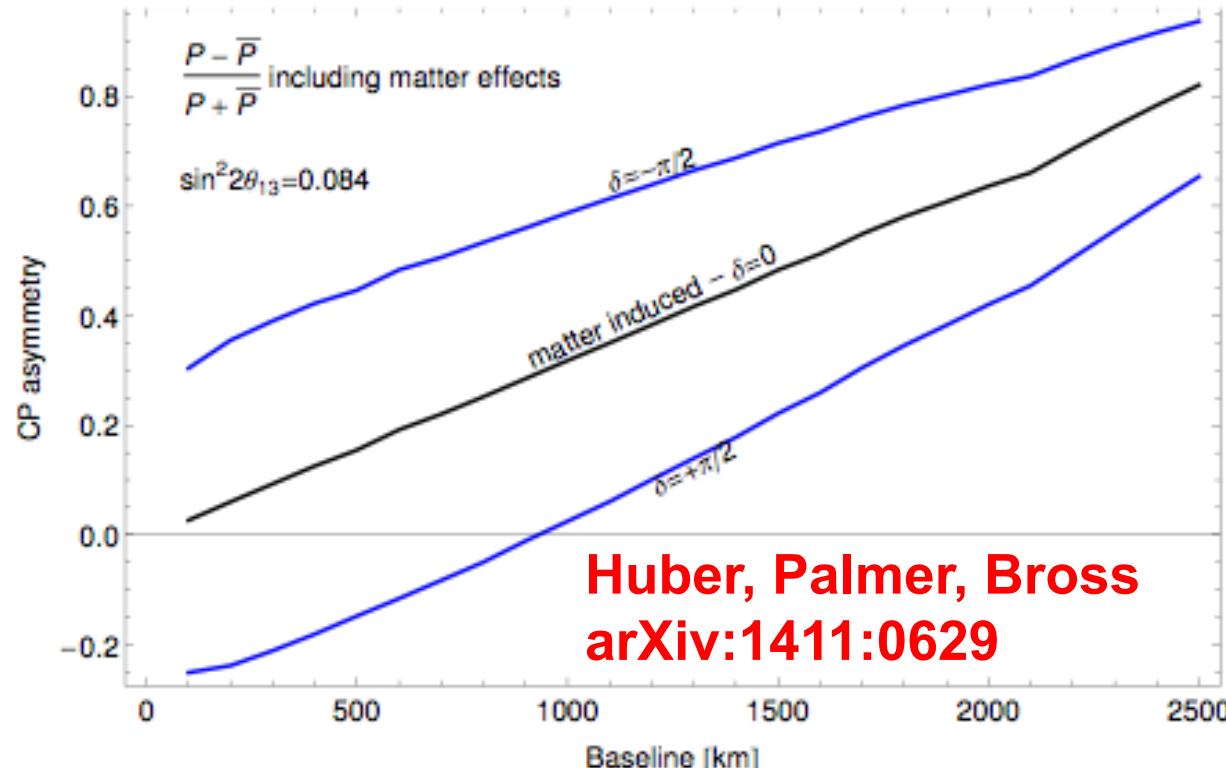
Comprehensive review:
King, Luhn, Rep. Prog. Phys. 76 (2013) 056201



Precision of long-baseline experiments

- ❑ Precision requirement for CP violation:
 - For 75% of CP asymmetry coverage at 3σ : A_{CP} as low as 5%
 - Requires 1.5% measurement of $P - \bar{P}$ ($\sim 1\%$ syst. error), but we measure rate:

$$R_{\alpha\beta}(E_{vis}) = N \int dE \Phi_\alpha(E) \sigma_\beta(E, E_{vis}) \epsilon_\beta(E) P(\nu_\alpha \rightarrow \nu_\beta, E)$$



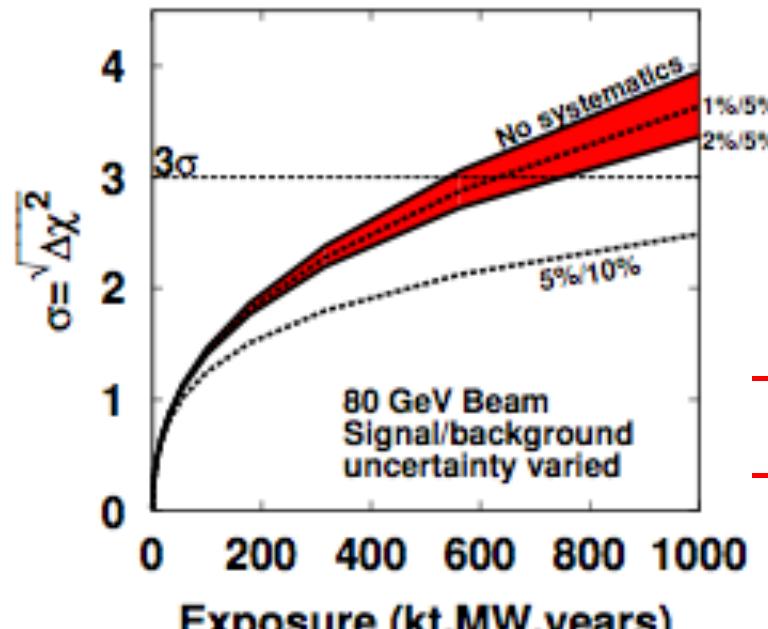
Precision of long-baseline experiments

- ❑ Precision requirement for CP violation:

- In disappearance experiment we can satisfy:

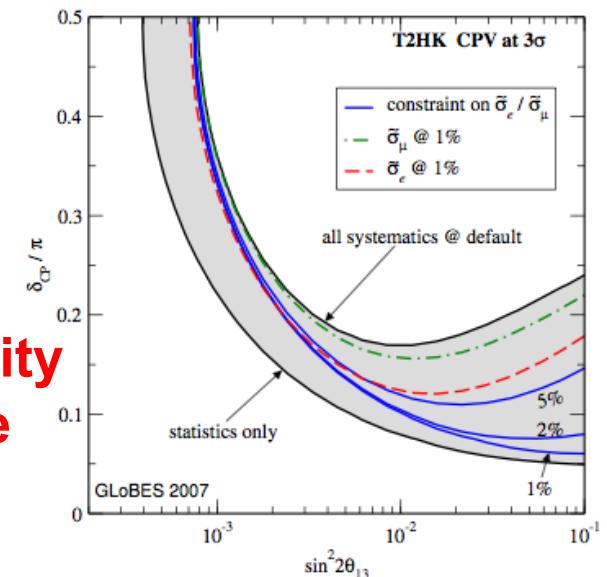
$$\frac{R_{\alpha\beta}(\text{far})L^2}{R_{\alpha\beta}(\text{near})} = \frac{N_{\text{far}}\Phi_\alpha\sigma_\beta\varepsilon_\beta P(\nu_\alpha \rightarrow \nu_\beta)}{N_{\text{near}}\Phi_\alpha\sigma_\alpha\varepsilon_\alpha 1} \quad \alpha = \beta$$

- In an appearance experiment $\alpha \neq \beta$, so ν_α beam cannot measure $\sigma_\beta\varepsilon_\beta$



**CP violation sensitivity
for 75% δ_{CP} coverage
at LBNE**

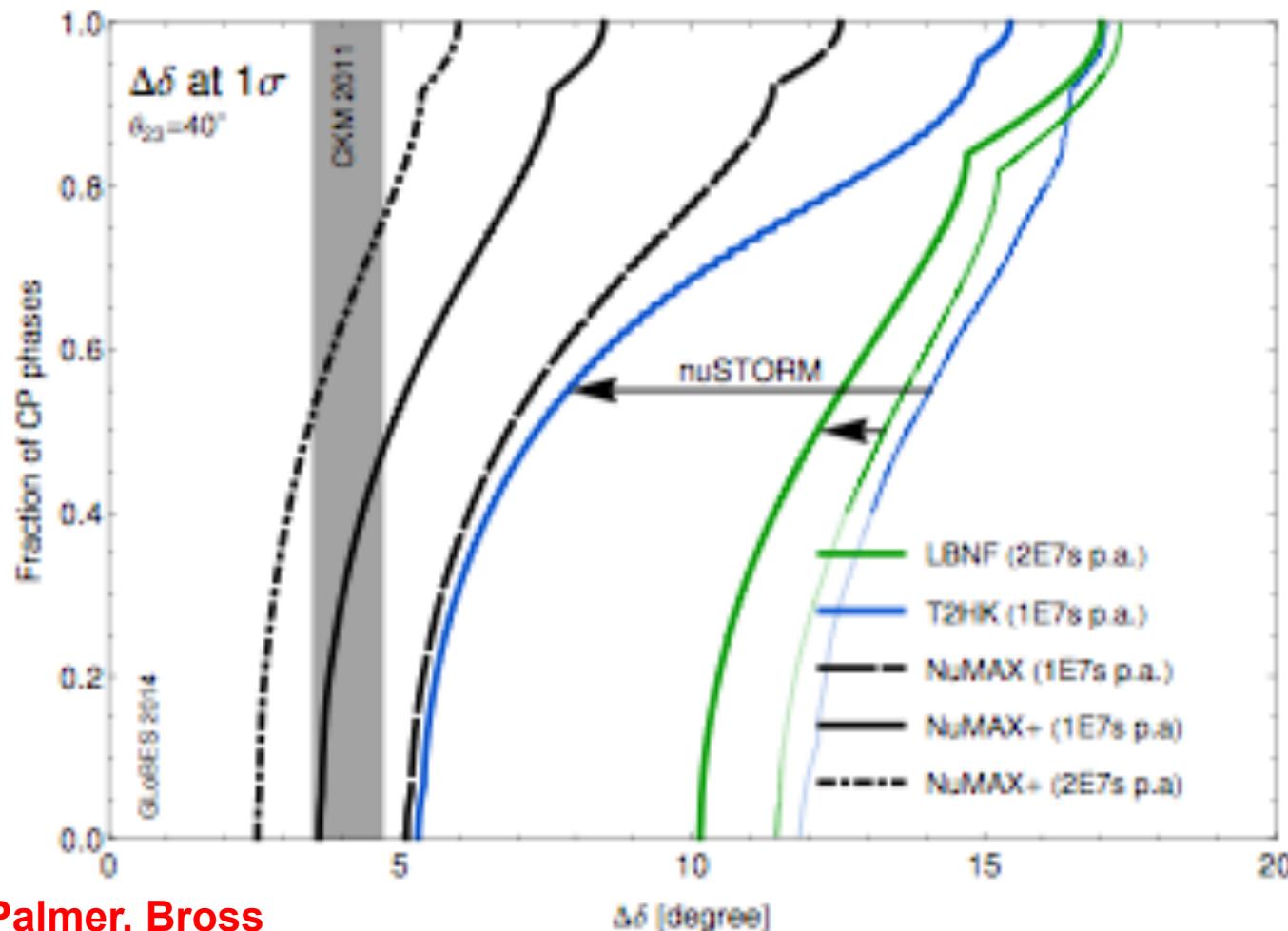
Huber, Mezzetto, Schwetz
arXiv:0711.2950



- Syst. error on ratio $\sigma_{\nu_e}/\sigma_{\nu_\mu}$ in T2HK
 - Difference in σ_{ν_μ} and σ_{ν_e} may be large

Precision of long-baseline experiments

- Influence of measurement of neutrino cross-sections with less than 1% precision (nuSTORM has that capability):



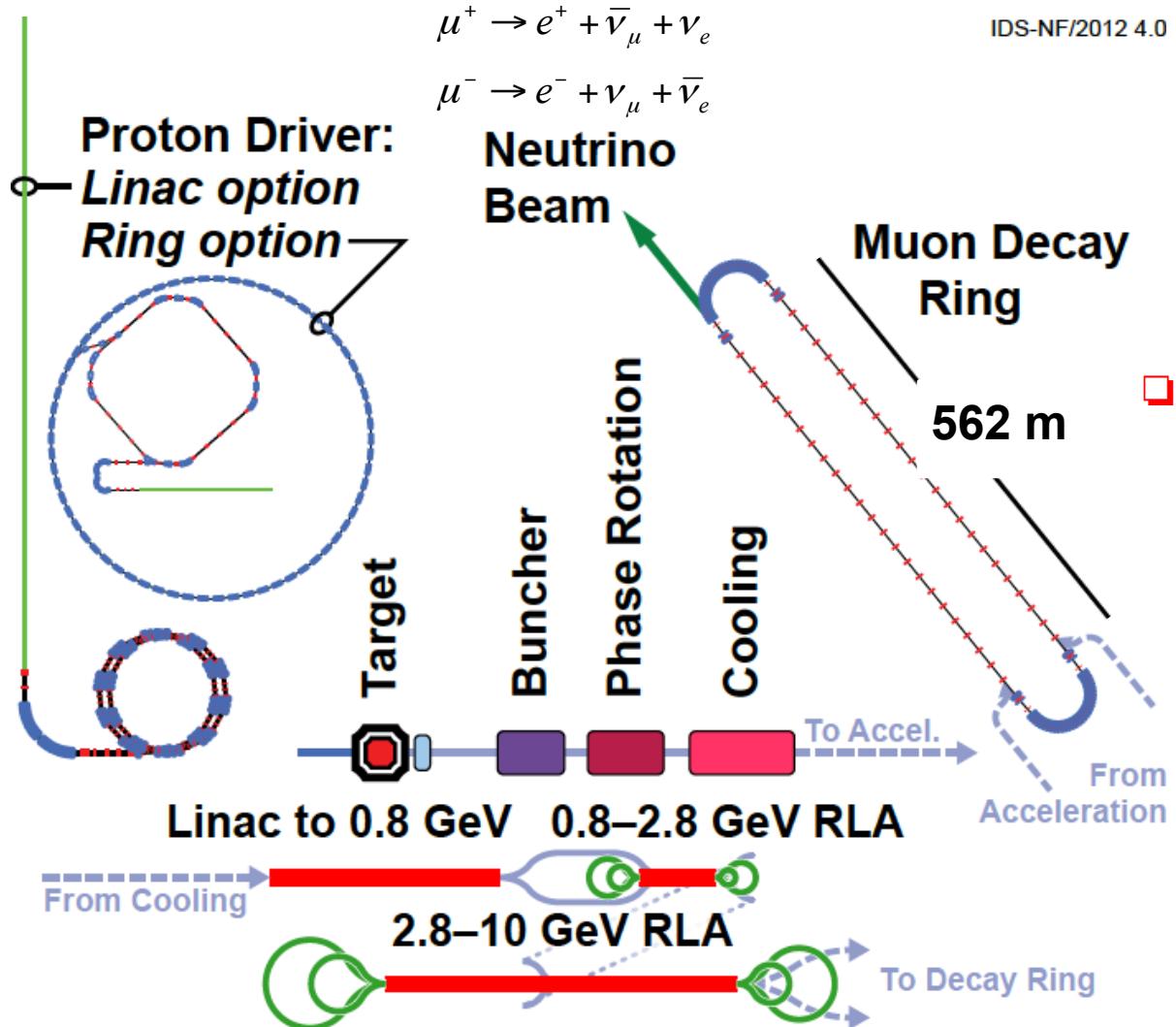
2. Neutrino Factory

Neutrino Factory Studies

- ❑ A Neutrino Factory is a neutrino beam facility from muon decay delivering 10^{21} muon decays per year
- ❑ Birth of modern Neutrino Factory:
 - S. Geer: Phys Rev D57, 6989 (1998)
- ❑ Neutrino Factory studies:
 - CERN study: CERN Yellow Report 99-02 (1999)
 - Feasibility Study I at Fermilab: Fermilab-Pub-00/108-E (2000)
 - Feasibility Study II at Brookhaven: BNL-52623 (2001)
 - Feasibility Study IIa at Brookhaven: BNL-72369 (2004)
 - International Design Study: Interim Design Report 2011
IDS-NF-020 arXiv:1102.2402
 - Muon Accelerator Staging Scenarios: launched by Muon Accelerator Programme (MAP) in USA 2013 (arXiv:1308.0494)

Neutrino Factory Baseline

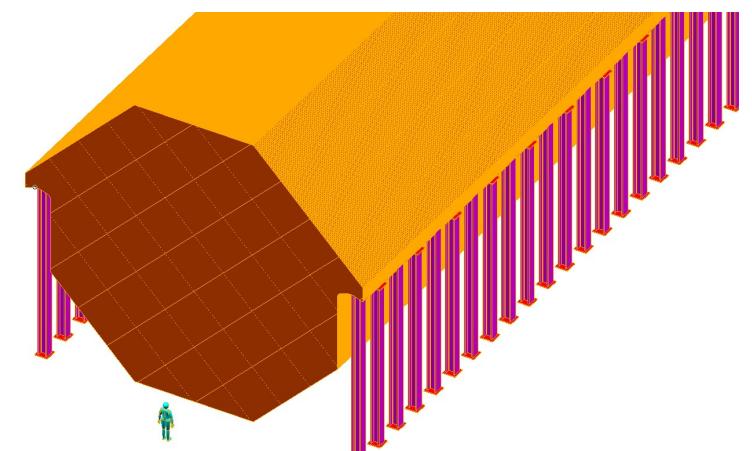
- ❑ International Design Study for a Neutrino Factory (IDS-NF)



IDS-NF/2012 4.0

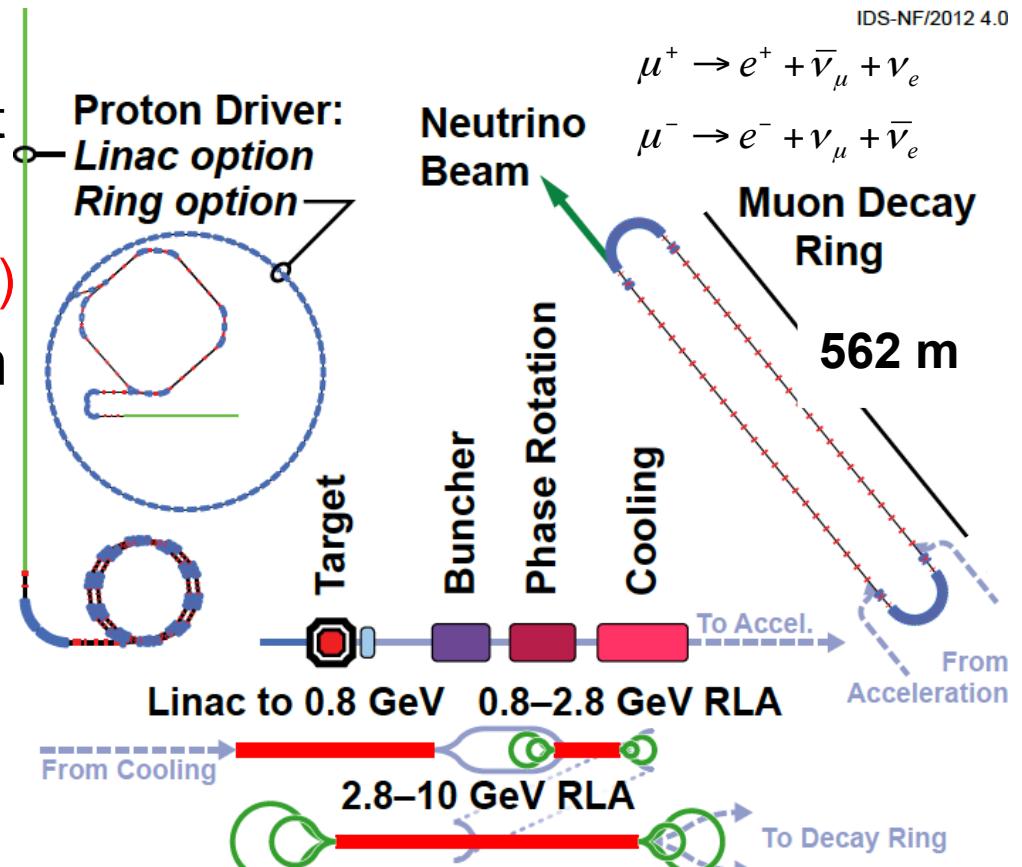
Baseline reviewed 2012:
from 25 GeV to 10 GeV muons
(v4.0), one storage ring with
detector at 2000 km, after
discovery that θ_{13} is large

- ❑ Magnetised Iron Neutrino Detector (MIND):
 - 100 kton at ~2000 km

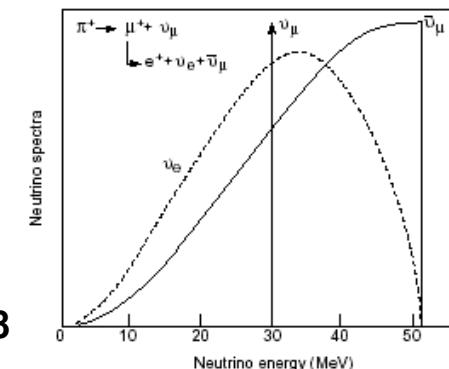


Neutrino Factory Baseline

- ❑ Proton driver
 - Proton beam ~8 GeV on target
- ❑ Target, capture and decay
 - Create π , decay into μ (MERIT)
- ❑ Bunching and phase rotation
 - Reduce ΔE of bunch
- ❑ Ionization Cooling
 - Reduce transverse emittance (MICE)
- ❑ Acceleration
 - 120 MeV \rightarrow 10 GeV with RLAs
 - FFAG option now not favoured
- ❑ Decay ring
 - Store for ~100 turns
 - Long straight sections
 - 10^{21} muons/year

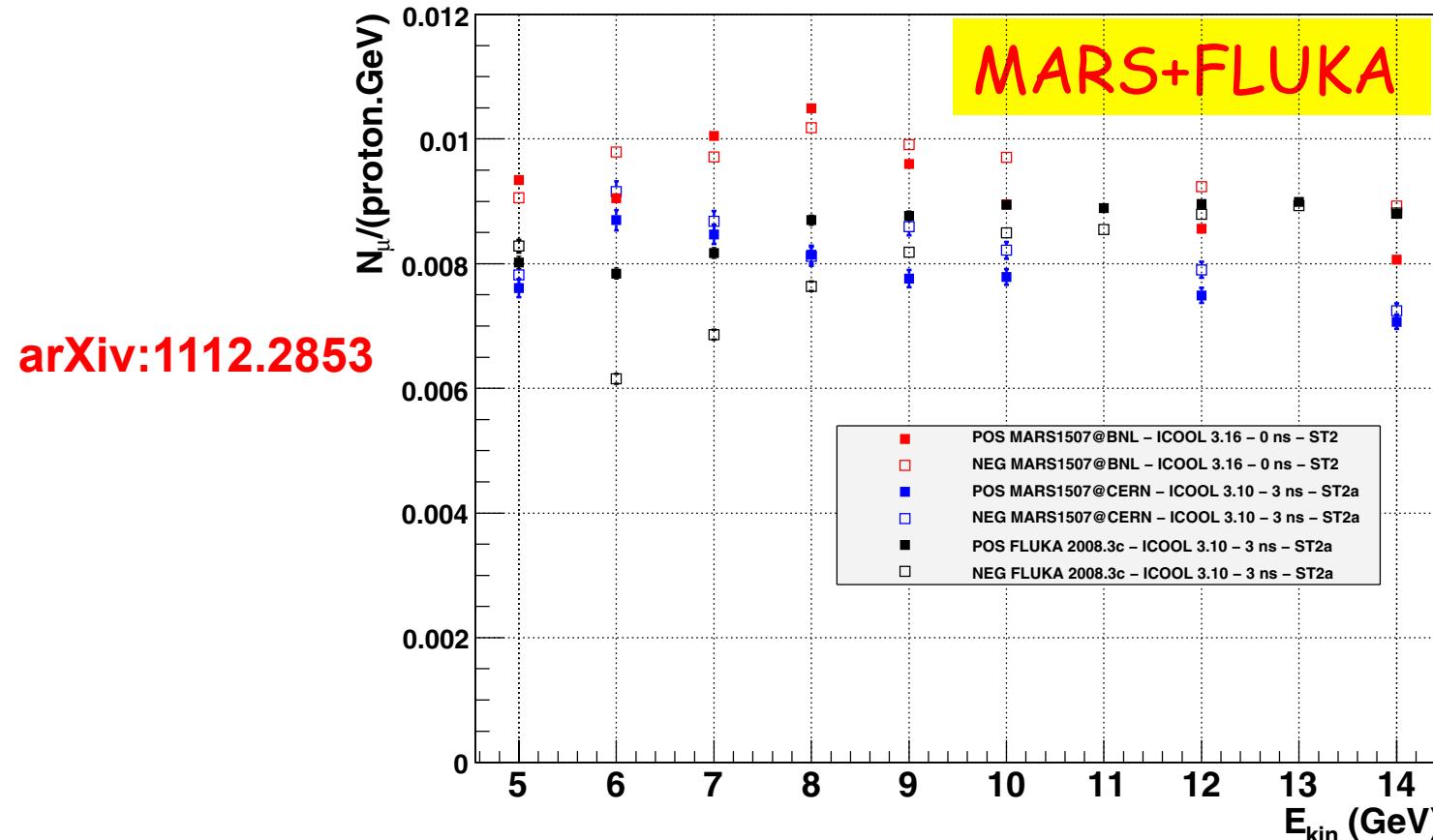


Neutrino spectra
calculable to high
accuracy



Optimum energy proton driver

- ❑ Optimum beam energy
 - Depends on choice of target
 - Optimum energy for high-Z targets around 8 GeV
 - Results validated by HARP hadron production experiment



Proton Driver

❑ Requirements:

[arXiv:1112.2853](#)

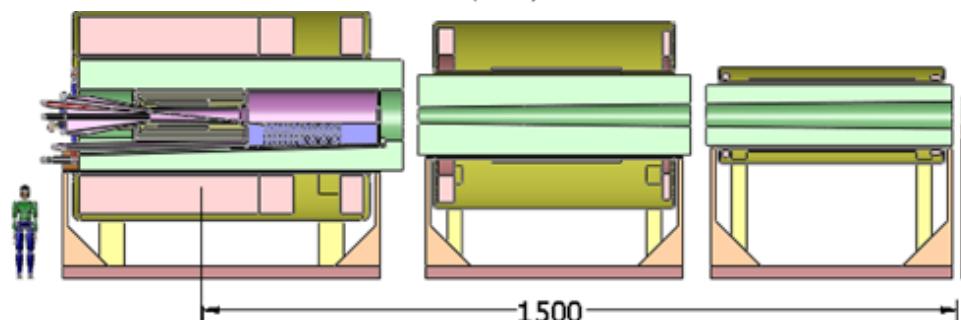
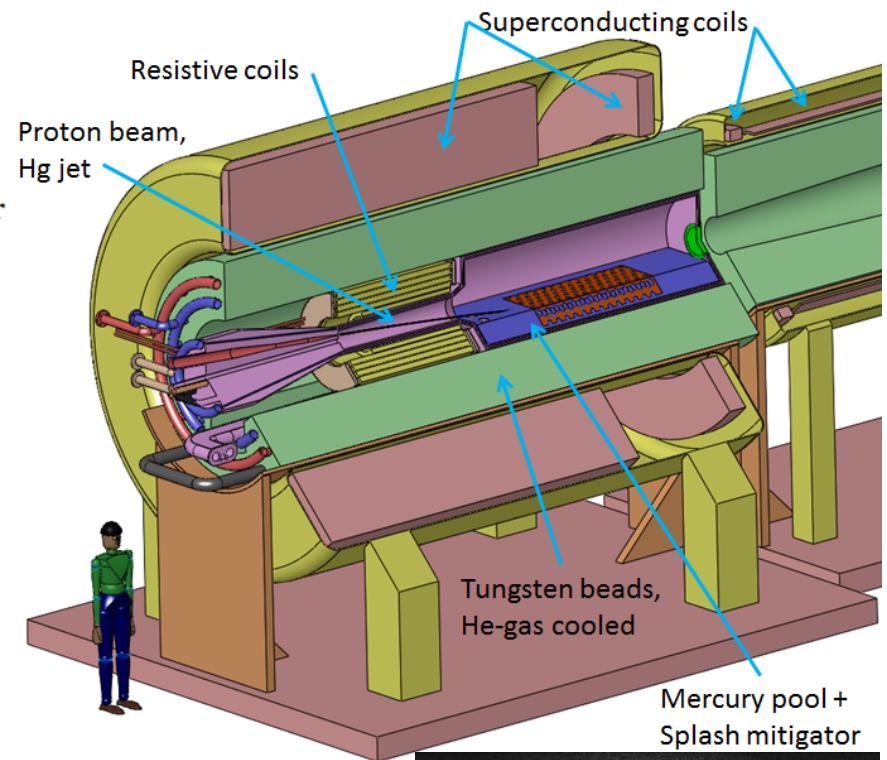
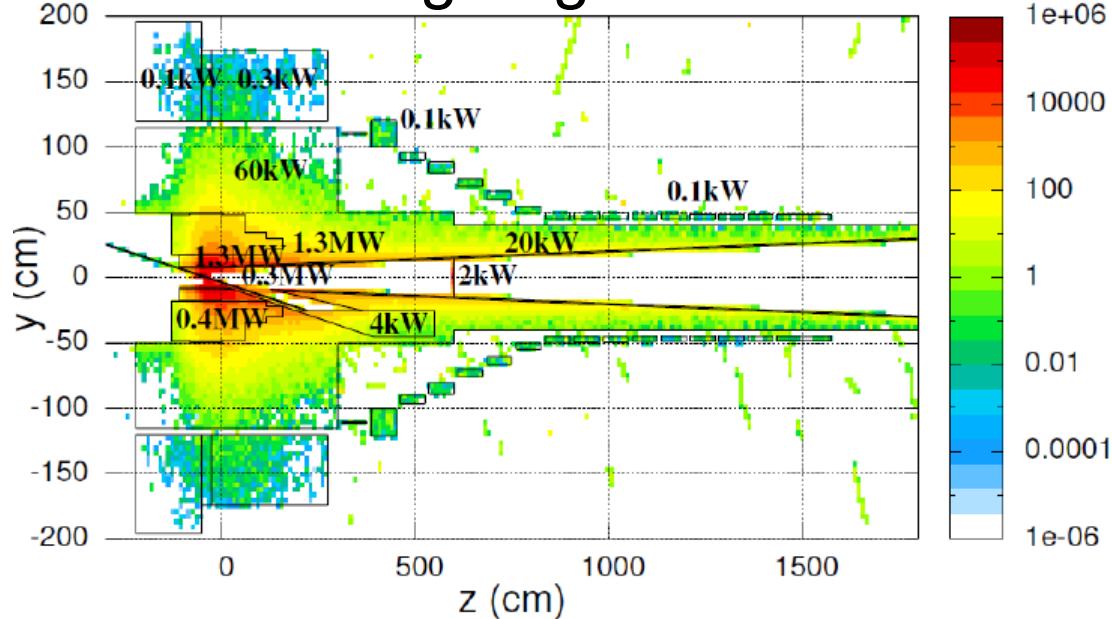
Parameter	Value
Kinetic energy	5–15 GeV
Average beam power $(3.125 \times 10^{15} \text{ protons/s})$	4 MW
Repetition rate	50 Hz
Bunches per train	3
Total time for bunches	240 μs
Bunch length (rms)	1–3 ns
Beam radius	1.2 mm (rms)
Rms geometric emittance	< 5 μm
β^* at target	$\geq 30 \text{ cm}$

❑ Choice of proton driver depends on site:

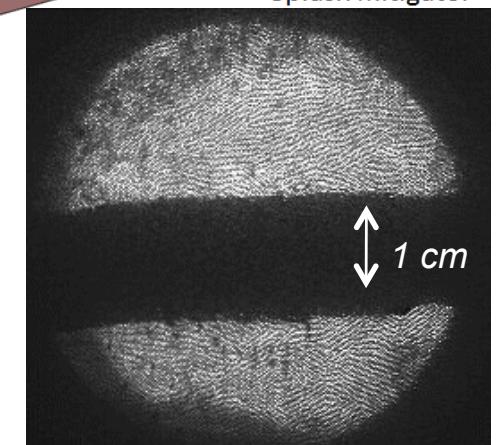
- LINAC based (SPL) proton driver at CERN
- Synchrotron(s)/FFAG based proton driver (green field solution) – studied at RAL.
- PIP-2 LINAC based solution at Fermilab.

Target

- ❑ Liquid Hg target in 20 T solenoid
- ❑ Increased radiation shielding in surrounding target solenoid



Target station & decay channel



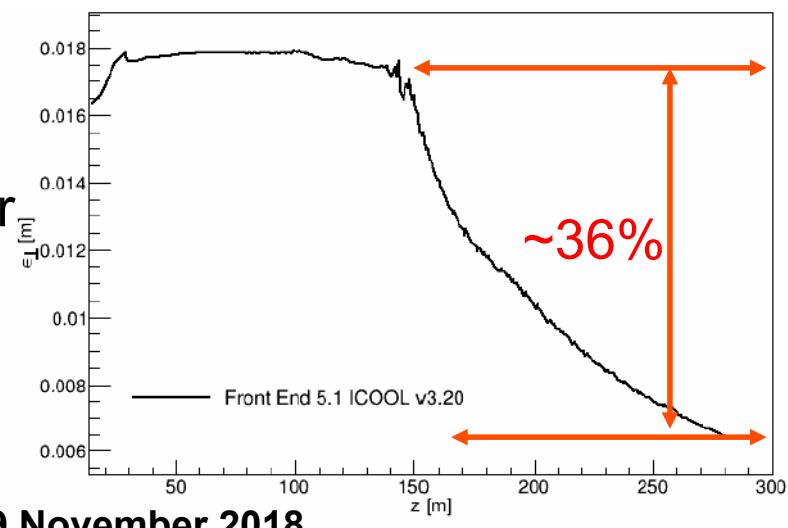
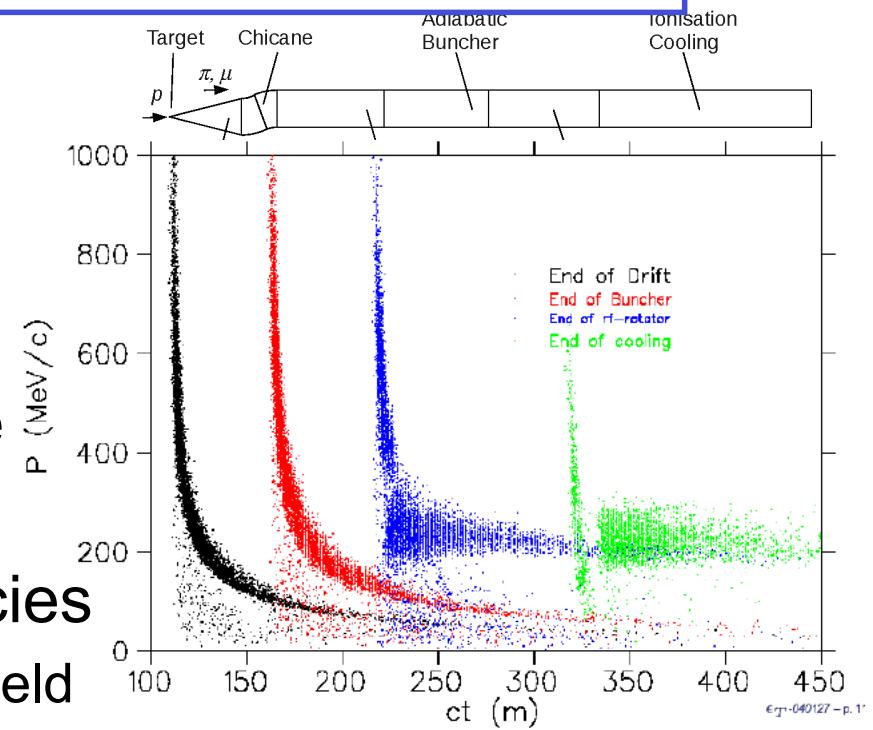
Seminar, Kyoto University: 29 November 2018

MERIT

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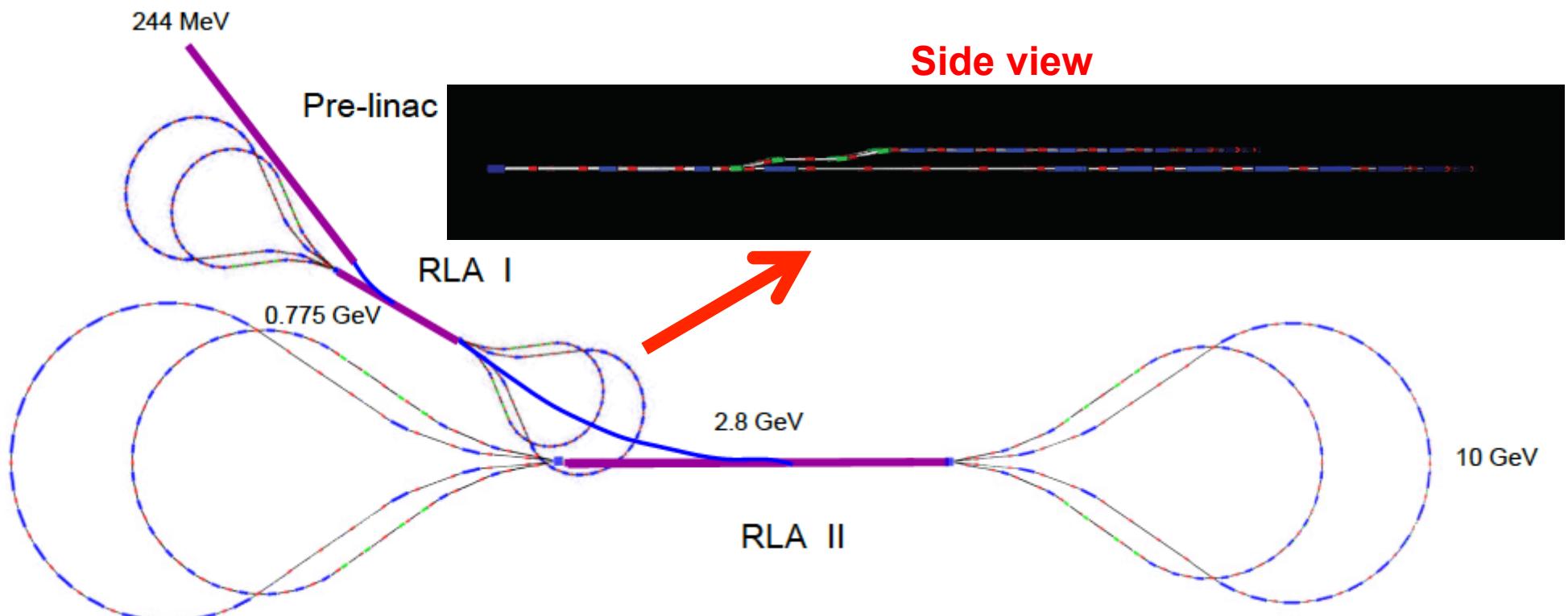
Muon Front End

- ❑ Adiabatic B-field taper from Hg target to longitudinal drift
- ❑ Add chicane to remove protons
- ❑ Drift in ~ 1.5 T, ~ 60 m solenoid
- ❑ Adiabatically bring on RF voltage to bunch beam
- ❑ Phase rotation: variable frequencies
 - High energy front sees negative E-field
 - Low energy tail sees positive E-field
 - End up with smaller energy spread
- ❑ Ionization Cooling: MICE demonstrator
 - Reduce transverse emittance by 36%
 - Performance: $0.066 \mu/\text{proton}$
 - Cooling increases muon yield by ~ 2.2



Acceleration

- ❑ Baseline acceleration scheme at 10 GeV
 - Two “dog-bone” Recirculating Linear Accelerators (RLA)
 - First RLA up to 2.8 GeV
 - Second RLA up to 10 GeV

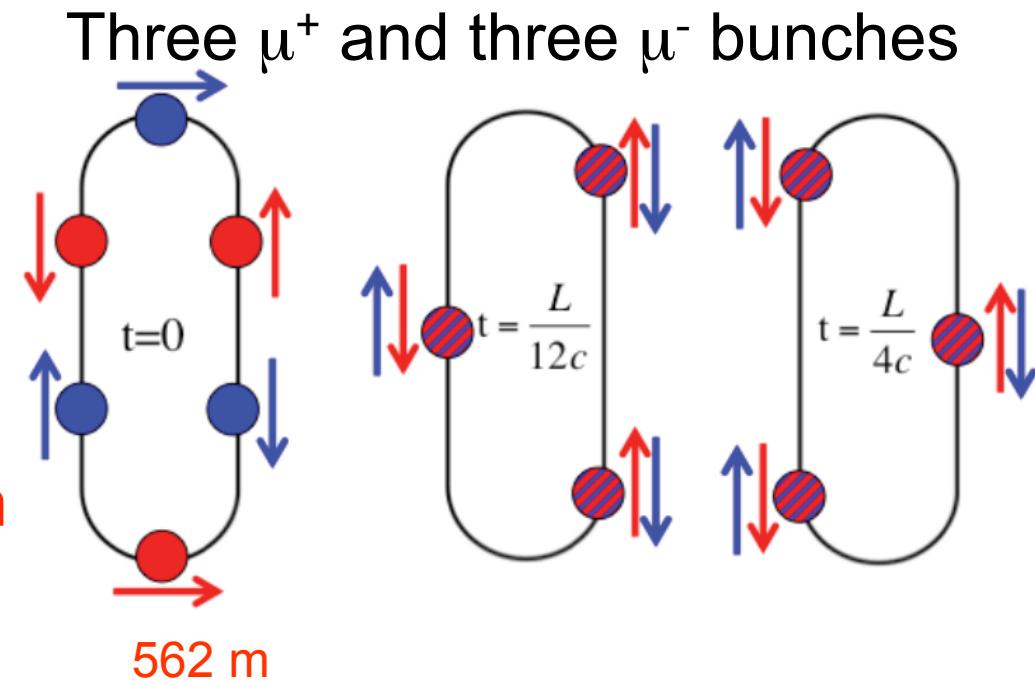


Decay Ring Geometry

- ❑ Racetrack geometry for decay ring with insertion

- Straight: 562 m
- Upper arc: 121 m
- Lower arc: 113 m
- Insertion: 46 m
- Matching: 105 m (total)

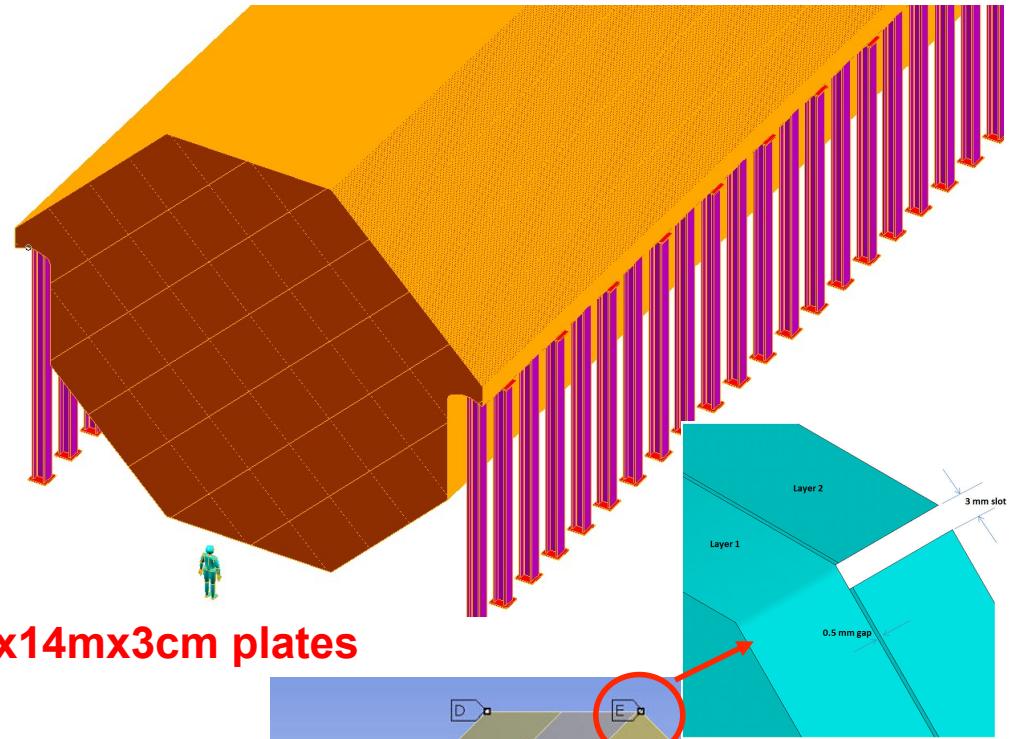
➔ Circumference = 1556 m



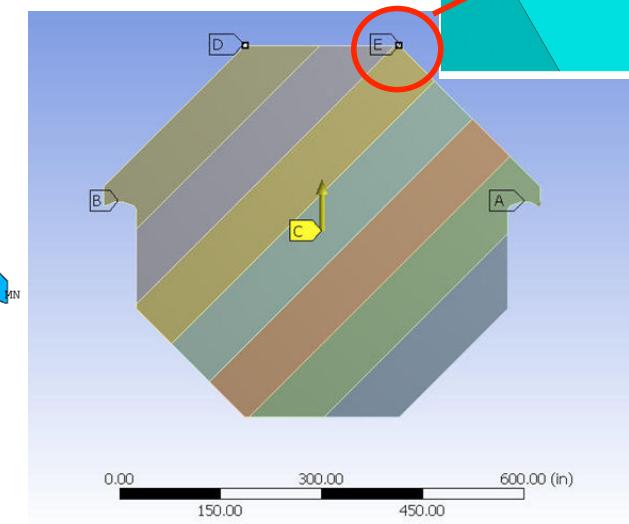
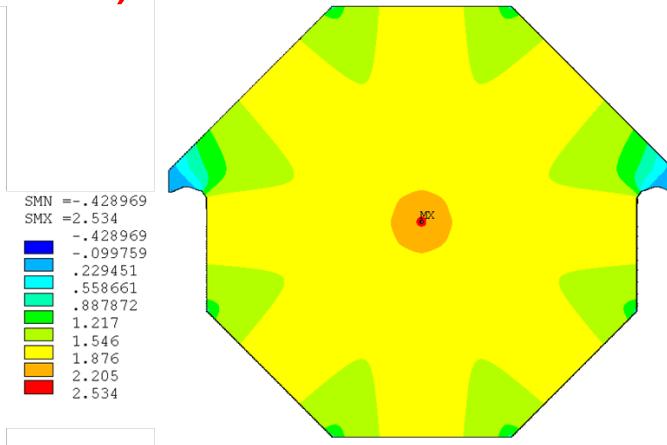
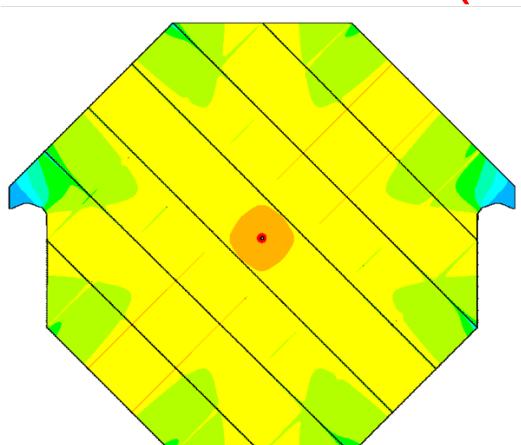
Divergence $< 0.1/\gamma$

Far Detector

- ❑ Magnetised Iron neutrino Detector (MIND): 100 kton
- ❑ Octagonal plates and toroidal field (as in MINOS)
- ❑ Engineering metal plates
- ❑ Magnetic field delivered by 100 kA current



Bross, Wands (FNAL)

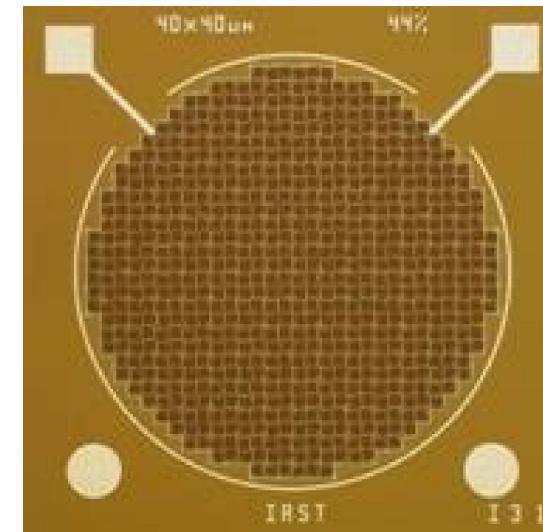
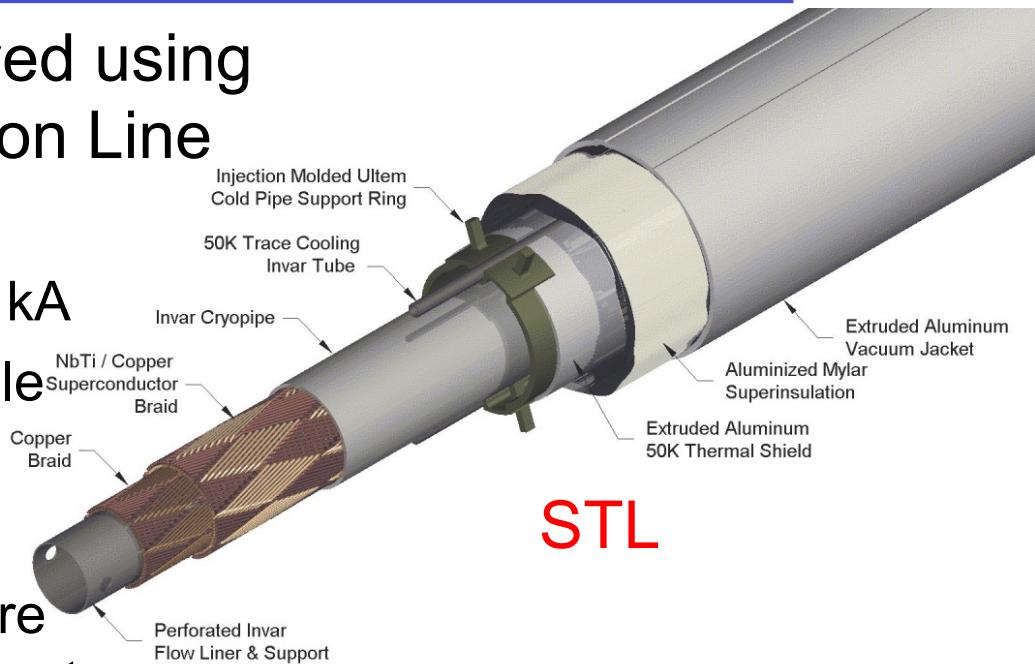
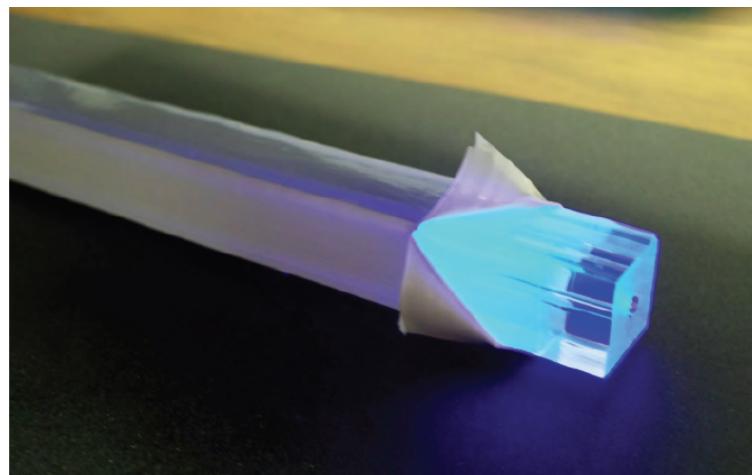


MIND magnetisation

- ❑ Magnetisation can be achieved using Superconducting Transmission Line (STL) developed for VLHC:

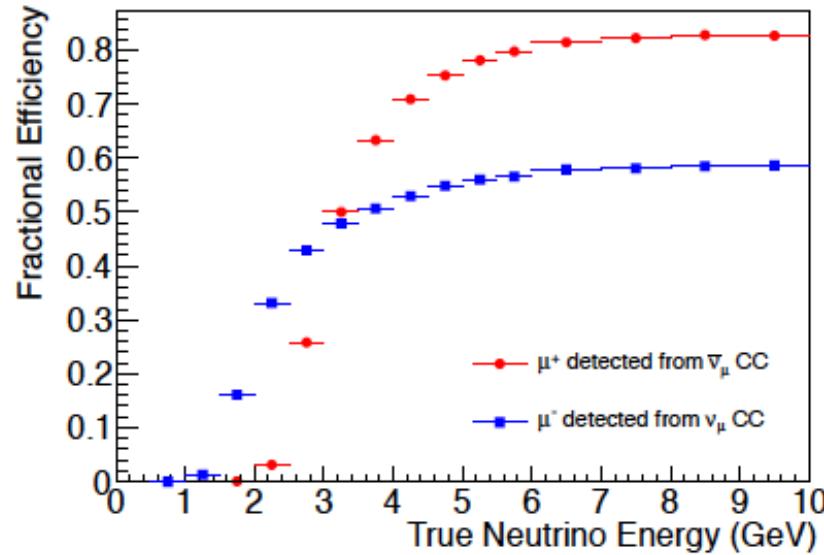
- Either one 100 kA turn or 8x15 kA
- Only need ~10 cm diameter hole

- ❑ Extruded scintillator:
 - Kuraray wavelength shifting fibre with double-ended SiPMT readout

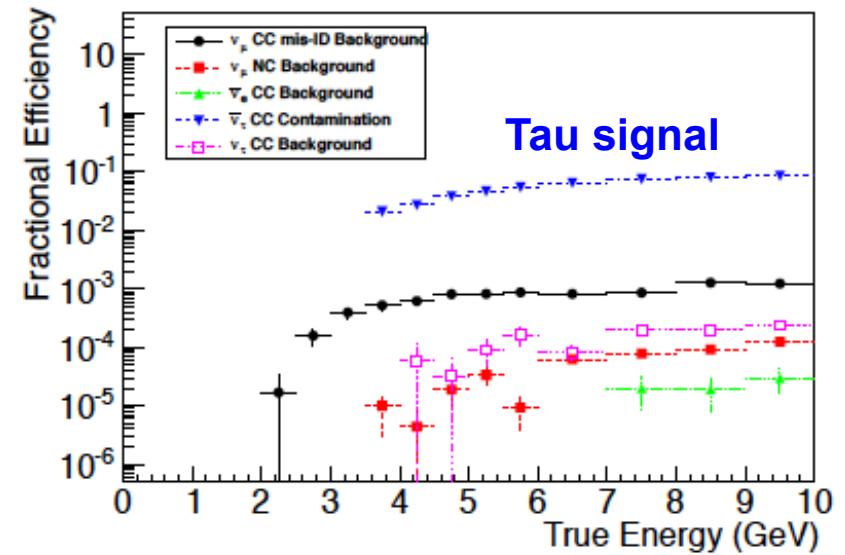


MIND efficiencies and background

BDT efficiency, focussing μ^+

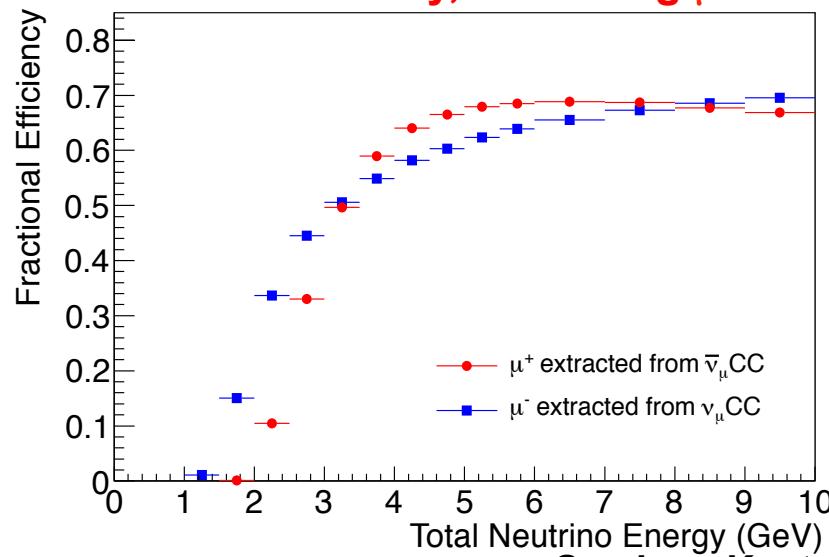


BDT background (stored μ^- , focussing μ^+)

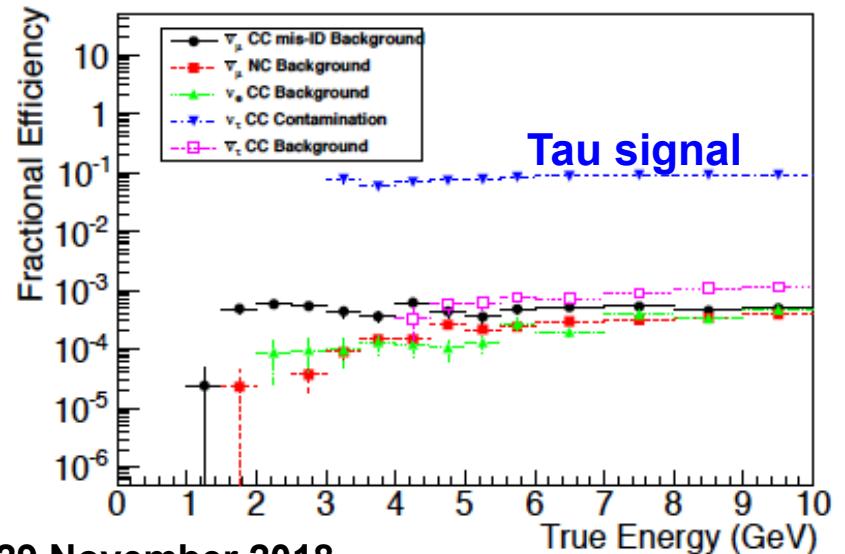


Courtesy
R. Bayes
UofG

BDT efficiency, focussing μ^-

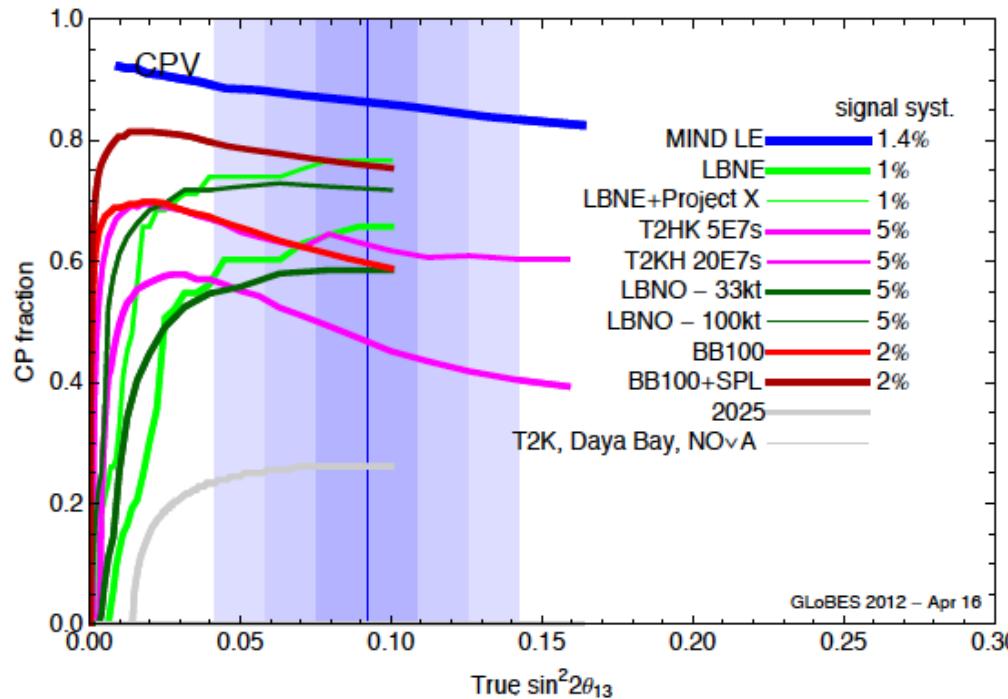


BDT background (stored μ^+ , focussing μ^+)

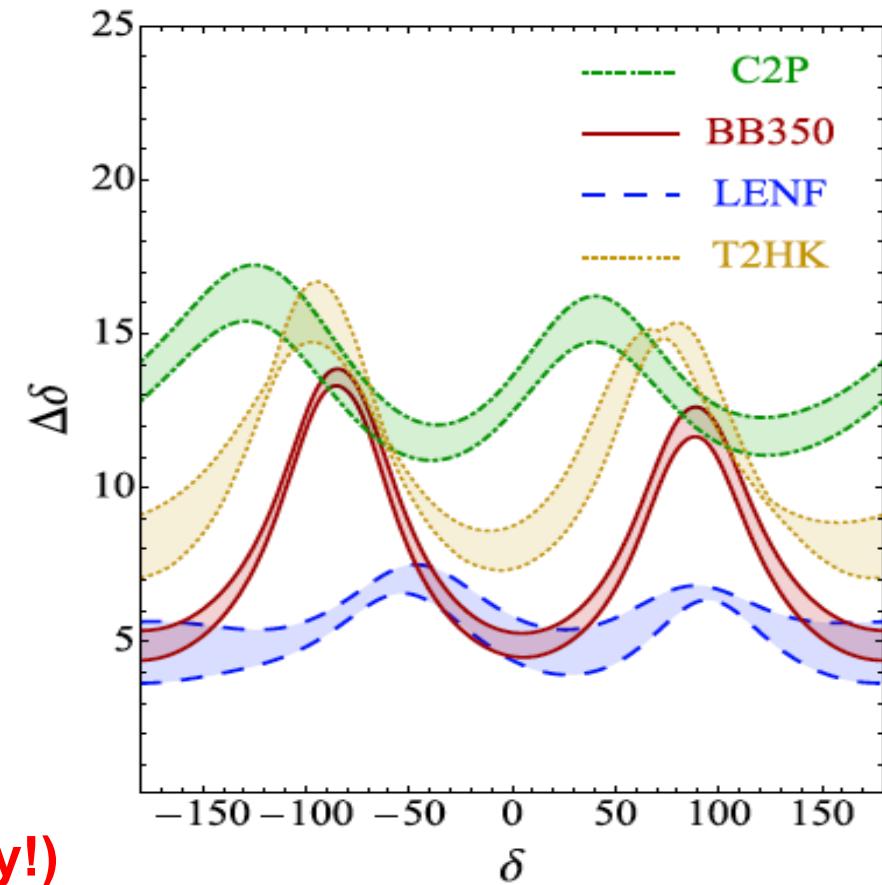


Performance 10 GeV Neutrino Factory

- ❑ Optimisation for 10 GeV Neutrino Factory, $10^{21} \mu/\text{year}$ with 100 kton MIND at 2000 km gives best sensitivity to CP violation
- ❑ Best possible performance for a Neutrino Factory: $\Delta\delta_{\text{CP}} \sim 5^\circ$



**More than 85% 5σ coverage
(ie. 85% probability of CPV discovery!)**



arXiv:1203.5651

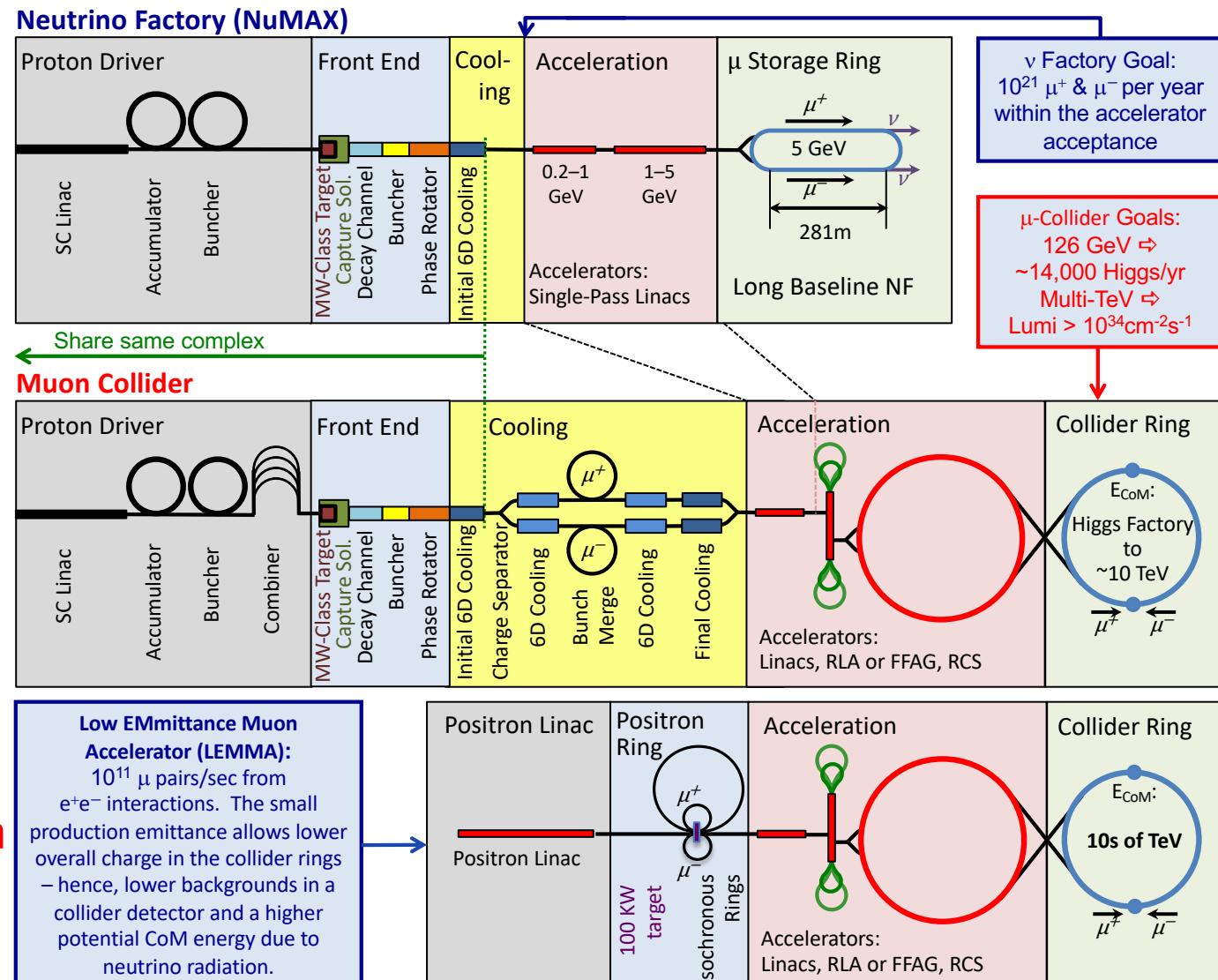
3. Neutrino Factory Staging

Muon Accelerator Staging Programme

- Staging Neutrino Factory allows to produce physics at each stage and spreads out cost – first step towards muon collider

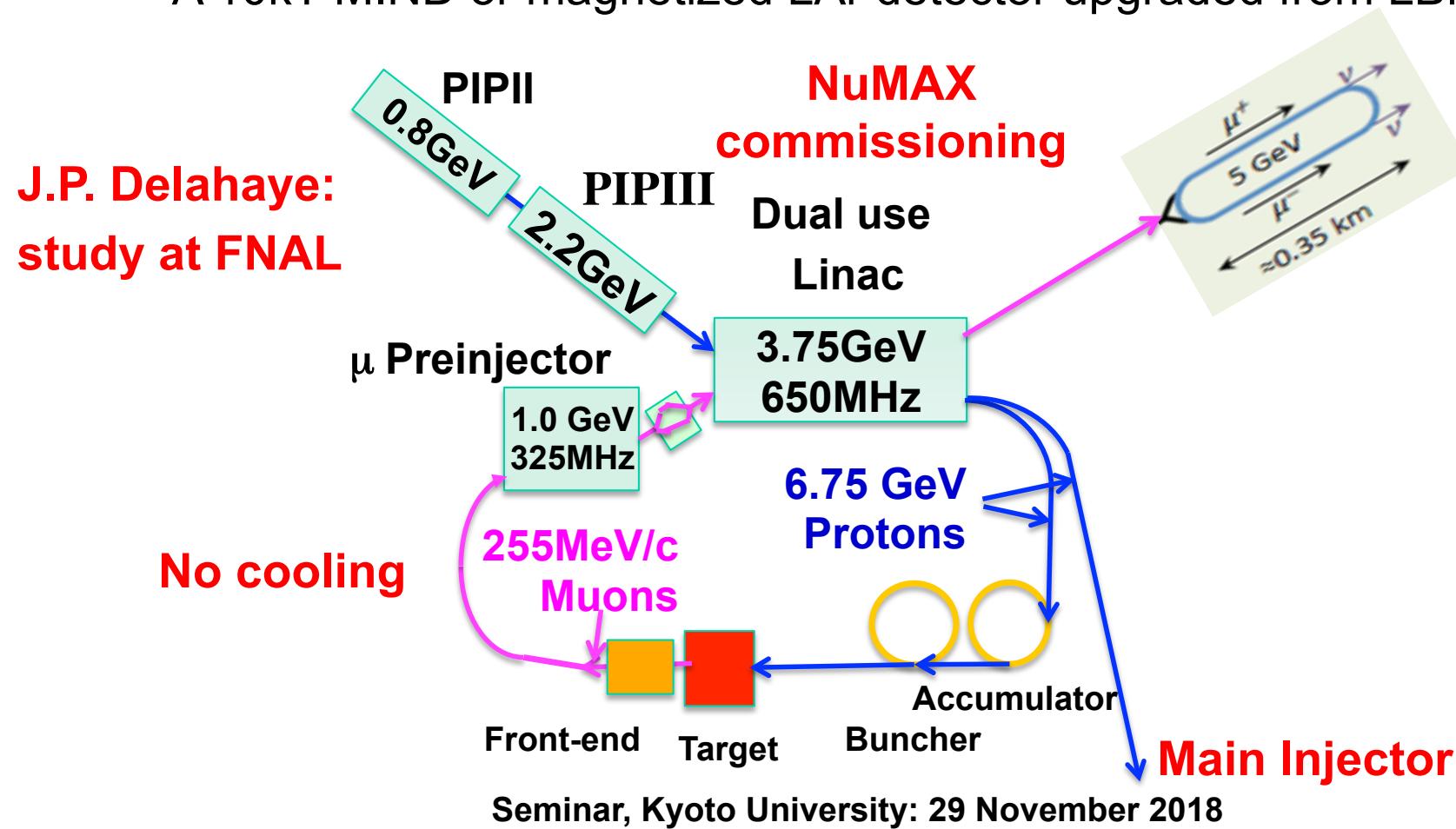
arXiv:1808.01858

**Staging study
at FNAL:
from 5 GeV
Neutrino Factory
to Muon Collider**



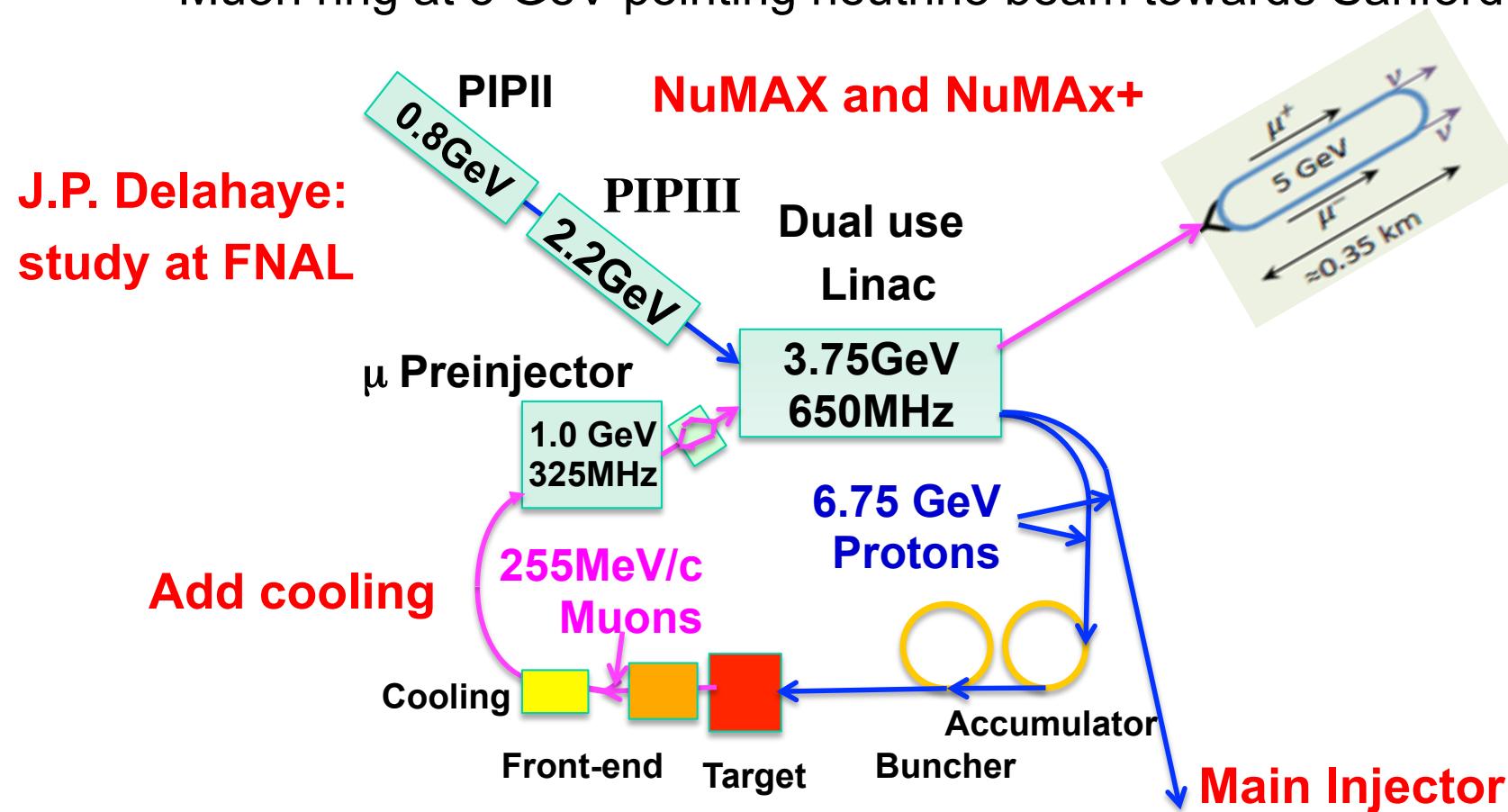
Stage 1: NuMAX commissioning

- Neutrinos from a Muon Accelerator CompleX (NuMAX)
 - Neutrino Factory with 10^{20} straight muons decays/year @ 5 GeV
 - Muon ring at 5 GeV pointing neutrino beam towards Sanford
 - A 10kT MIND or magnetized LAr detector upgraded from LBNE



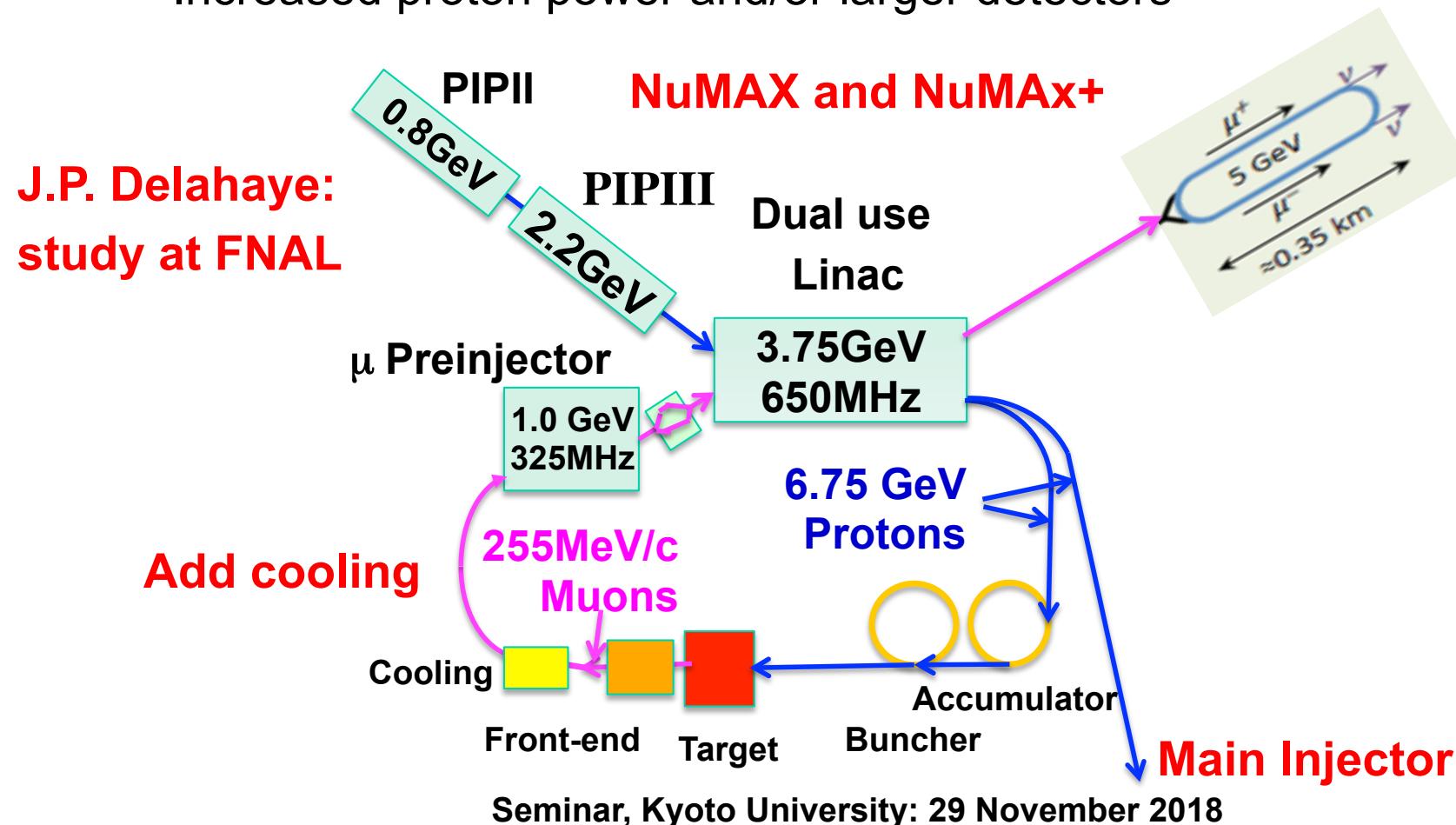
Stage 2: NuMAX

- Neutrinos from a Muon Accelerator CompleX (NuMAX)
 - Add small amount of 6D cooling
 - Neutrino Factory with 5×10^{20} straight muon decays/year @ 5 GeV
 - Muon ring at 5 GeV pointing neutrino beam towards Sanford



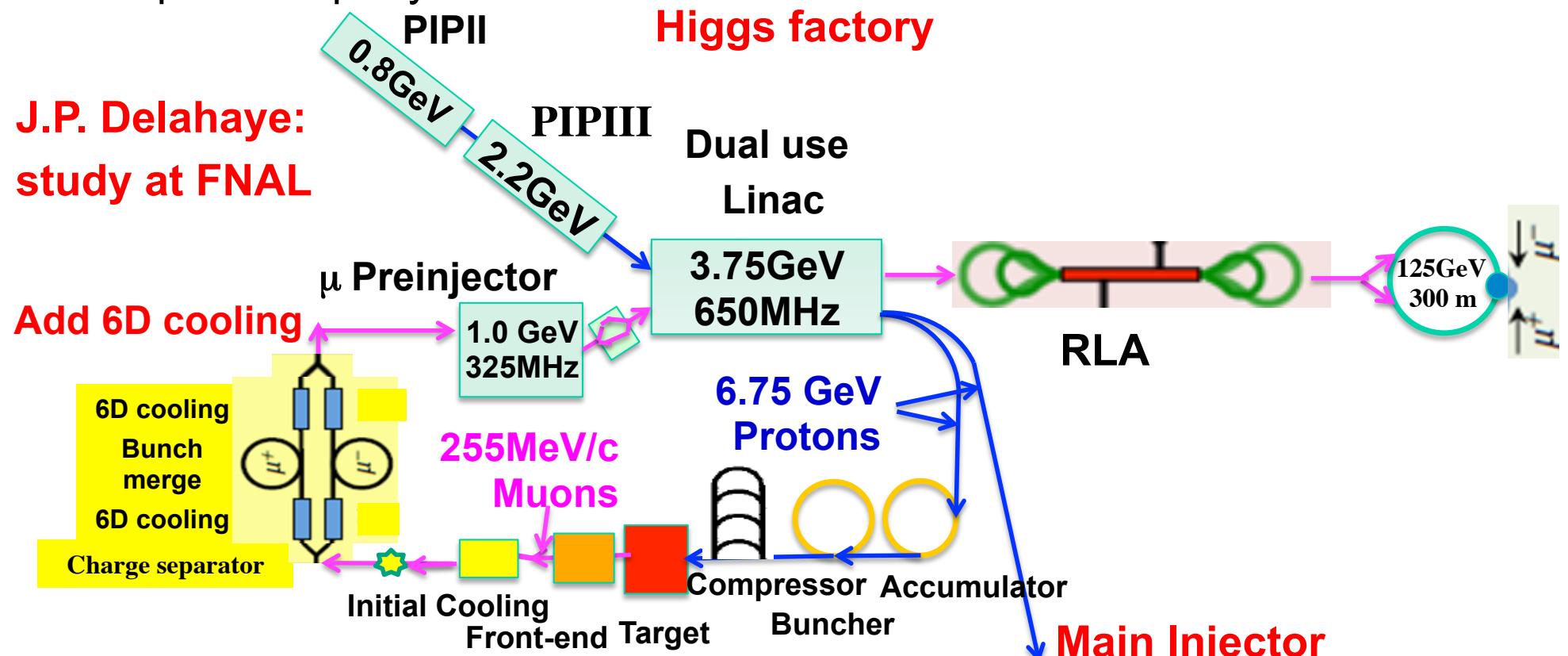
Stage 3: NuMAX+

- Neutrinos from a Muon Accelerator CompleX (NuMAX+)
 - Neutrino Factory with 10^{21} straight muons decays/year @ 5 GeV
 - Muon ring at 5 GeV pointing neutrino beam towards Sanford
 - Increased proton power and/or larger detectors



Stage 4: Higgs Factory

- ❑ Higgs Factory: production of Higgs at 126 GeV CM
 - Collider capable of providing ~13,500 Higgs events per year with exquisite energy resolution: direct Higgs mass and width
 - Possible upgrade to a Top Factory with production of up to 60000 top particles per year

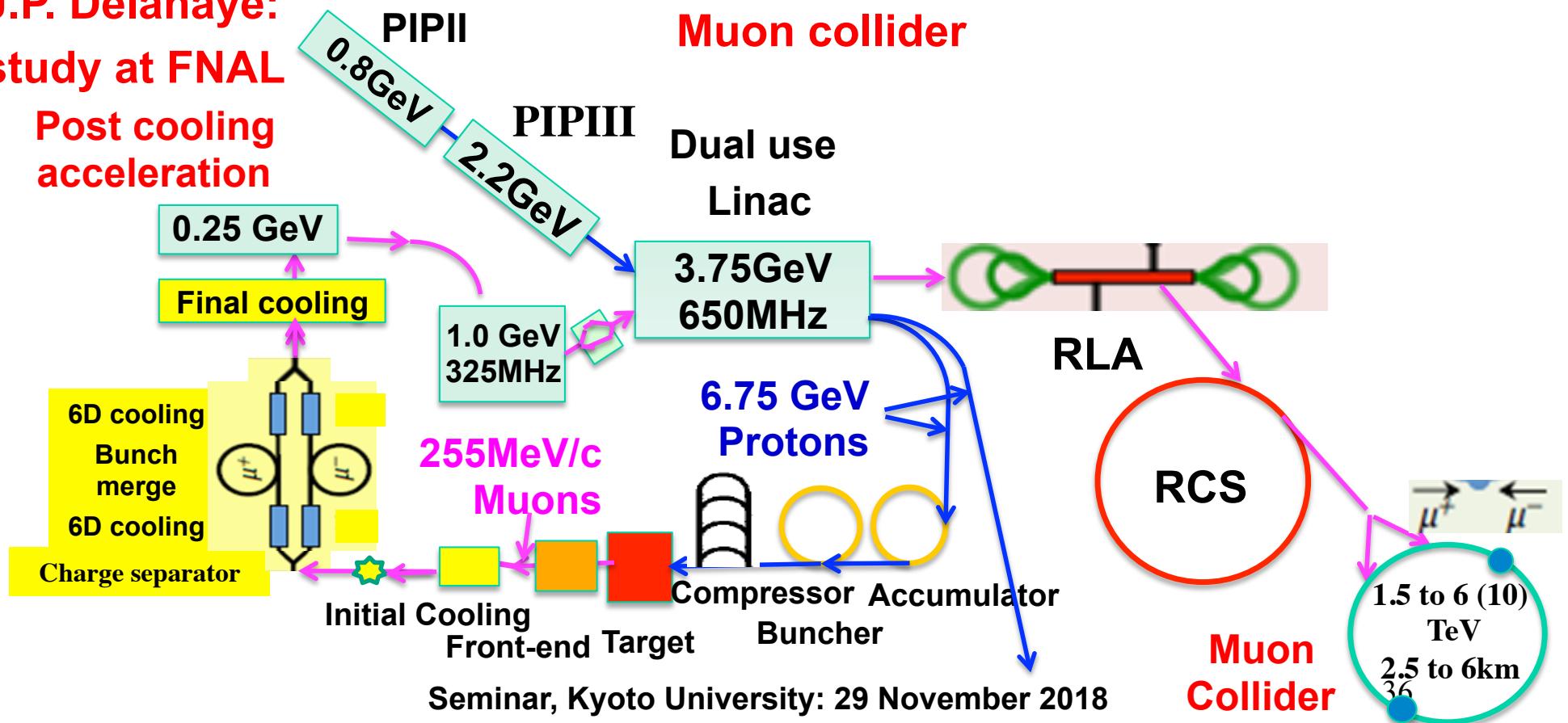


Stage 5: Muon Collider

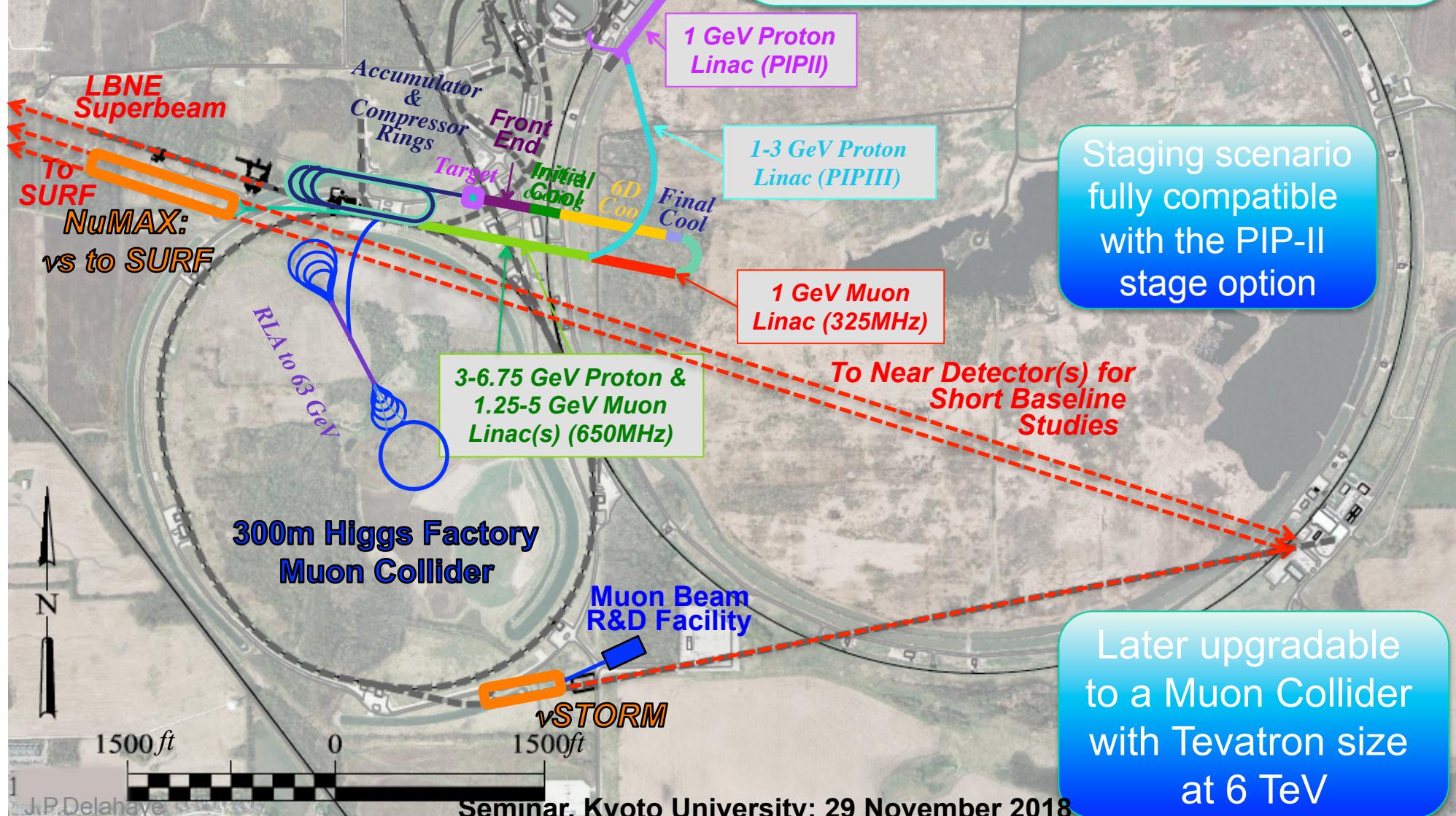
- Multi-TeV muon collider:
 - If warranted by LHC results a muon collider can reach up to 10 TeV
 - Likely offers the best performance, least cost and power consumption of any lepton collider operating in the multi-TeV regime.

**J.P. Delahaye:
study at FNAL**

**Post cooling
acceleration**



A Potential Muon Accelerator Complex at Fermilab: νSTORM → NuMAX → Higgs Factory



Staging summary

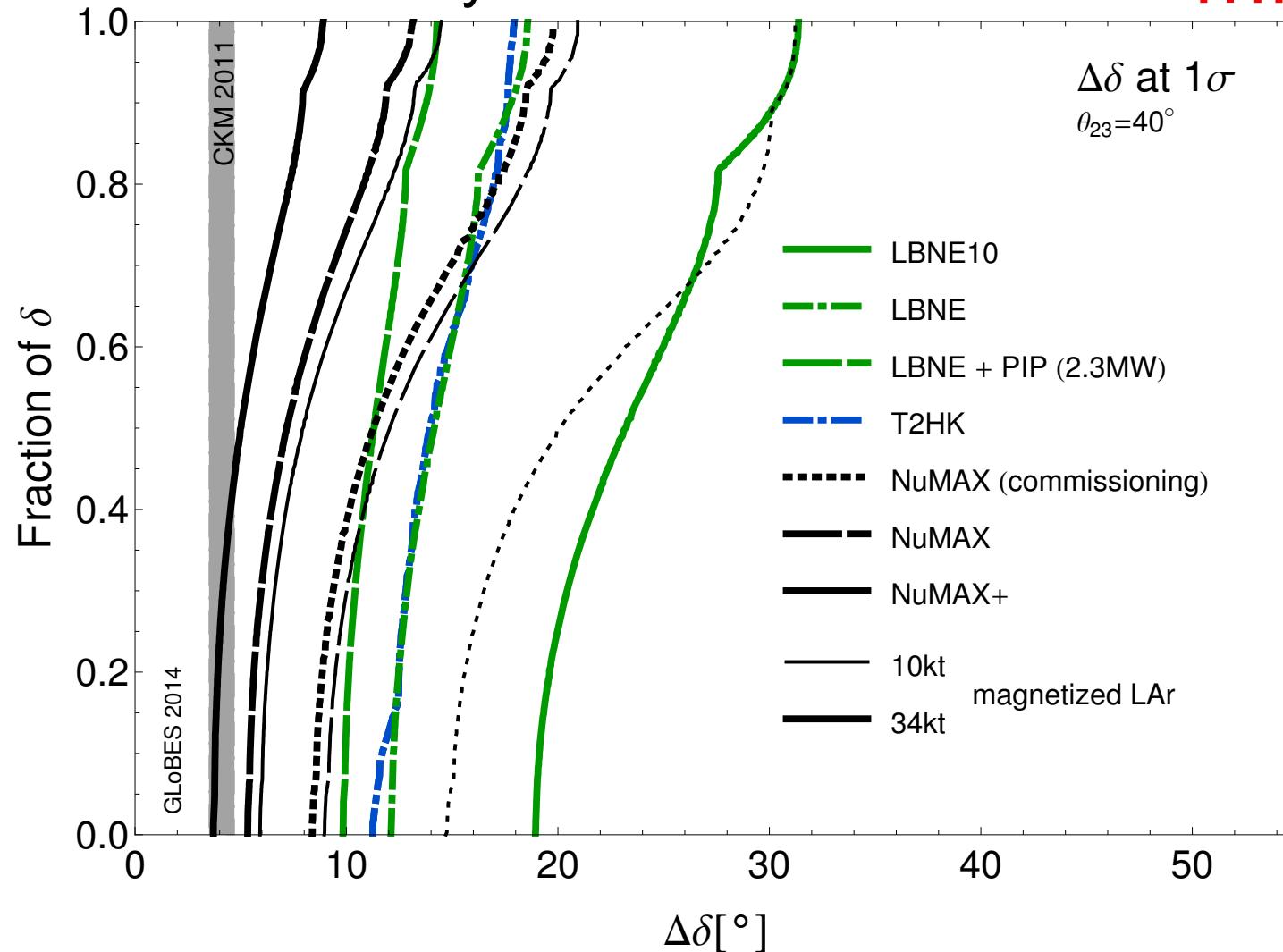
- Summary of machine parameters as a function of staging scenarios

	NuMAX Commissioning	NuMAX	NuMAX+	Higgs Fact 125 GeV	Muon Coll. 6 TeV ***
Beam energy (GeV/c)	5	5	5	62.5	3000
Cooling	No	Initial 6D	Initial 6D	6D no final	Full 6D
Proton beam power on target	1MW	1MW	2.75 MW	4 MW	1.8 MW
Proton beam energy on target	6.75 GeV	6.75 GeV	6.75 GeV	6.75 GeV	6.75 GeV
Acceleration cycle rep rate(Hz)	60	60	60	15	6
μ / cycle at front end	$1.36 \cdot 10^{12}$	$1.36 \cdot 10^{12}$	$3.75 \cdot 10^{12}$	$2.6 \cdot 10^{13}$	$2.9 \cdot 10^{13}$
Transmission efficiency (%)	15.3	56.7	56.7	15.4	6.9
μ / bunch in ring	$3.5 \cdot 10^9$	$1.3 \cdot 10^{10}$	$3.5 \cdot 10^{10}$	$4 \cdot 10^{12}$	$2.0 \cdot 10^{12}$
Bunches in ring	60	60	60	1	1
ν towards detector/year(10^7 s)	$4.9 \cdot 10^{19}$	$1.8 \cdot 10^{20}$	$5.0 \cdot 10^{20}$		
Higgs per year (10^7 sec)				13500	
Luminosity ($10^{34} \text{ cm}^{-2}\text{s}^{-1}$)					12

Physics performance of NuMAX

- Physics performance in terms of fraction of CP phase δ with measurement accuracy at or below $\Delta\delta$

P. Huber

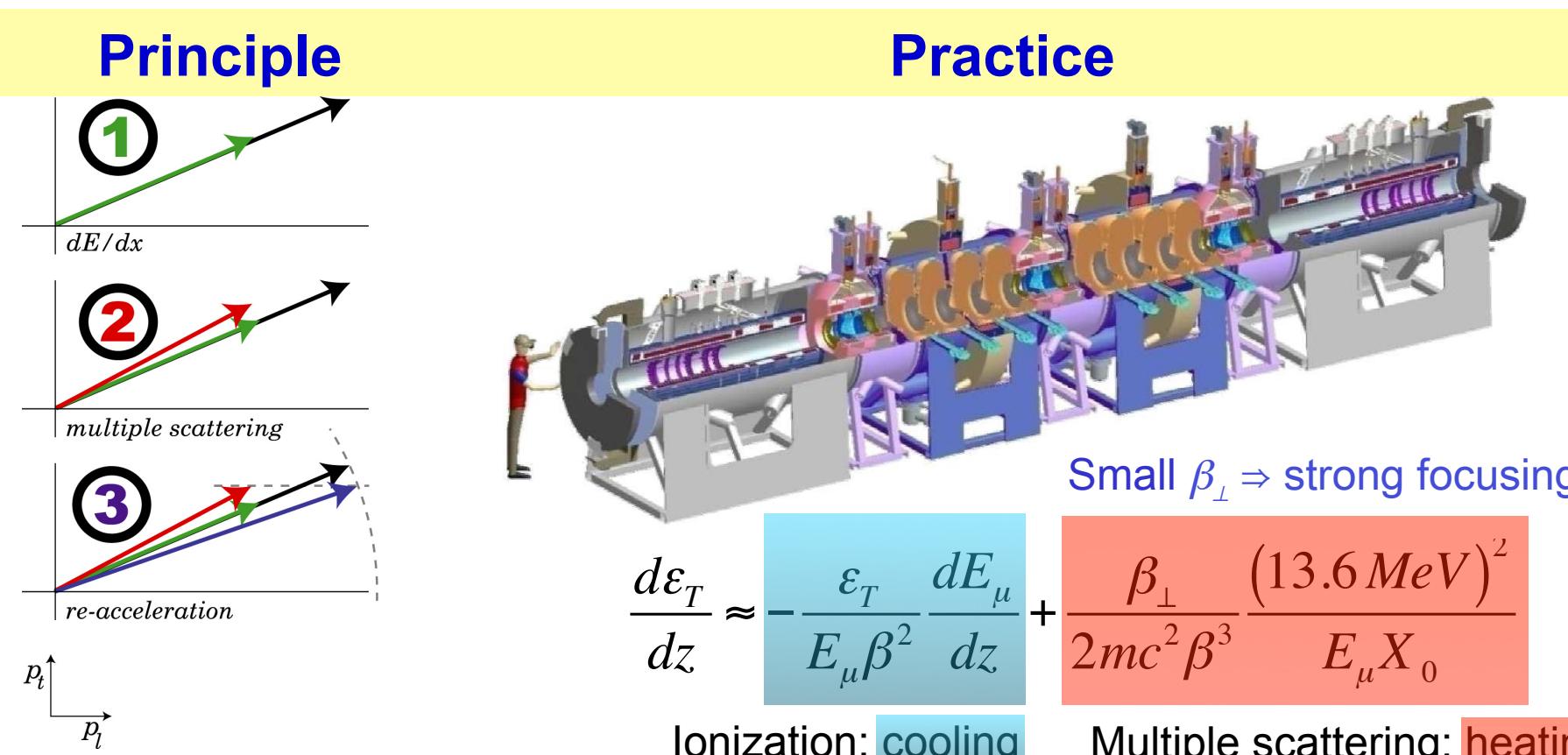


4. Muon Ionization Cooling Experiment (MICE)

Muon Cooling

❑ Muon Ionization Cooling:

- Muon Ionization Cooling is the key technology required to be able to build front-end of a Neutrino Factory and a Muon Collider (ie. stochastic cooling enabled proton-antiproton collider in 1980s)



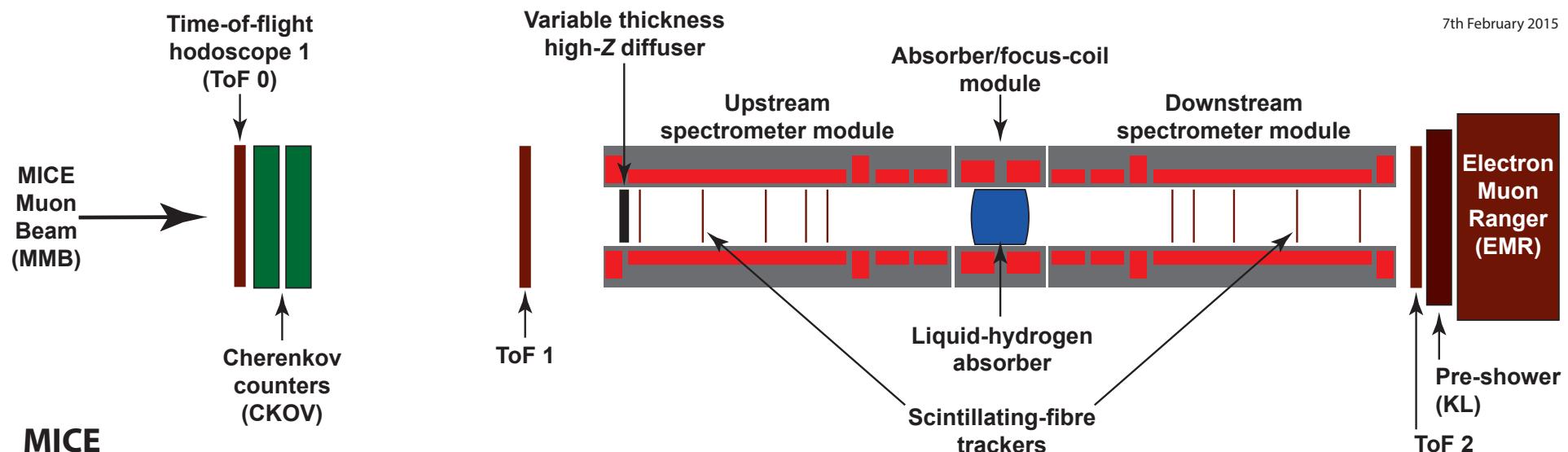
Ionization: **cooling**

Multiple scattering: **heating**

Muon Ionization Cooling Experiment

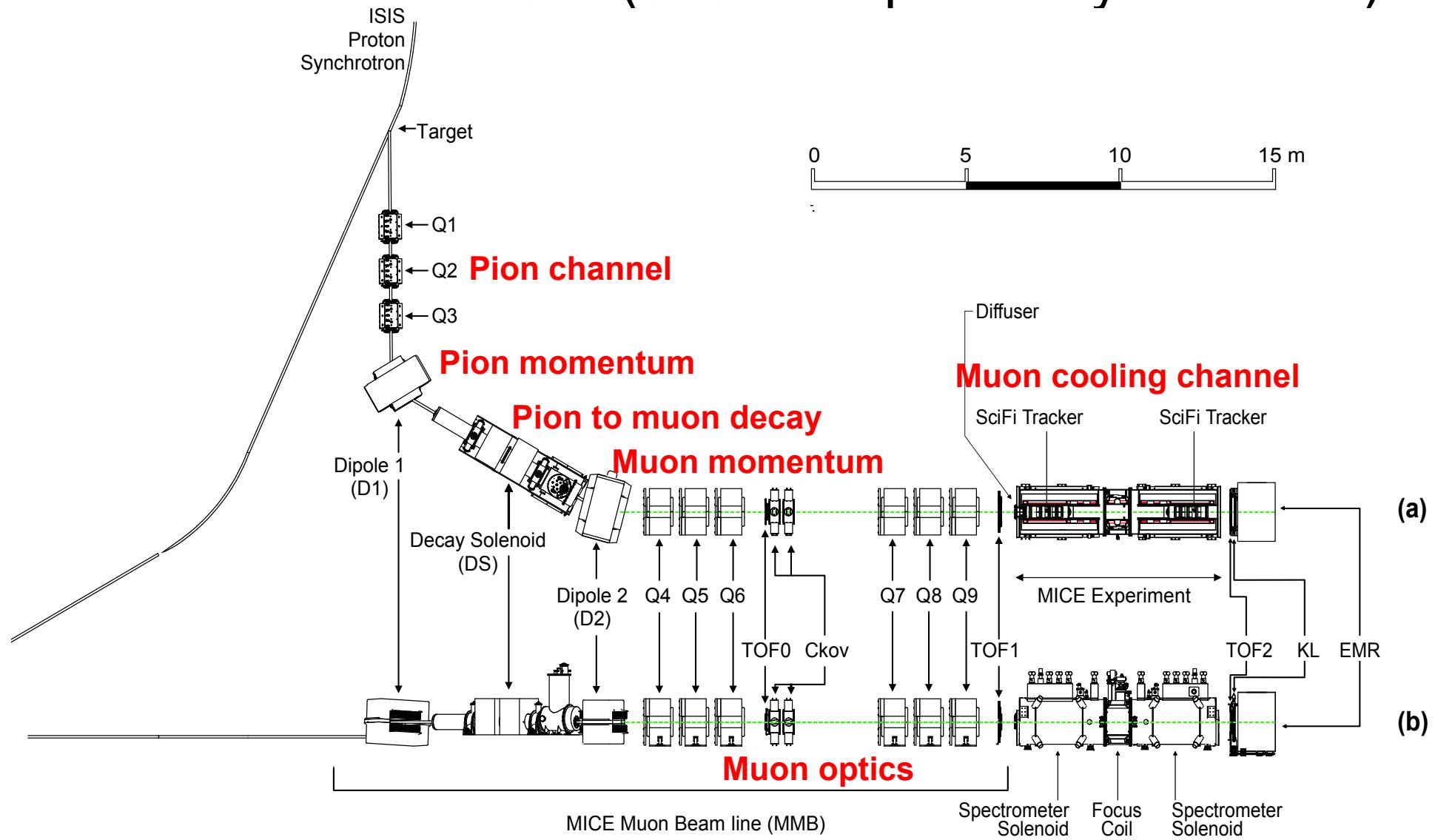
❑ Muon Ionization Cooling Experiment:

- Letter of Intent: **November 2001**
- Proposal at Rutherford Appleton Laboratory (RAL): **January 2003**
- International collaboration built muon ionization cooling experiment at RAL



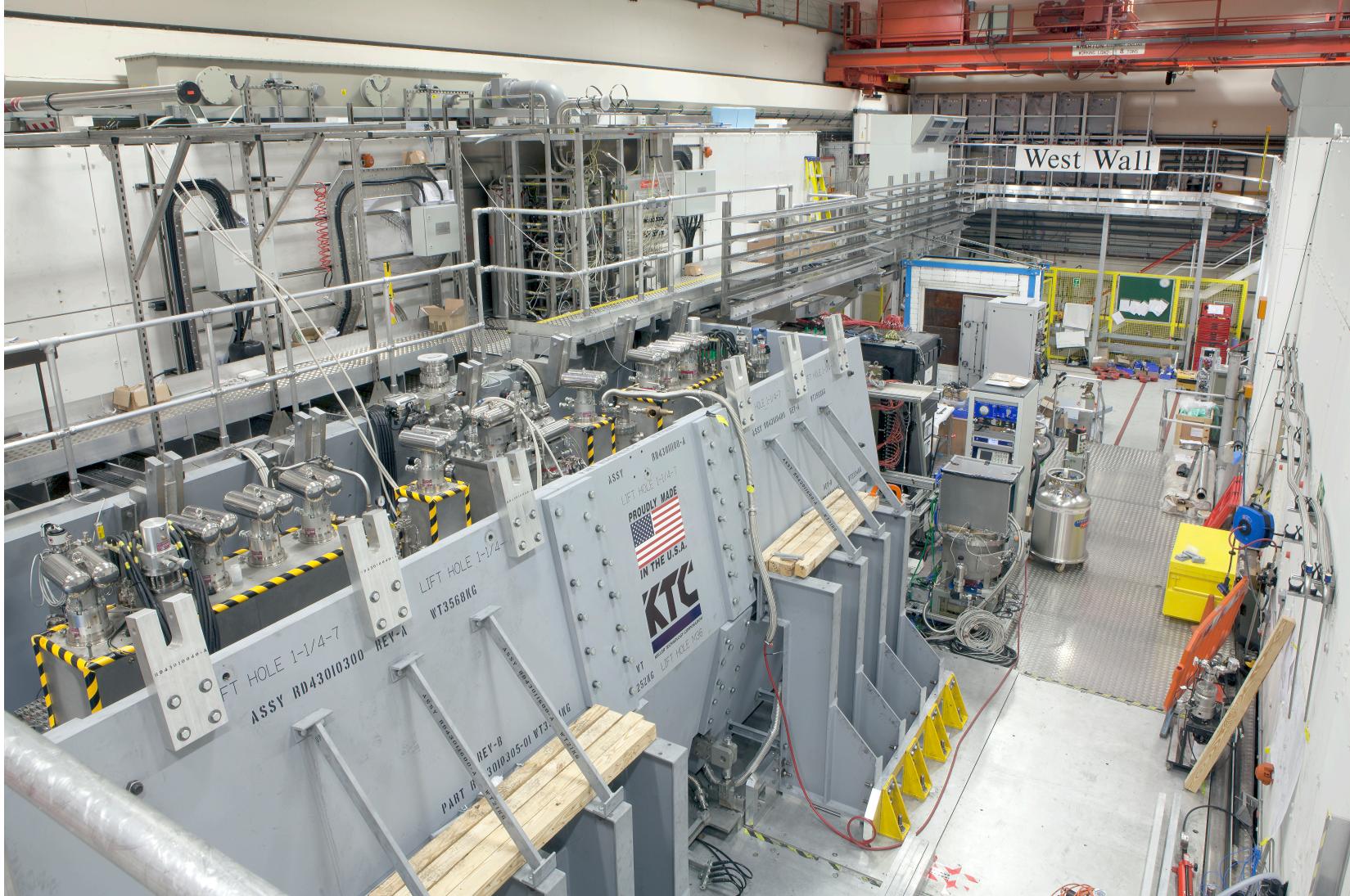
MICE Beam

- Muon beam from ISIS (800 MeV proton synchrotron)



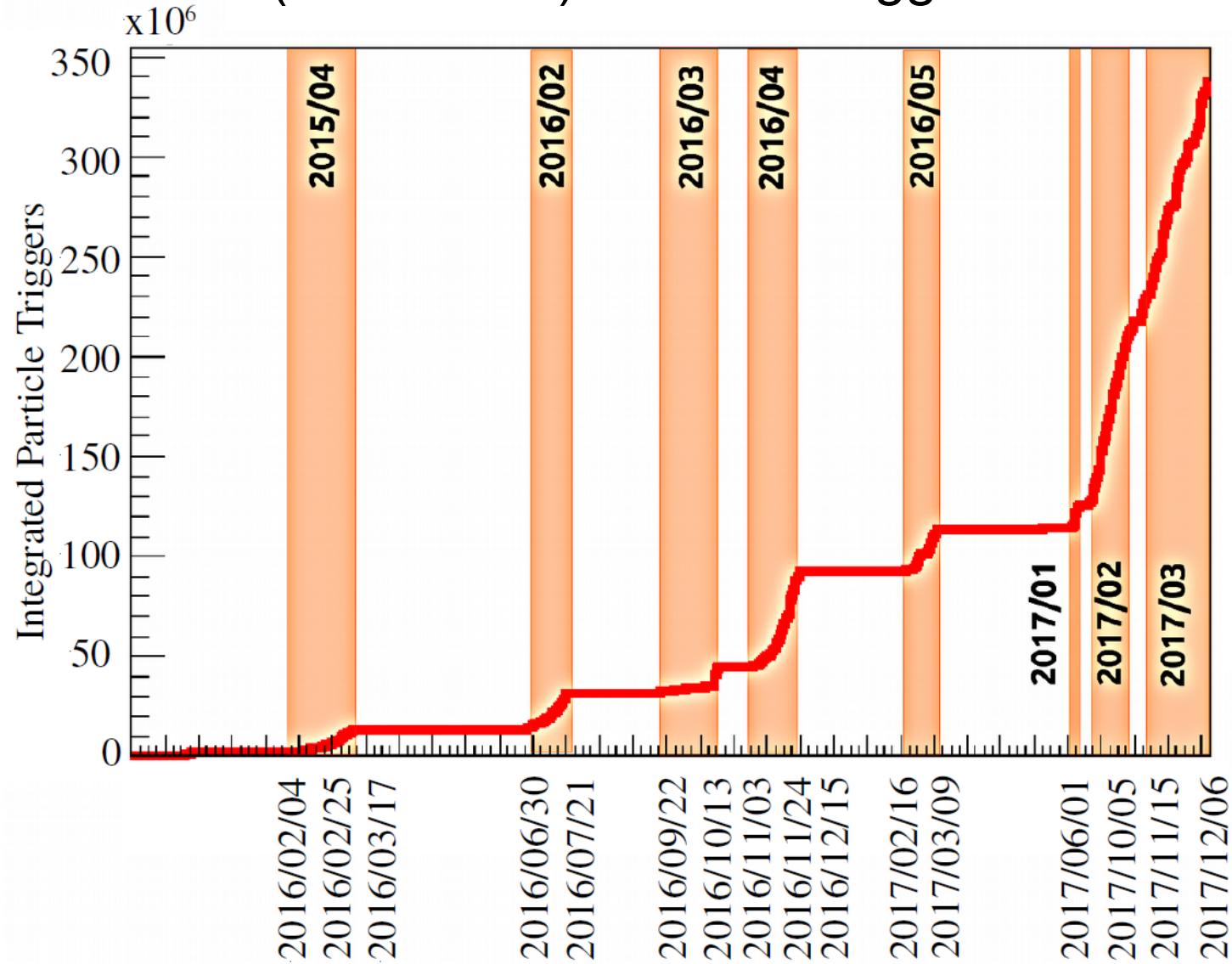
Muon Ionization Cooling Experiment

□ Cooling Channel with Partial Return Yoke



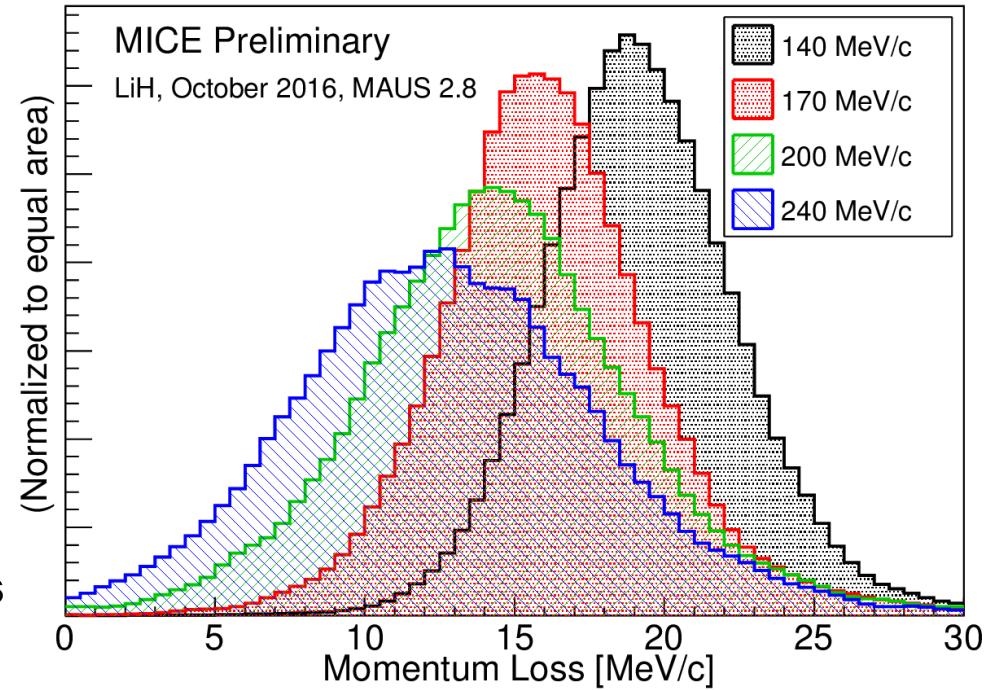
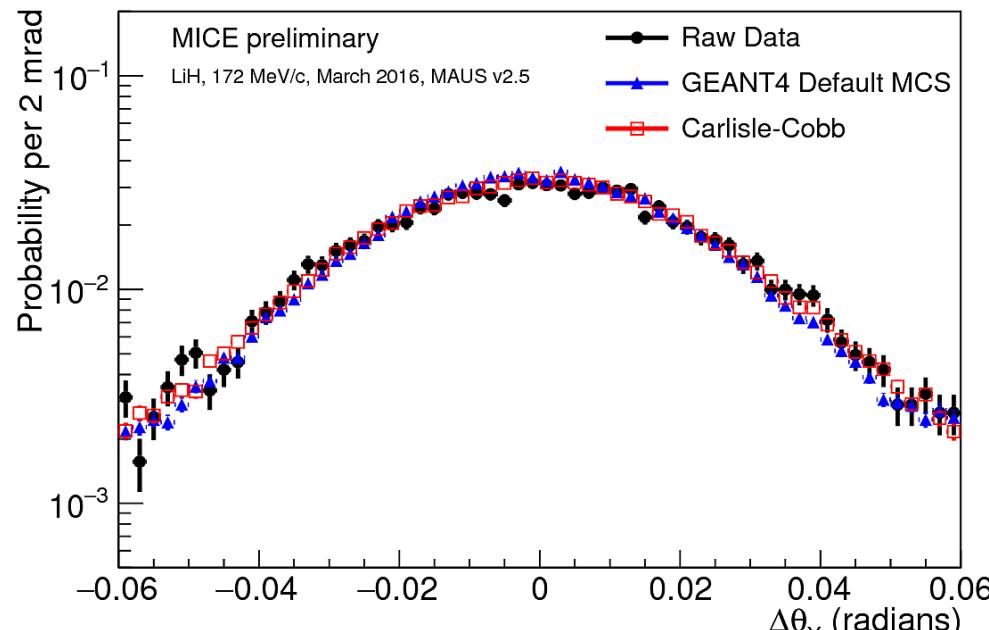
MICE Data

- ❑ MICE data set (2015-2017): 350×10^6 triggers



Multiple Coulomb Scattering

- ❑ First measurement of muon Multiple Coulomb Scattering in lithium hydride at 140-240 MeV/c **R. Bayes, J. Nugent**
 - Validation of Molière scattering model and Geant4
- ❑ Validation of energy loss model

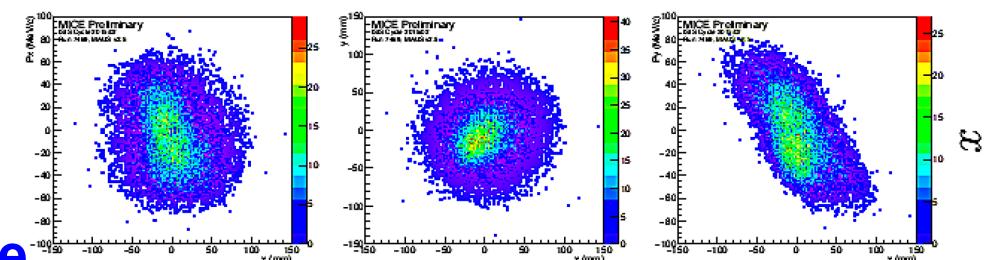


Measurement of beam emittance

- ❑ Single particle reconstruction: creates virtual beams by performing ensemble of all particles
- ❑ 4D-phase space of particles: (x, p_x, y, p_y)
- ❑ Normalised RMS transverse emittance: $\epsilon_T = \frac{\sqrt[4]{\Sigma_{4D}}}{mc}$ 4D covariance matrix: Σ_{4D}

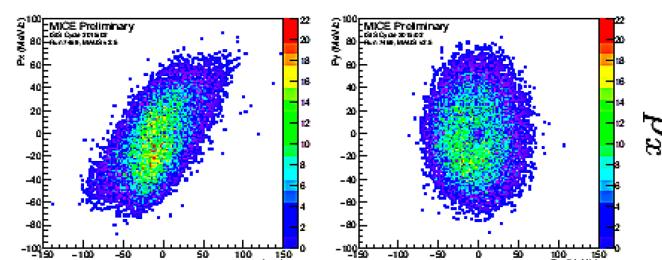
**Ellipsoid containing
4D phase-space
RMS volume**

$$\sigma_{xx}^2$$



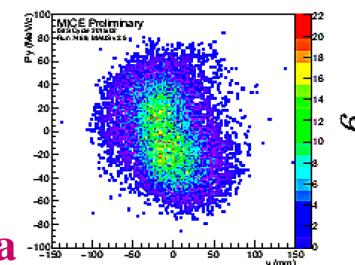
**Reconstructed phase space
shows coupling of different
variables for emittance
calculation**

$$\sigma_{p_x p_x}^2$$



- ❑ Ionization cooling implies reduction of transverse emittance after absorber

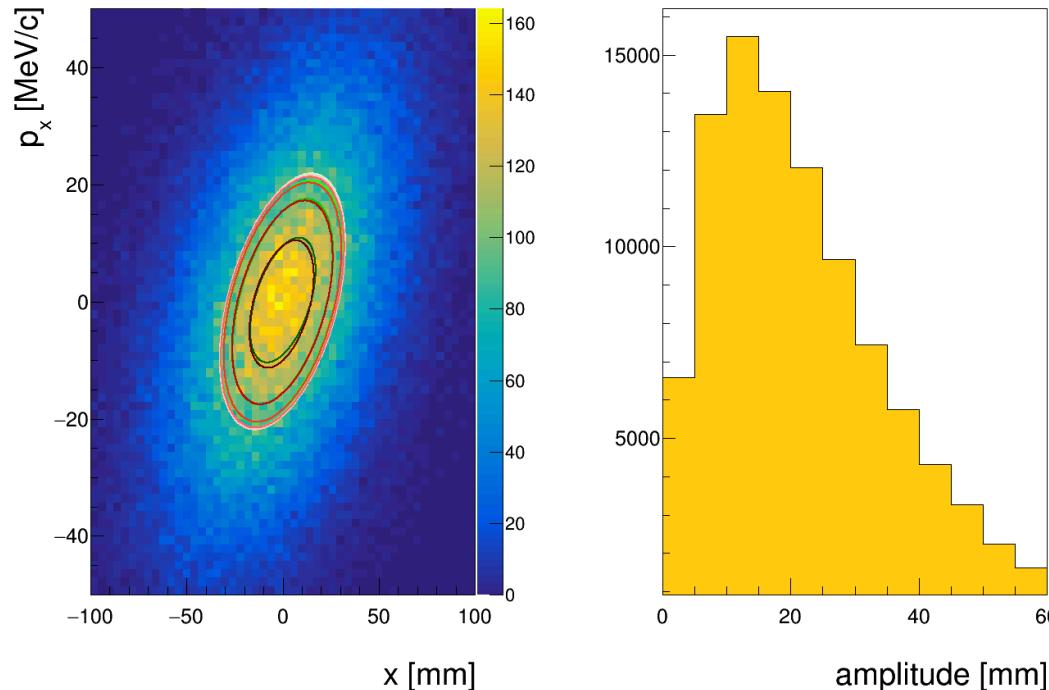
$$\sigma_{yy}^2$$



Transverse single-particle amplitude

- ❑ Transverse single-particle amplitude:
 - Phase-space distance of muon from beam core

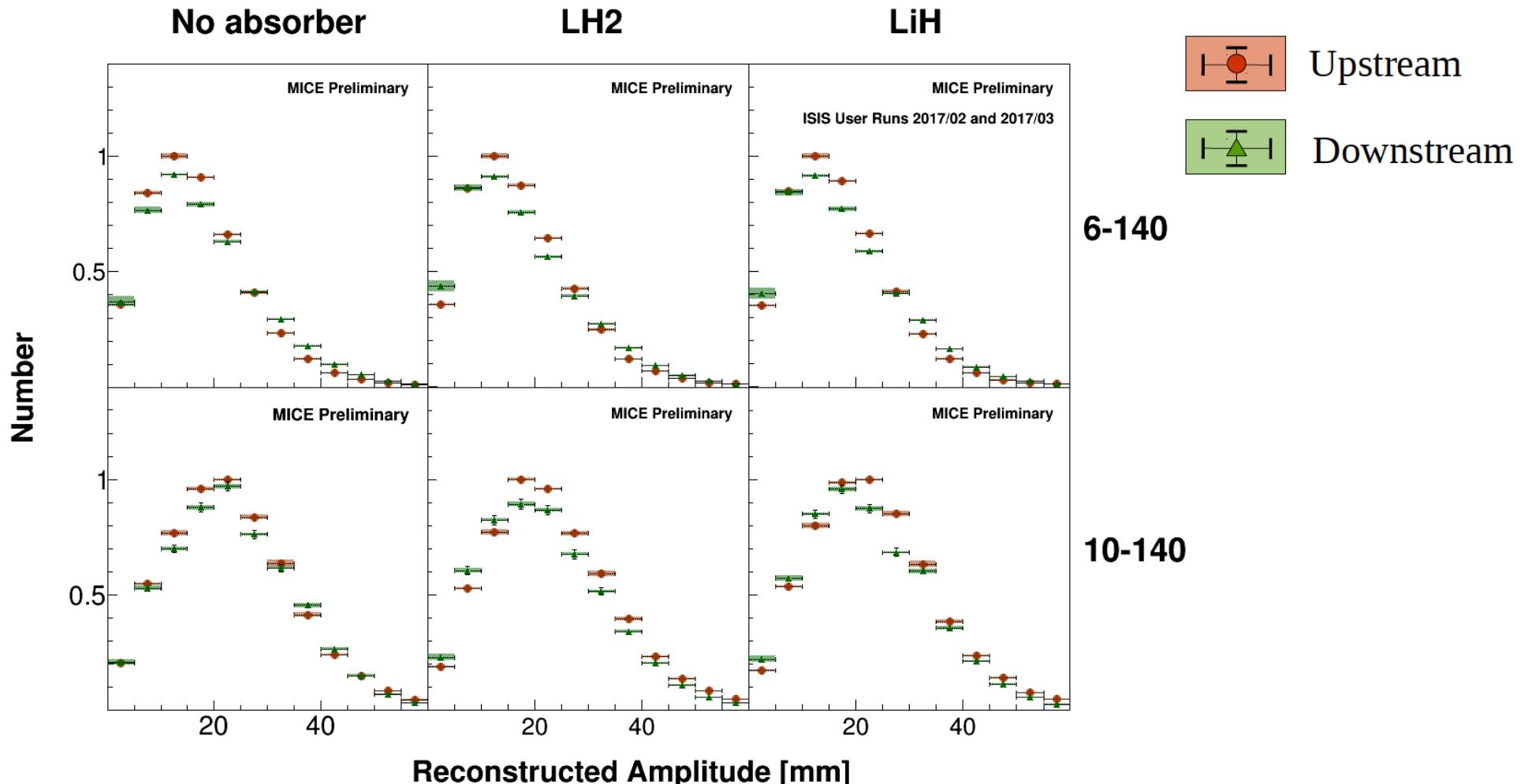
$$A_{\perp} = \varepsilon_T \mathbf{u}^T \Sigma^{-1} \mathbf{u} \quad \text{with} \quad \mathbf{v} = (x, p_x, y, p_y) \quad \text{and} \quad \mathbf{u} = \mathbf{v} - \langle \mathbf{v} \rangle$$



- ❑ Mean amplitude is proportional to RMS emittance
- ❑ Ionization cooling reduces amplitude in the core of the beam
(higher amplitude density at low amplitudes)

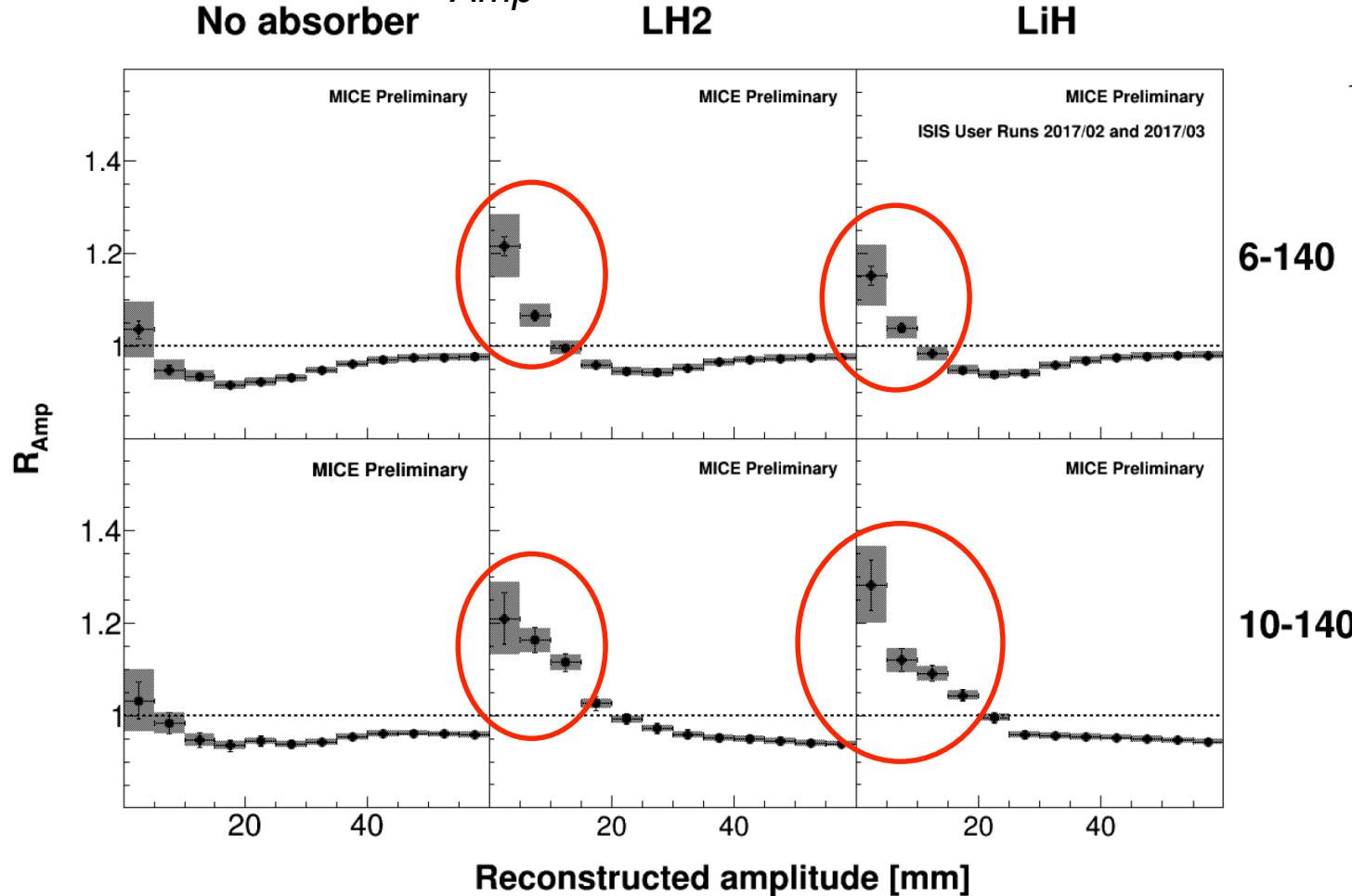
Change in amplitude across absorber

- ❑ No absorber: decrease in number of core muons
- ❑ Absorber: increase in number of core muons (cooling signal)



Ratio of cumulative core densities

- ❑ Cumulative core density increase for LH2 and LiH absorbers
- ❑ More cooling ($R_{Amp} > 1$) at higher input emittances



$$R_{Amp}^N \equiv \frac{\sum_{n=1}^N A_n^{down}}{\sum_{n=1}^N A_n^{up}}$$

First demonstration and characterisation of ionization cooling!

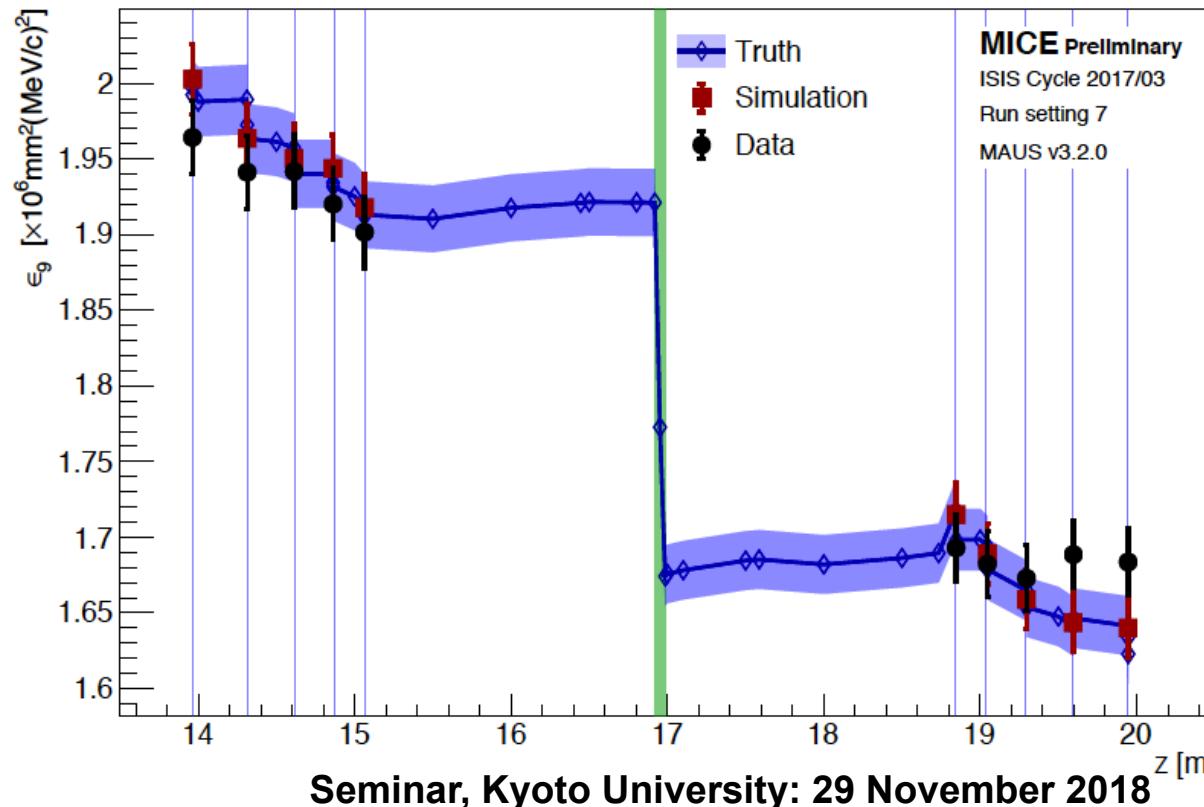
Seminar, Kyoto University: 29 November 2018

Fractional emittance evolution

- ❑ Fractional emittance is phase-space volume occupied by fraction α of beam ($\alpha=9\%$ is 1σ of 4D phase space)

$$\varepsilon_\alpha = \frac{1}{2} (\pi m c \varepsilon_T)^2 \Rightarrow \frac{\Delta \varepsilon_\alpha}{\varepsilon_\alpha} \approx \frac{2 \Delta \varepsilon_T}{\varepsilon_T}$$

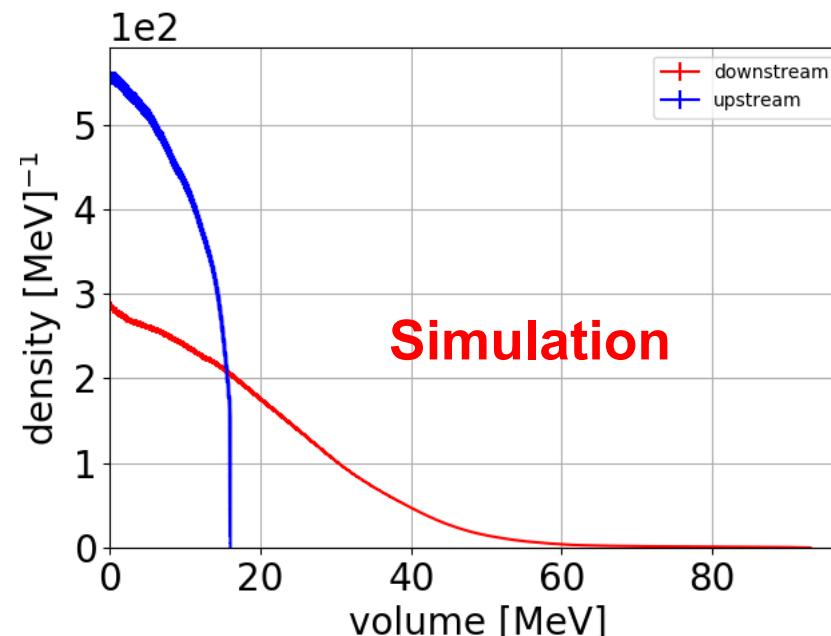
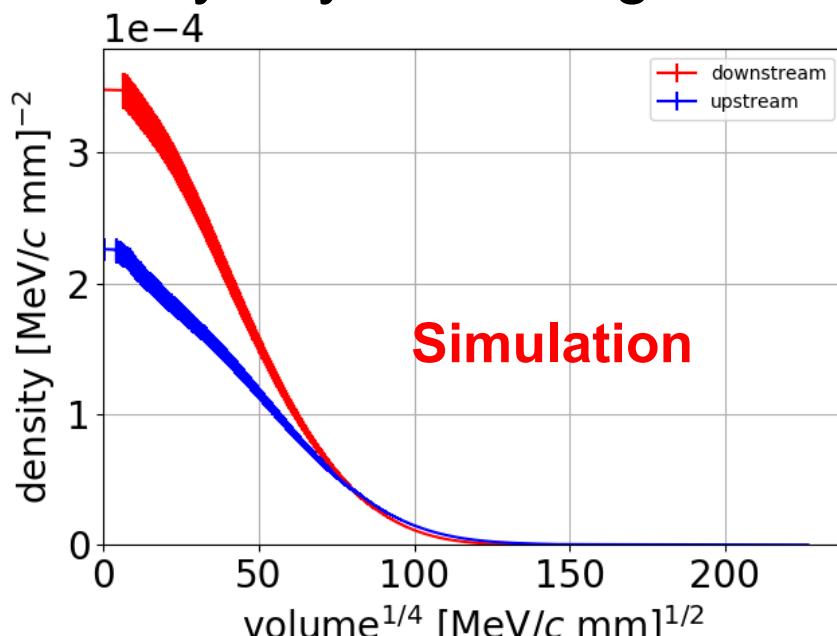
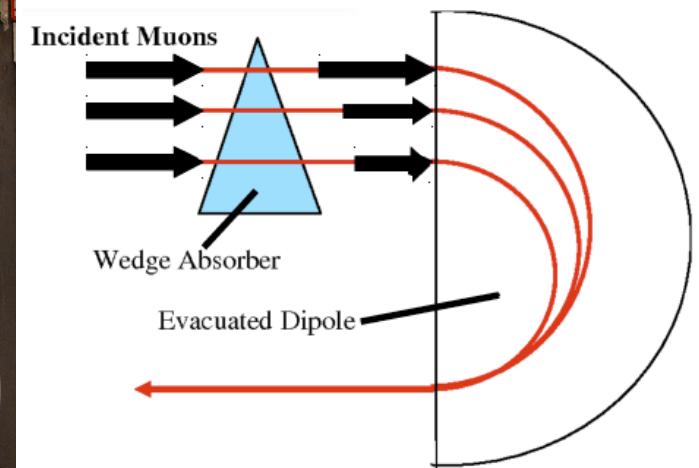
- ❑ Fractional (9%) emittance evolution 6 mm, 140 MeV/c, LiH, flip



Also shows
ionization
cooling!

Reverse emittance exchange

- ❑ Emittance exchange: muon collider 6D cooling and g-2
- ❑ Reverse emittance exchange lengthens bunch and increases luminosity in MC
- ❑ Polyethylene wedge absorber

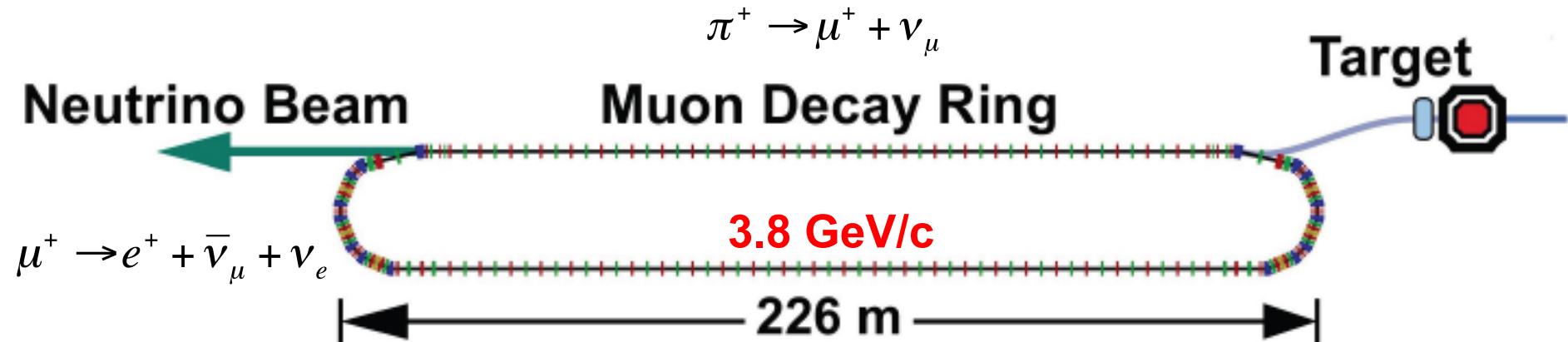


Reverse emittance exchange: transverse cooling and longitudinal heating

5. nuSTORM

nuSTORM: Neutrinos from STORed Muons

- nuSTORM: storage ring for 3.8 GeV/c muons

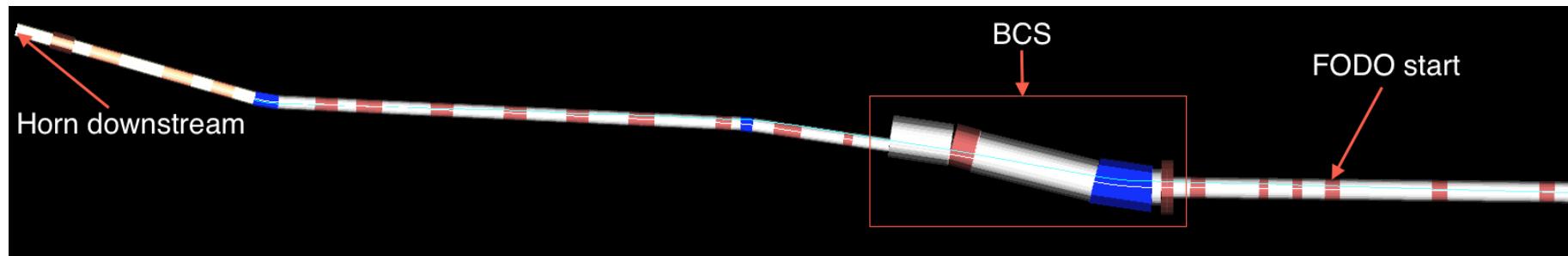


- Pions of 5 GeV/c captured and injected into ring.
- 52% of pions decay to muons before first turn: $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- For 10^{20} POT, flash of neutrinos from 8.6×10^{18} pion decays
- Muon momentum acceptance: $p = 3.8 \text{ GeV} \pm 10\%$
- Muon decays (1 lifetime=27 orbits): $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$
- For 10^{20} POT, expect $2.6 \times 10^{17} \mu^+$ decays
- Creates hybrid beam of neutrinos from pions & muons

nuSTORM Facility

- nuSTORM facility:

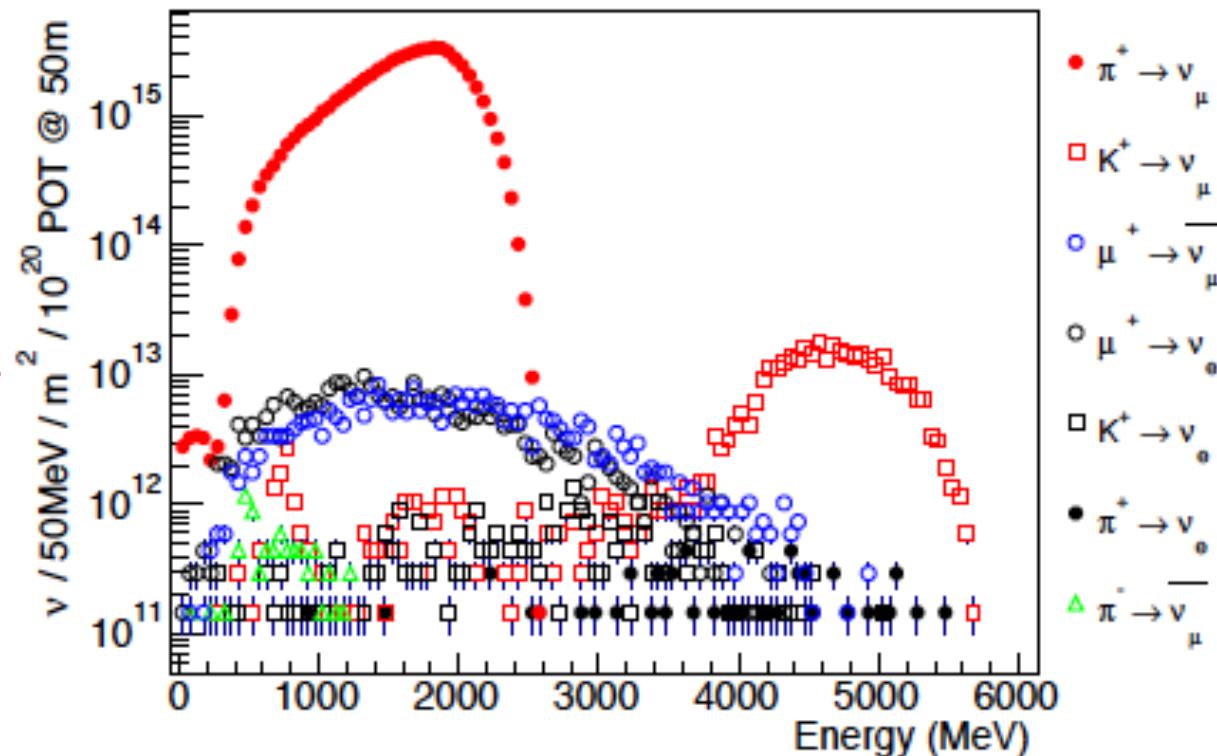
- 120 GeV protons on carbon or inconel target (100 kW)
- NuMI-style horn for pion collection
- Stochastic injection pions ($5 \text{ GeV}/c \pm 10\%$) into storage ring: $0.09 \pi/\text{POT}$
- Storage ring: large aperture FODO lattice ($3.8 \text{ GeV}/c \pm 10\%$) muons: $8 \times 10^{-3} \mu/\text{POT}$



nuSTORM Flux

□ nuSTORM flux and energy spectrum

Use muon decay neutrinos to calibrate hadron decay neutrinos?



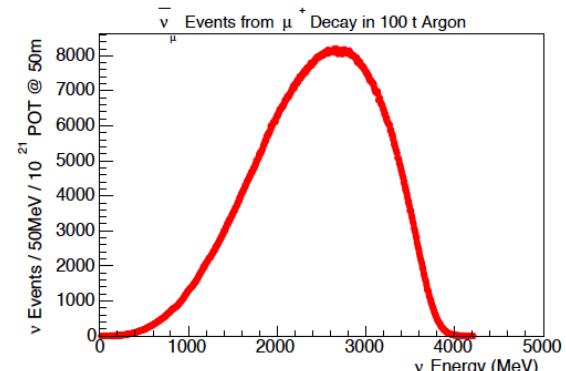
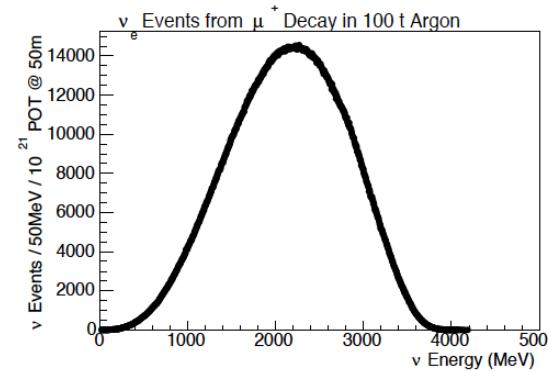
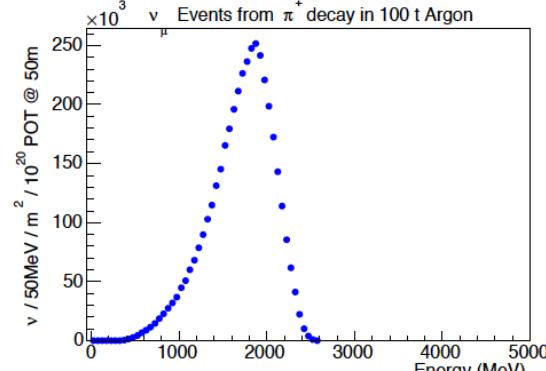
- ν_μ from pion decay $\pi^+ \rightarrow \mu^+ + \nu_\mu$ flux: $6.3 \times 10^{16} \text{ v/m}^2$ at 50 m
- ν_e from muon decay $\mu^+ \rightarrow e^+ + \bar{\nu}_\mu + \nu_e$ flux: $3.0 \times 10^{14} \text{ v/m}^2$ at 50 m
- ν_μ from kaon decay $K^+ \rightarrow \mu^+ + \nu_\mu$ flux: $3.8 \times 10^{14} \text{ v/m}^2$ at 50 m
- Can be used for cross-section measurements and short baseline experiments

nuSTORM event rates

- ❑ Flux uncertainties for nuSTORM: < 1%
- ❑ Event rates per 10^{21} POT in 100 tons of Liquid Argon at 50 m

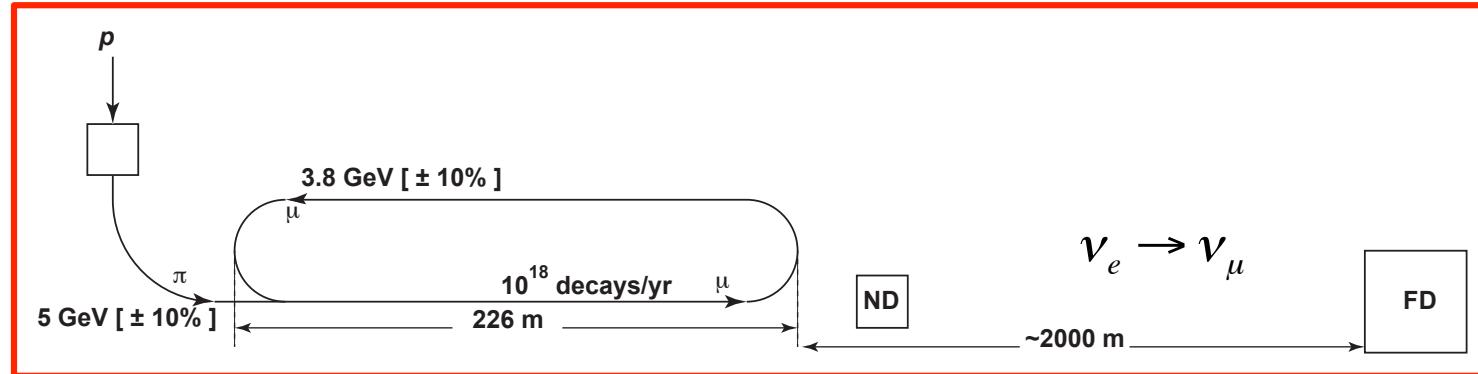
μ^+		μ^-	
Channel	N_{evts}	Channel	N_{evts}
$\bar{\nu}_\mu$ NC	1,174,710	$\bar{\nu}_e$ NC	1,002,240
ν_e NC	1,817,810	ν_μ NC	2,074,930
$\bar{\nu}_\mu$ CC	3,030,510	$\bar{\nu}_e$ CC	2,519,840
ν_e CC	5,188,050	ν_μ CC	6,060,580
π^+		π^-	
ν_μ NC	14,384,192	$\bar{\nu}_\mu$ NC	6,986,343
ν_μ CC	41,053,300	$\bar{\nu}_\mu$ CC	19,939,704

- Limited by detector systematics:



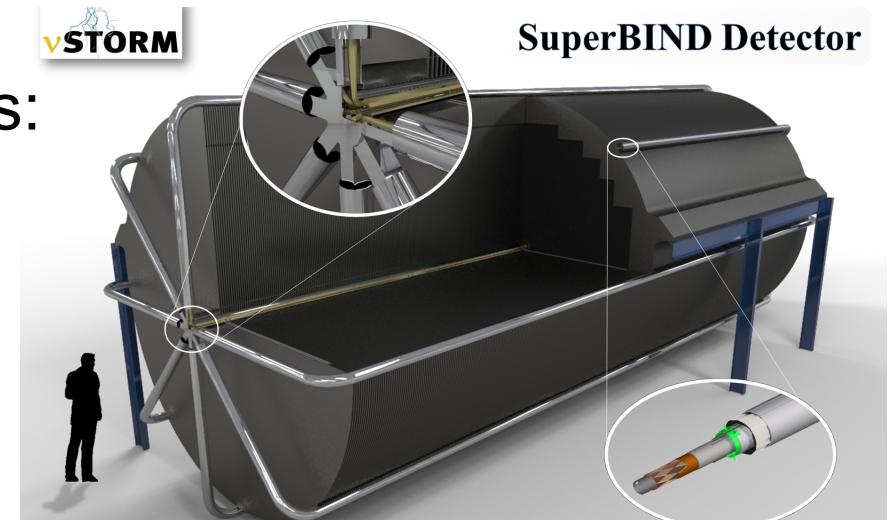
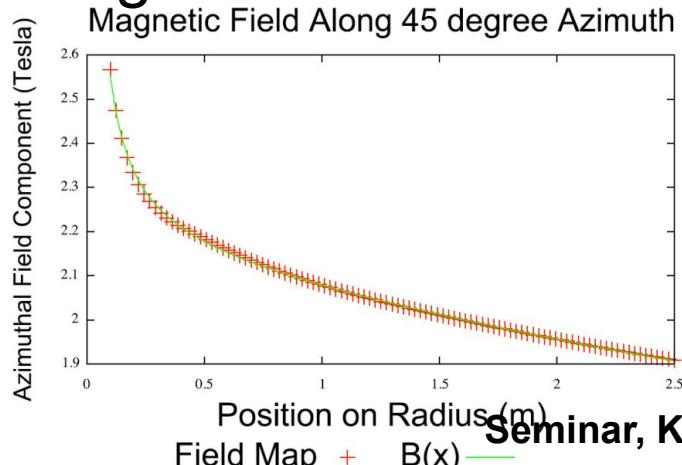
Sterile neutrino search

- ❑ Requires two magnetised detectors for neutrino oscillations:



- ❑ Super-saturated Magnetised Iron to remove wrong-sign muons:
SuperBIND

- ❑ Magnetic field: 1.5-2.6 T

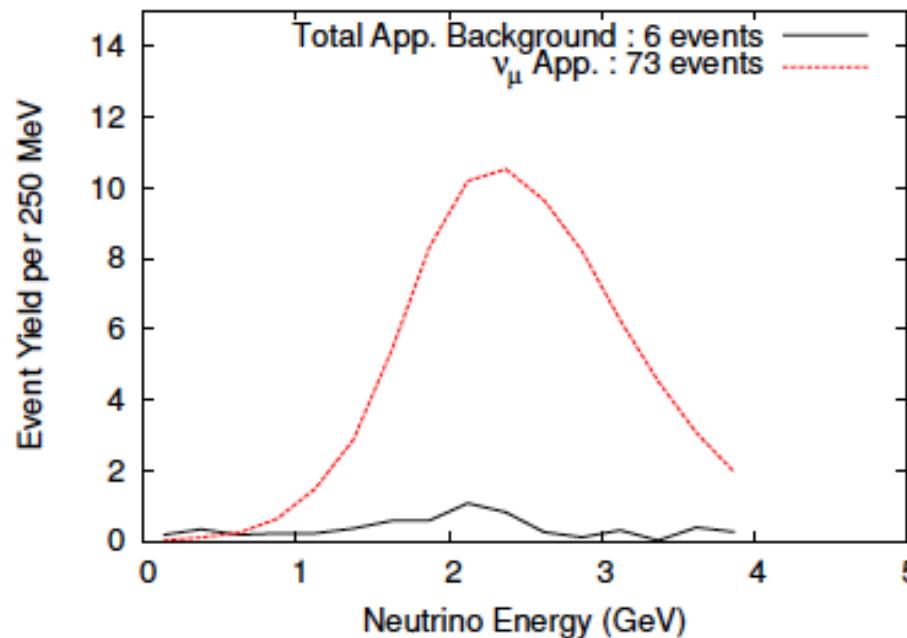


**240 kA from 8 Superconducting
Transmission Lines**

Sterile neutrino search

- ❑ Appearance search: **Adey et al., PRD 89 (2014) 071301**

$$P_{e\mu}(x) = 4|U_{e4}|^2 |U_{\mu 4}|^2 \sin^2\left(\frac{\Delta m_{14}^2 x}{4E}\right) \equiv \sin^2(2\theta_{e\mu}) \sin^2\left(\frac{\Delta m_{14}^2 x}{4E}\right)$$



**With full reconstruction
and efficiencies, 10²¹ POT**

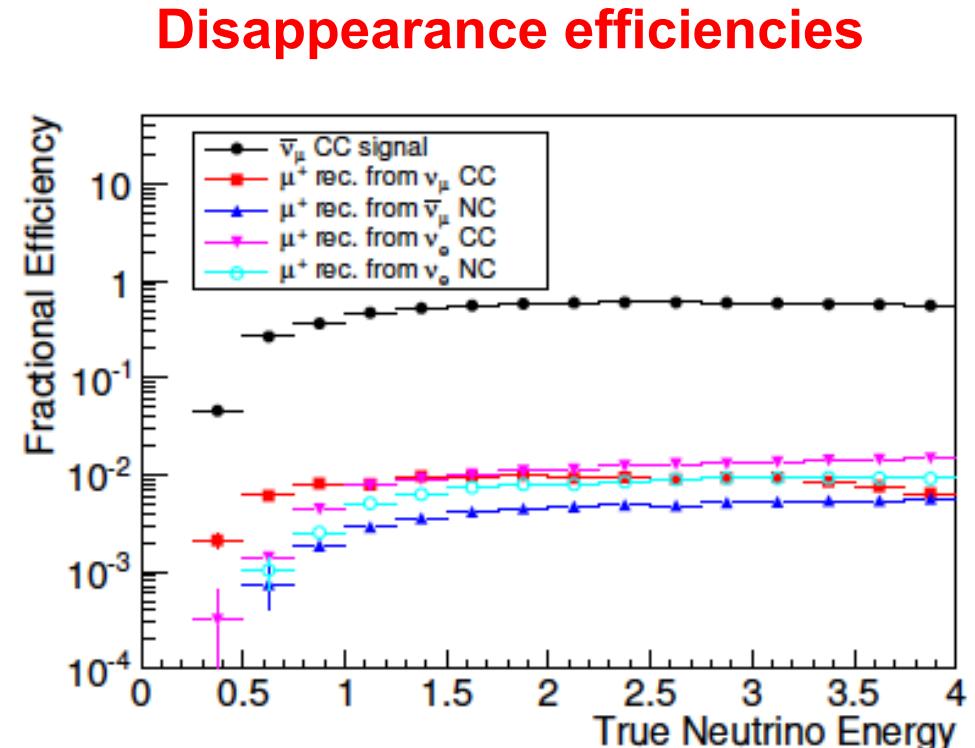
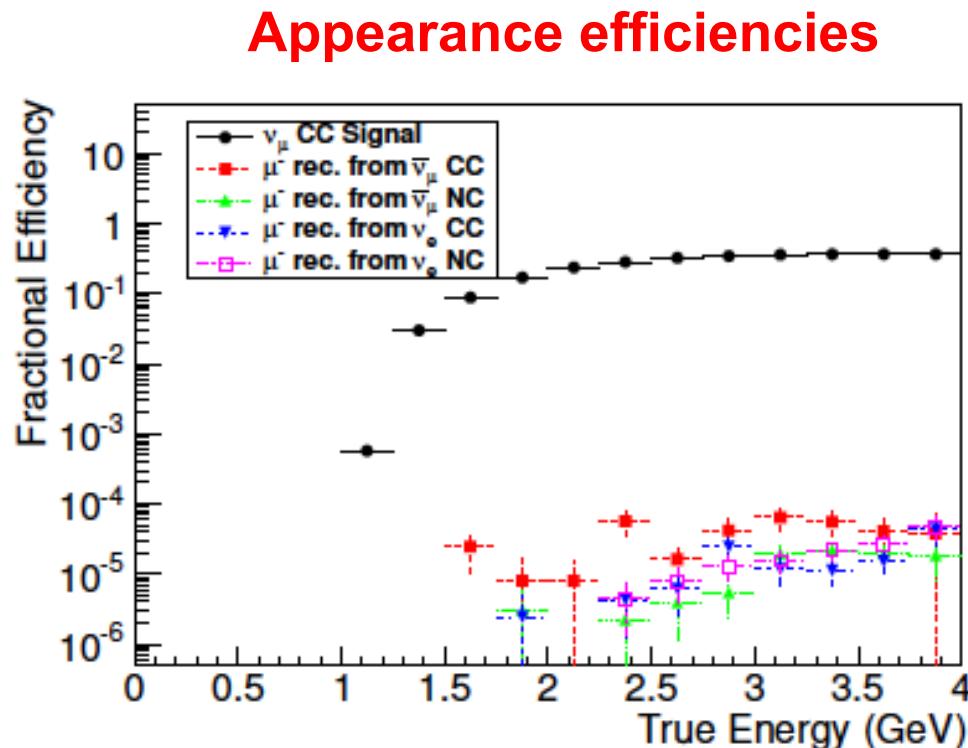
- ❑ Disappearance search:

$$P_{\mu\mu}(x) = 4|U_{\mu 4}|^2 \left(1 - |U_{\mu 4}|^2\right) \sin^2\left(\frac{\Delta m_{14}^2 x}{4E}\right) \equiv \sin^2(2\theta_{\mu\mu}) \sin^2\left(\frac{\Delta m_{14}^2 x}{4E}\right)$$

Sterile neutrino search

- ❑ Short-baseline oscillation search with near detector at 50 m and far detector at 2 km, 10^{21} POT exposure
- ❑ Appearance and disappearance multi-variate analyses

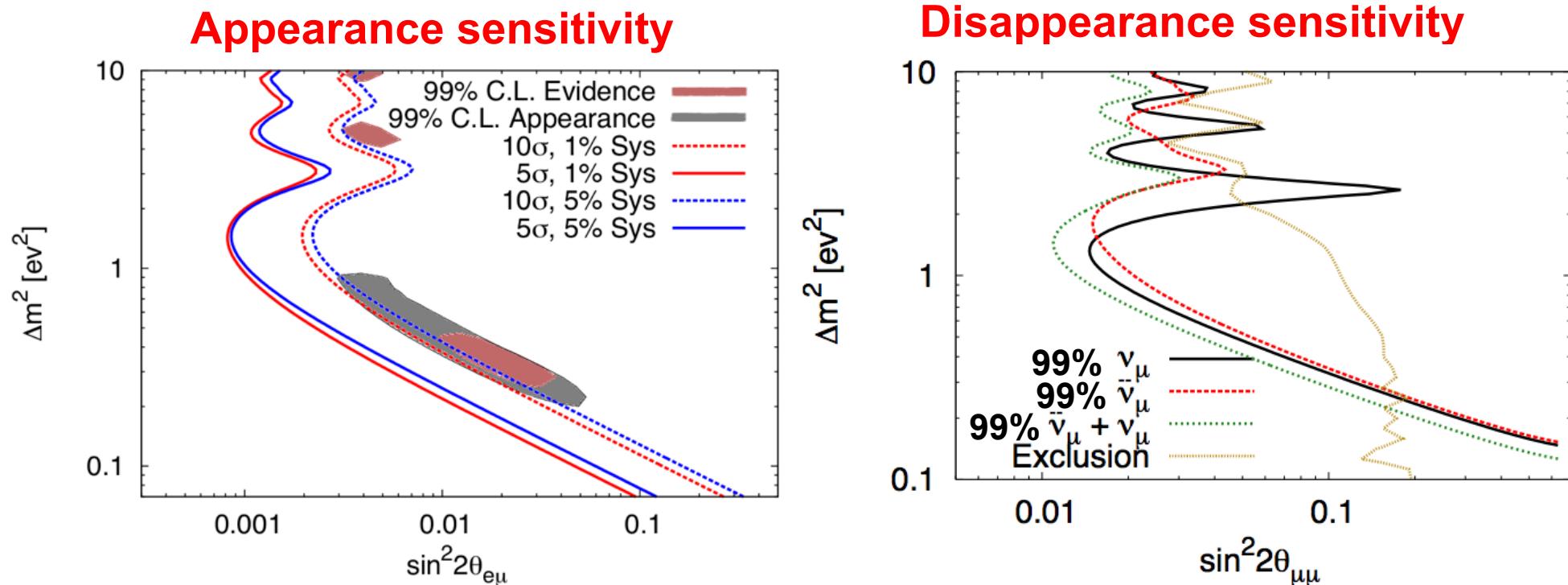
Adey et al., PRD 89 (2014) 071301 (Ryan Bayes' analysis)



Sterile neutrino search

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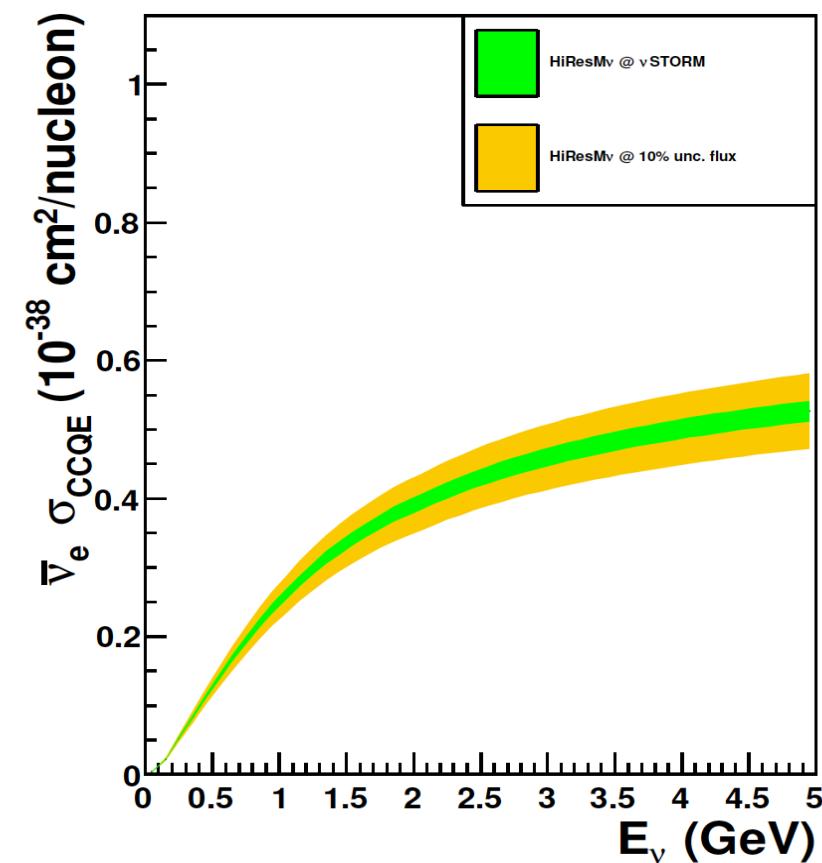
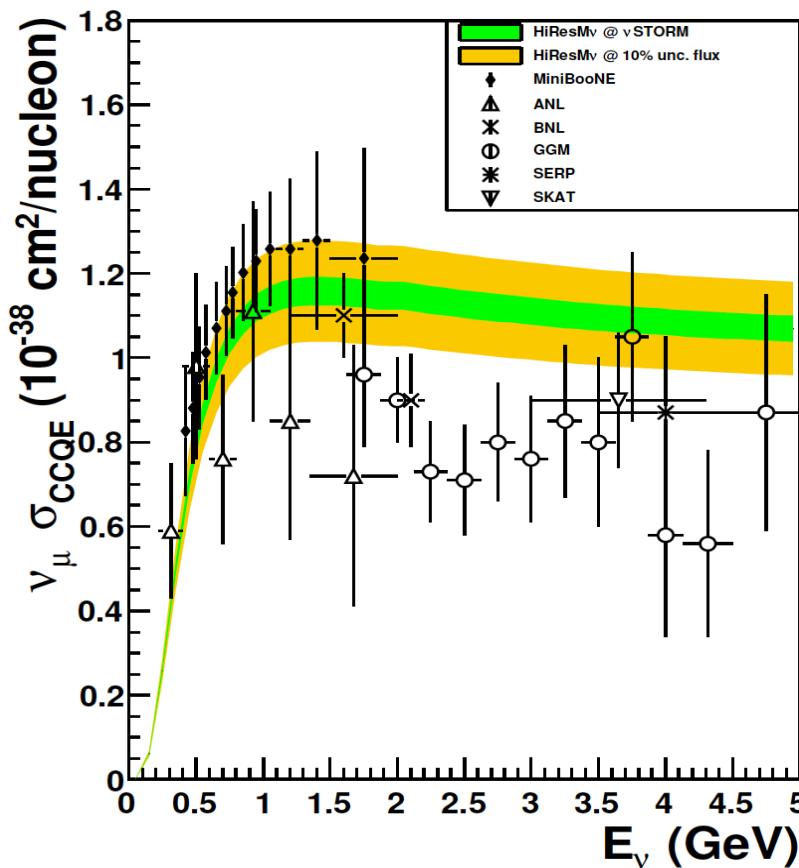
Adey et al., PRD 89 (2014) 071301 (Ryan Bayes' analysis)



After FNAL SBL programme, sterile neutrinos might not be relevant

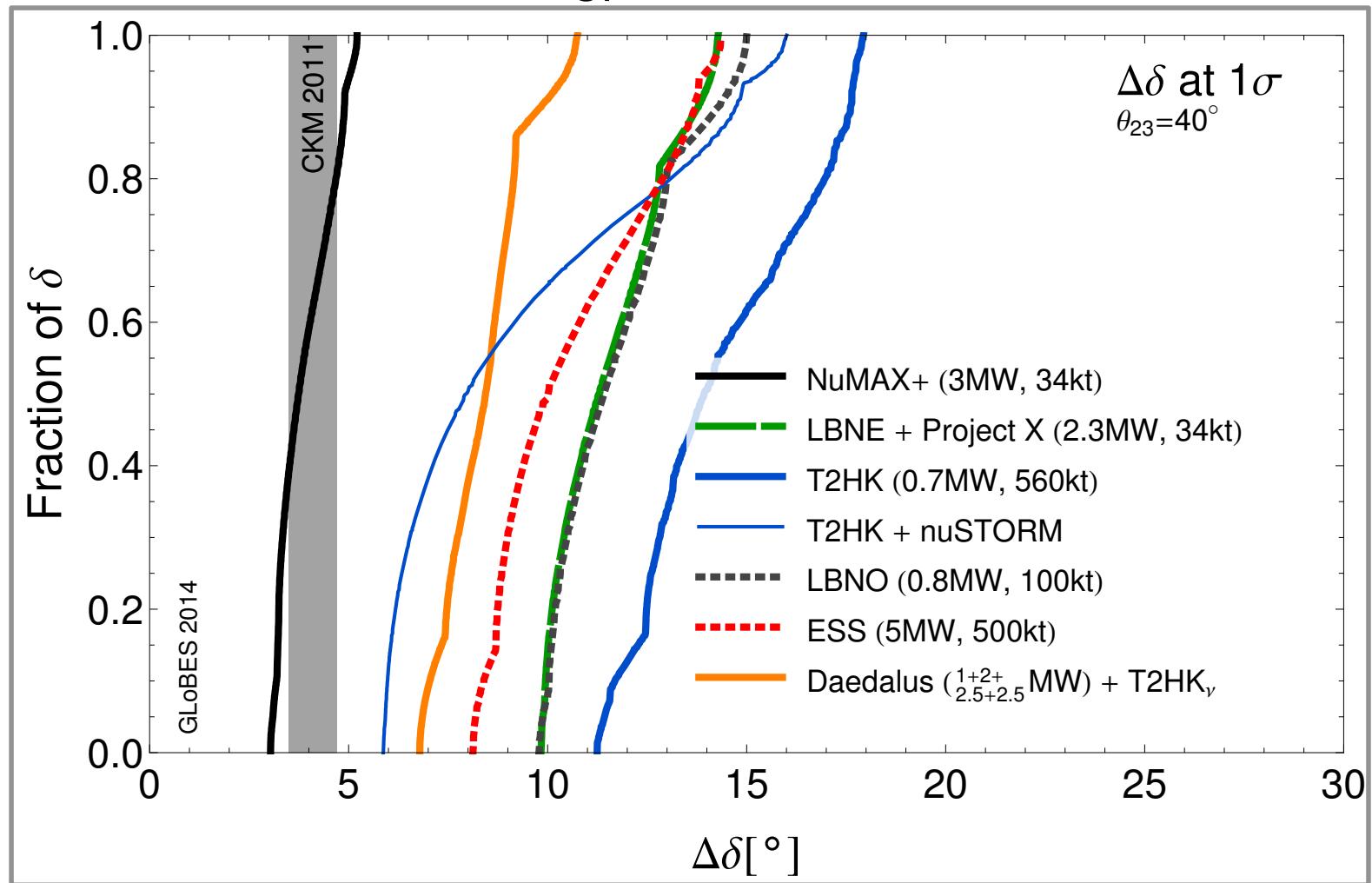
Neutrino interactions at nuSTORM

- ❑ Example of CCQE measurement errors: ~2-3%
 - Data for ν_μ and $\bar{\nu}_e$ cross-sections
 - Systematic errors completely dominated by detector



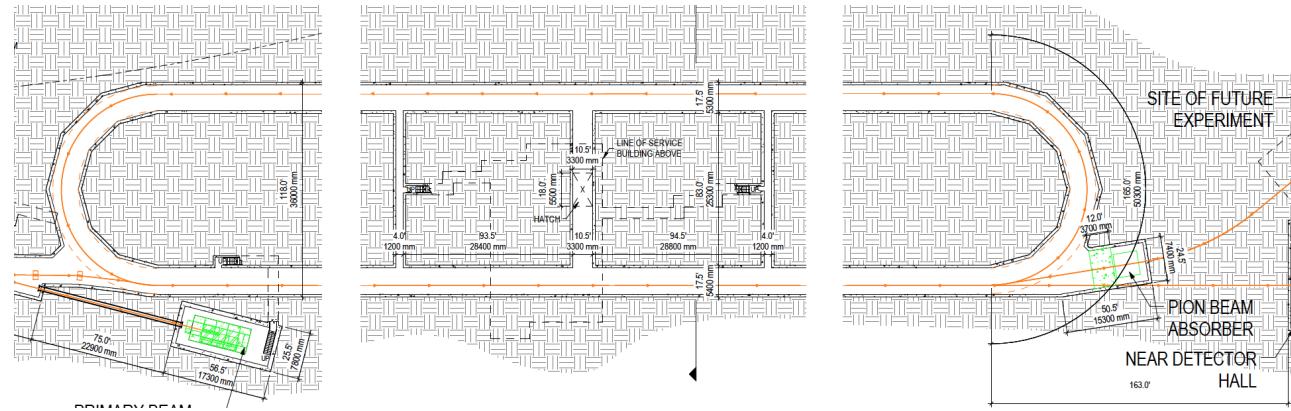
Neutrino interactions at nuSTORM

- Influence of nuSTORM cross-section measurements on DUNE and T2HK δ_{CP} measurements

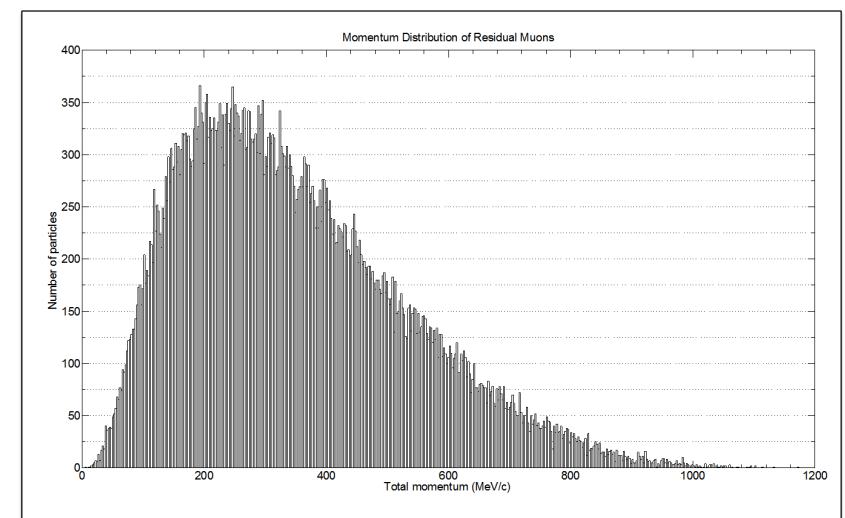
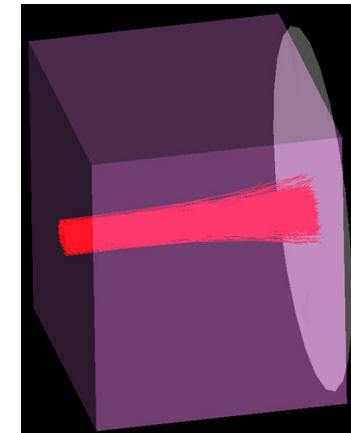
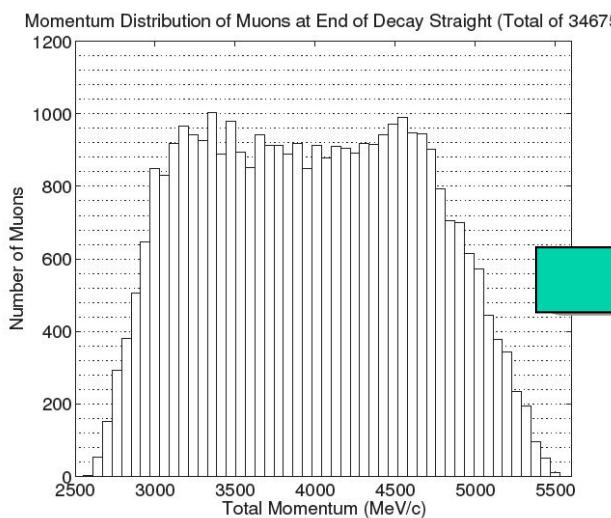


nuSTORM as 6D cooling testbed

- nuSTORM: testbed for 6D muon cooling experiment
 - At end of straight: 3.5 m iron pion absorber

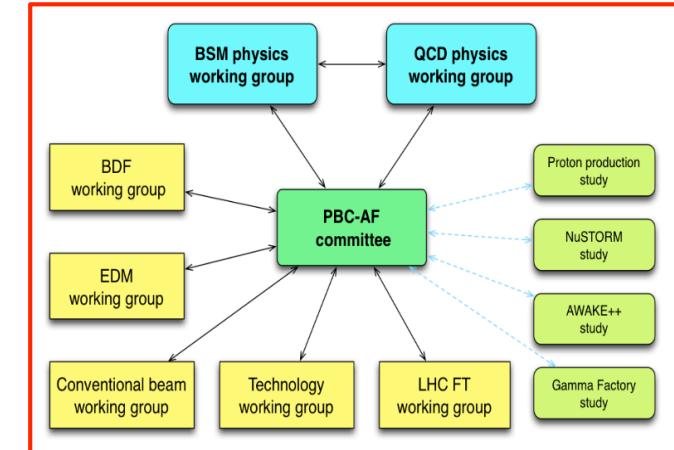
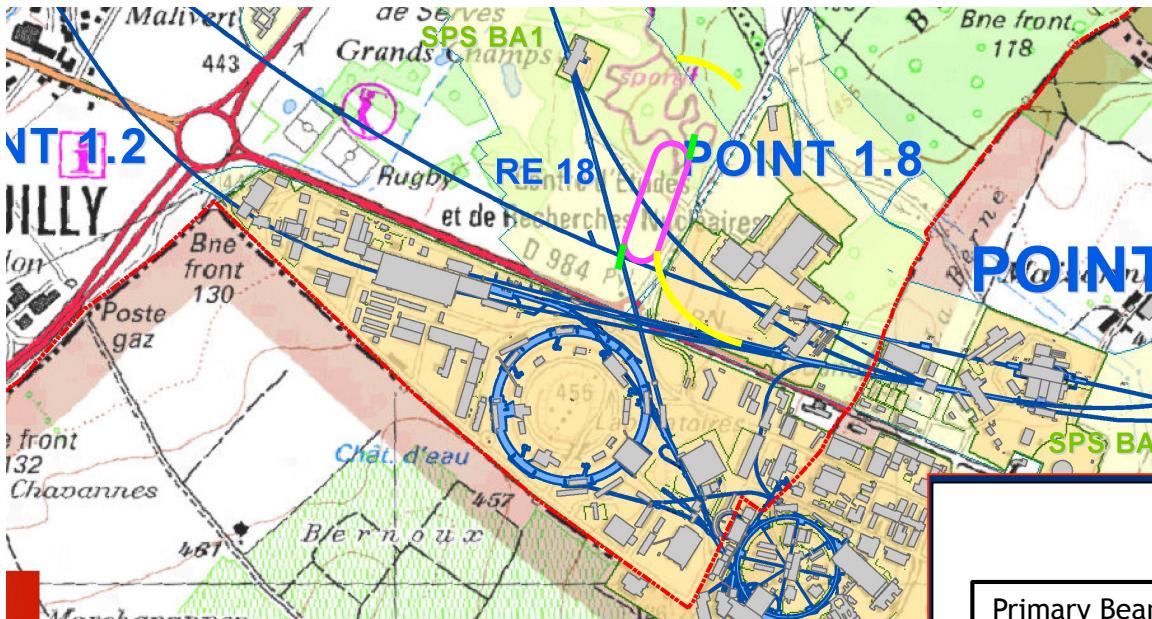


- After absorber: 10^{10} μ /pulse between 100-300 MeV/c



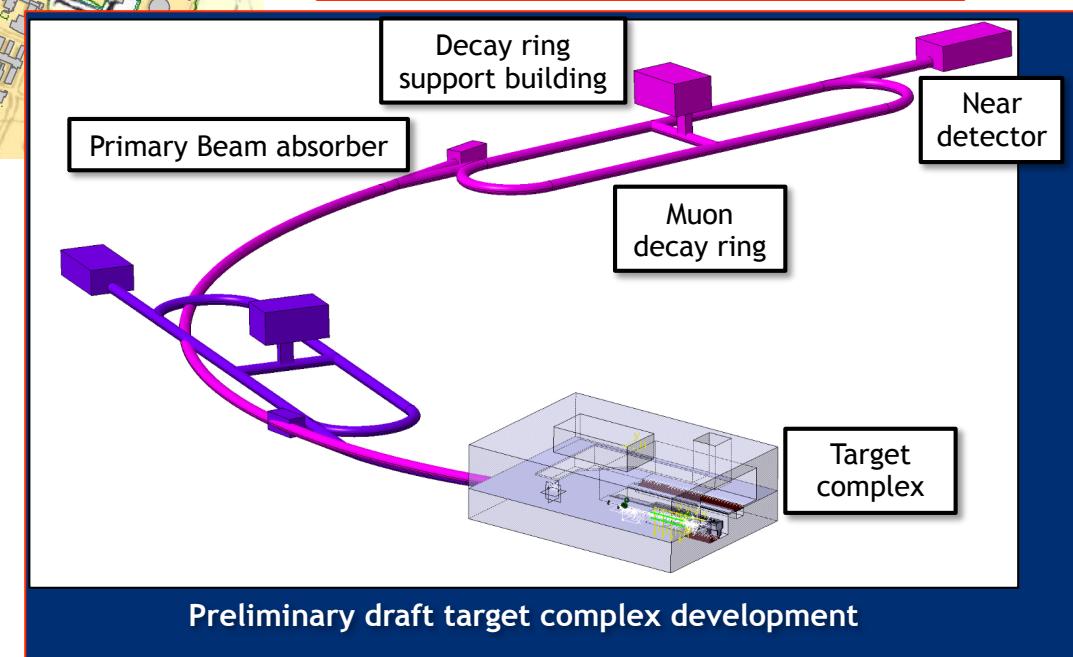
nuSTORM siting at CERN

- nuSTORM at CERN (Physics Beyond Colliders study group)



- Complementary physics programme at CERN to long-baseline experiments in Japan and USA

K. Long



Conclusions

- ❑ There is a physics case beyond Hyper-K and DUNE: test for three-neutrino paradigm and beyond Standard Model physics
- ❑ Design Study for a Neutrino Factory (IDS-NF)
 - Feasible Neutrino Factory has been designed
 - Staging of Neutrino Factory (ie. NuMAX) delivers physics at each stage
 - Provides a route to deliver high-energy muon collider
- ❑ **MICE has demonstrated muon ionization cooling for the first time: it shows that Neutrino Factory is feasible**
- ❑ NuSTORM could be first neutrino beam from muon decay
 - To be used for neutrino cross-section measurements and sterile neutrino search
 - Complementary to Hyper-K and DUNE – maximises physics impact of long-baseline experiments