

# An Effective Theory of Neutrino

Systematic decomposition of the neutrinoless double beta decay operator

Toshihiko Ota



based on

Florian Bonnet, Martin Hirsch, TO, Walter Winter

JHEP **1303** (2013) 055

arXiv.1212.3045

If the SM is a low- $E$  effective model of a fundamental theory...

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}}$$

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$\Lambda_{\text{NP}}$  : A typical scale of New physics

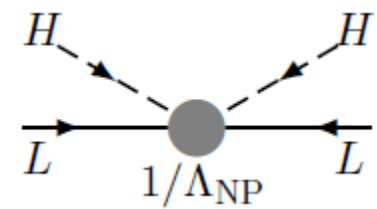
Effective operators are a typical low- $E$  remnant of New physics

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Weinberg op.

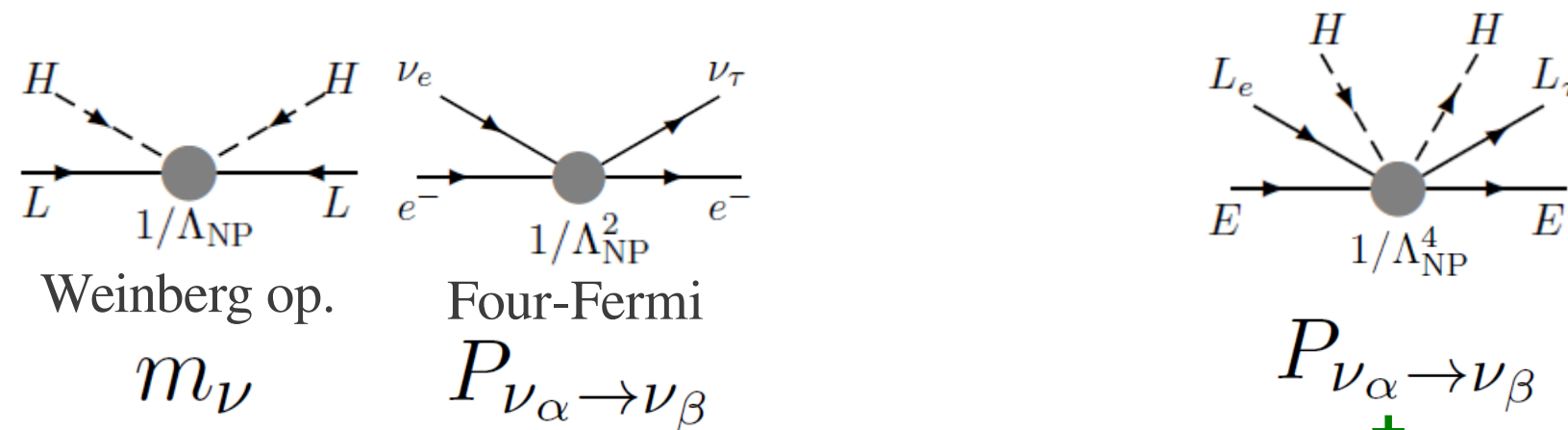
$m_\nu$

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Non-standard (**LFV**) neutrino ints  
→ Talk by O.Yasuda (Apr), J. Sato (Aug)

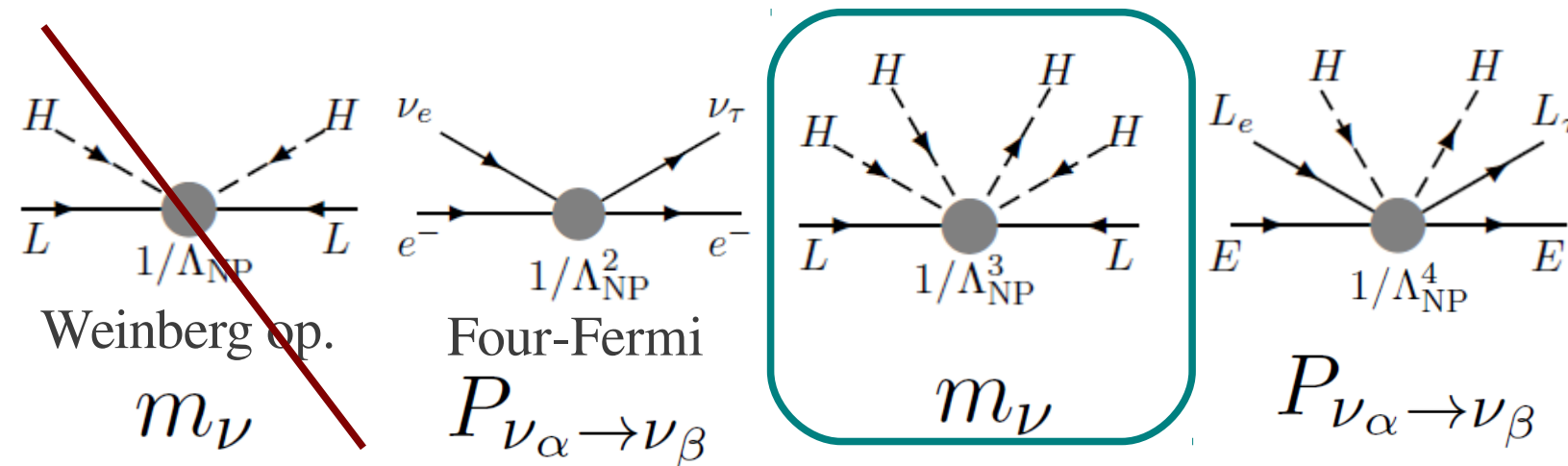
Related through  $SU(2)$  → Charged **LFV** (in SUSY)  
→ Talk by M. Nagai

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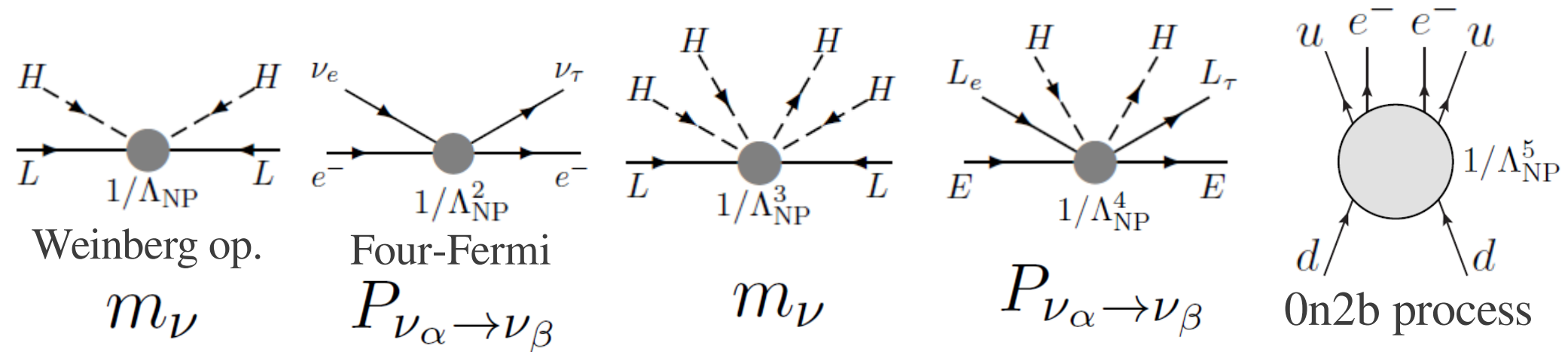


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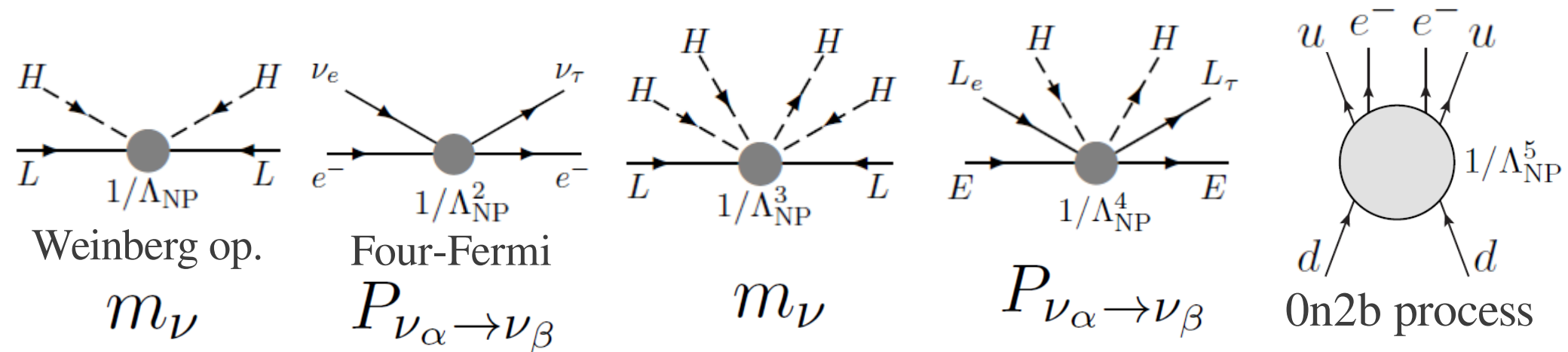


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High  $E$  completion @  $\Lambda_{\text{NP}}$

Seesaw mech.  
(tree)

Seesaw shaved with Occam's razor  
→ Talk by M. Ibe (Aug)

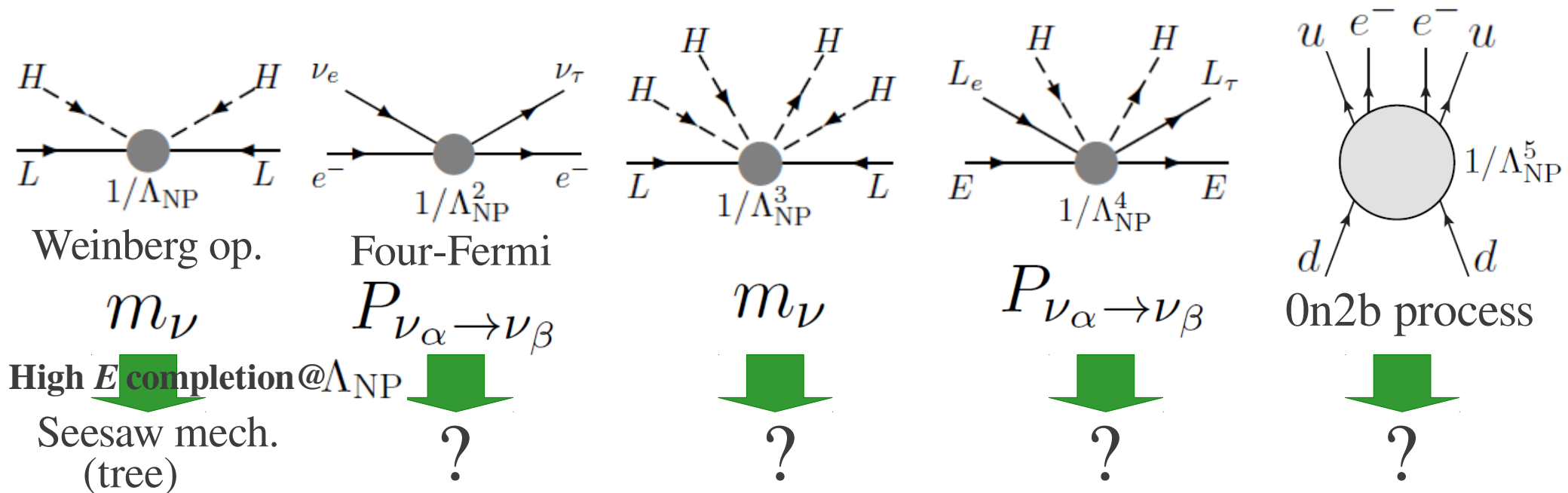


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What do these eff. ops. suggest to new physics at high  $E$  scales?

**Exhaustive bottom-up approach**

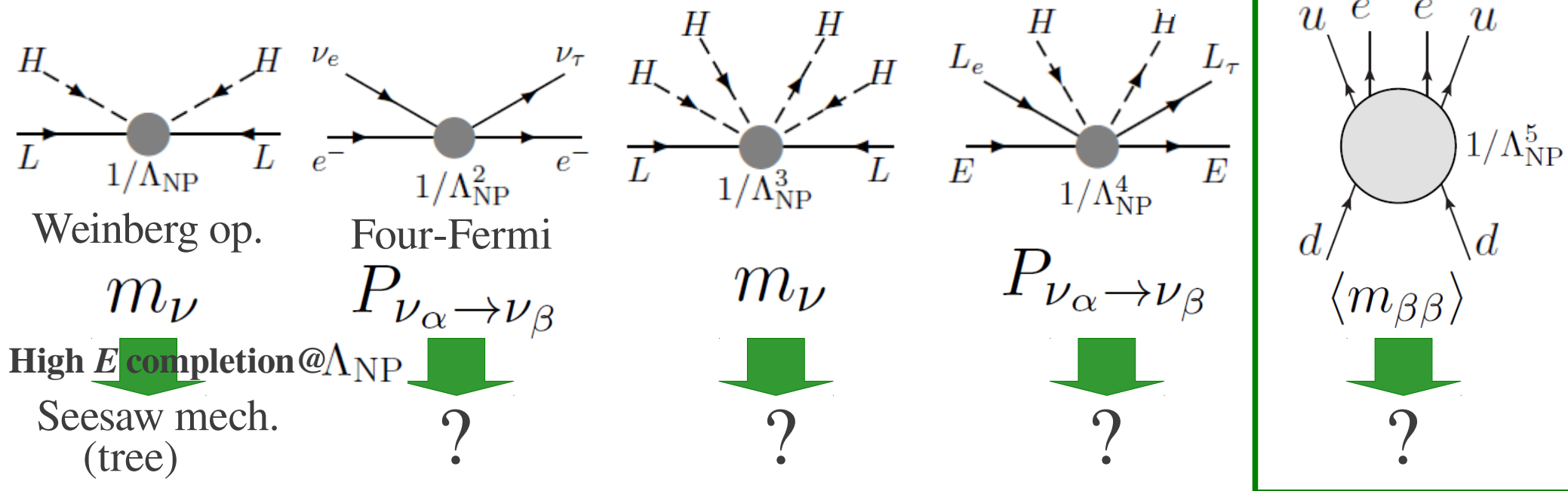
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Effective operators are a typical low- $E$  remnant

*We focus on  $d=9$  op in this talk*



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**Exhaustive bottom-up approach**

# Outline

New Physics ( $d=9$ ) contributions in neutrinoless double beta decay ( $0\nu 2b$ )

## 1 *Motivation: Why $0\nu 2b$ ? Why $dim=9$ ops?*

$d=9$  ops  $\rightarrow$  half-life time of  $0\nu 2b$  processes

*“How sensitive  $0\nu 2b$  experiments to the  $d=9$  ops?”*

## 2 *What do the $d=9$ ops suggest to TeV scale physics?*

$d=9$  ops  $\rightarrow$  decompose them to the fundamental ints.

$\rightarrow$  list the TeV signatures of each completion

*“The list helps us to discriminate the models”*

## 3 *Seeking a relation to the models at the TeV scale*

TeV scale models with LNV  $\rightarrow$  *Models for radiative neutrino masses*

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**Summary**



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TeV scale models with LNV  $\rightarrow$  *Models for radiative neutrino masses*

- In SM+3nu, **0n2b exp** are sensitive to

**Effective nu mass**

$$\langle m_{\beta\beta} \rangle \equiv \sum_{i=1}^3 (U_e^i)^2 m_i$$

$$U_e^1 = c_{12}c_{13}$$

$$U_e^2 = s_{12}c_{13}e^{i\alpha}$$

$$U_e^3 = s_{13}e^{i\beta}$$

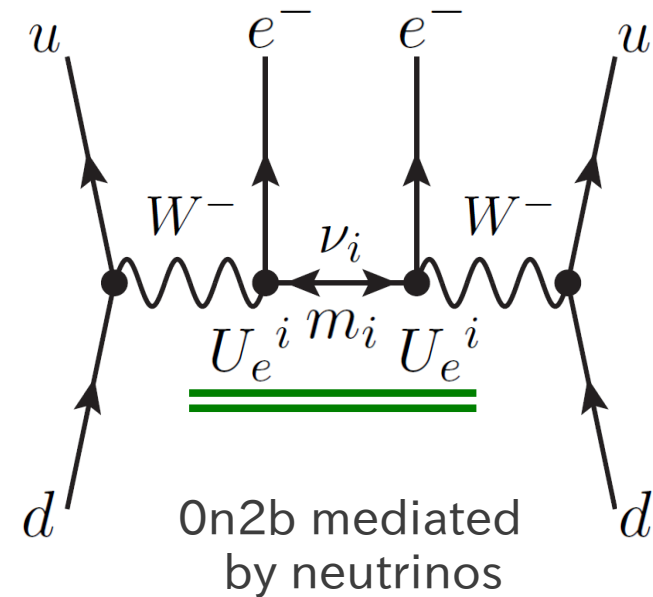
Normal hierarchy

$$m_1 = m_0, m_2 = \sqrt{\Delta m_{21}^2 + m_0^2}, m_3 = \sqrt{\Delta m_{31}^2 + m_0^2}$$

Inverted hierarchy

$$m_1 = \sqrt{|\Delta m_{31}^2| + m_0^2}, m_2 = \sqrt{\Delta m_{21}^2 + |\Delta m_{31}^2| + m_0^2},$$

$$m_3 = m_0$$



$m_0$  represents the lightest neutrino mass  
 $\alpha$  and  $\beta$  are Majorana phases

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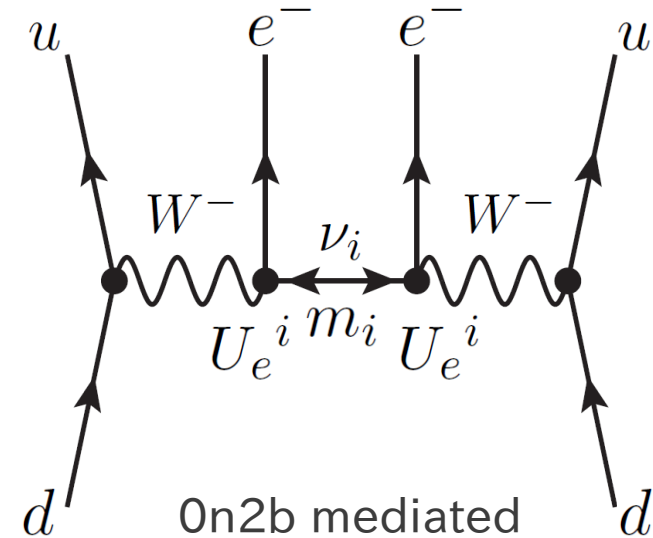
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0n2b mediated by neutrinos

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- Oscillation exp** told us... e.g., Gonzalez-Garcia Maltoni Salvado Schwetz, JHEP 1212 (2012) 123

$$s_{12}^2 = 0.3, \quad s_{23}^2 = 0.41(0.59), \quad s_{13}^2 = 0.023,$$

$$\Delta m_{21}^2 = 7.5 \cdot 10^{-5} \text{ eV}^2, \quad |\Delta m_{31}^2| = 2.5 \cdot 10^{-3} \text{ eV}^2$$

So far, we know

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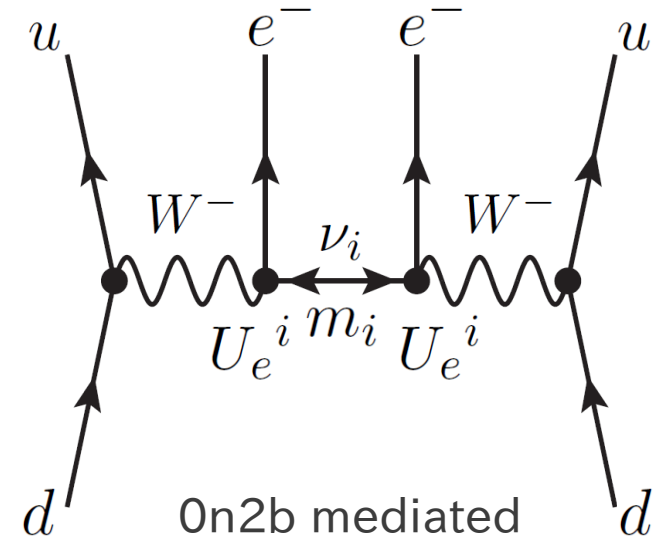
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- Cosmological obs** are sensitive to the other combination of params....

→Talk by M. Hasegawa (Aug)

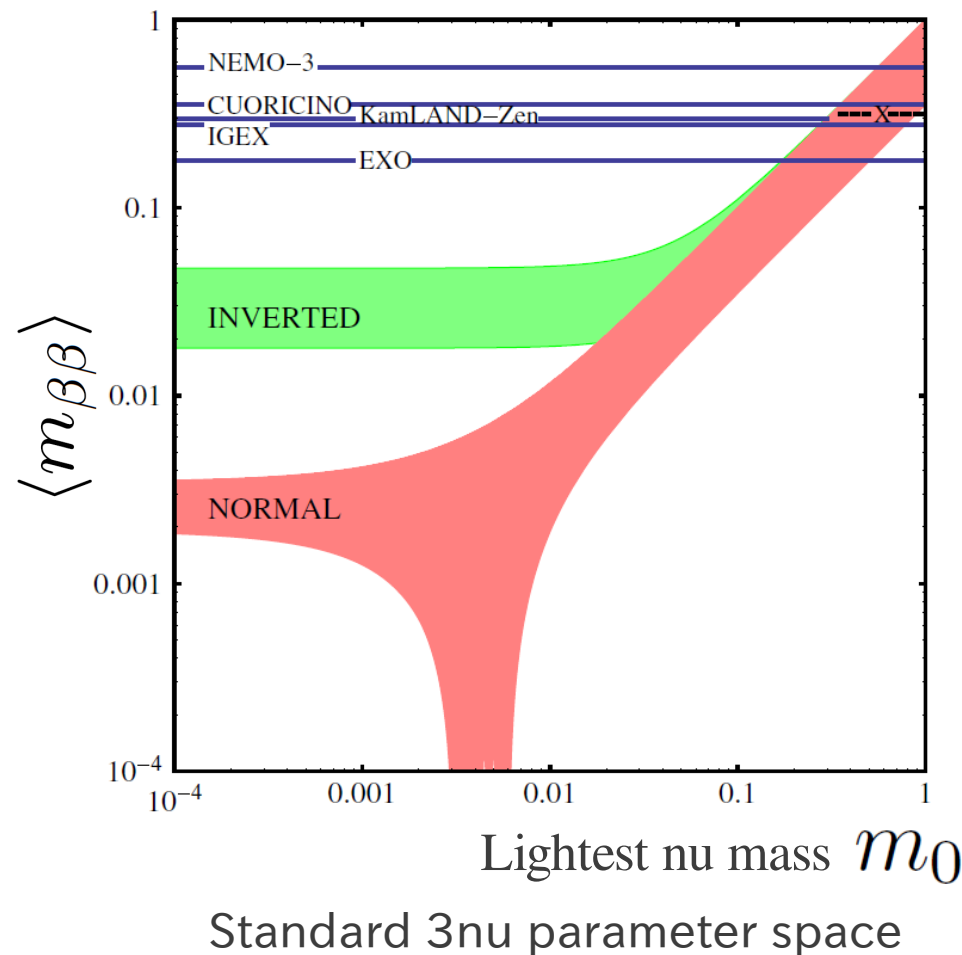


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Sum of nu masses

$$\sum_{i=1}^3 m_i (\simeq 3m_0 \text{ if } m_0 \gtrsim 0.1 \text{ eV})$$

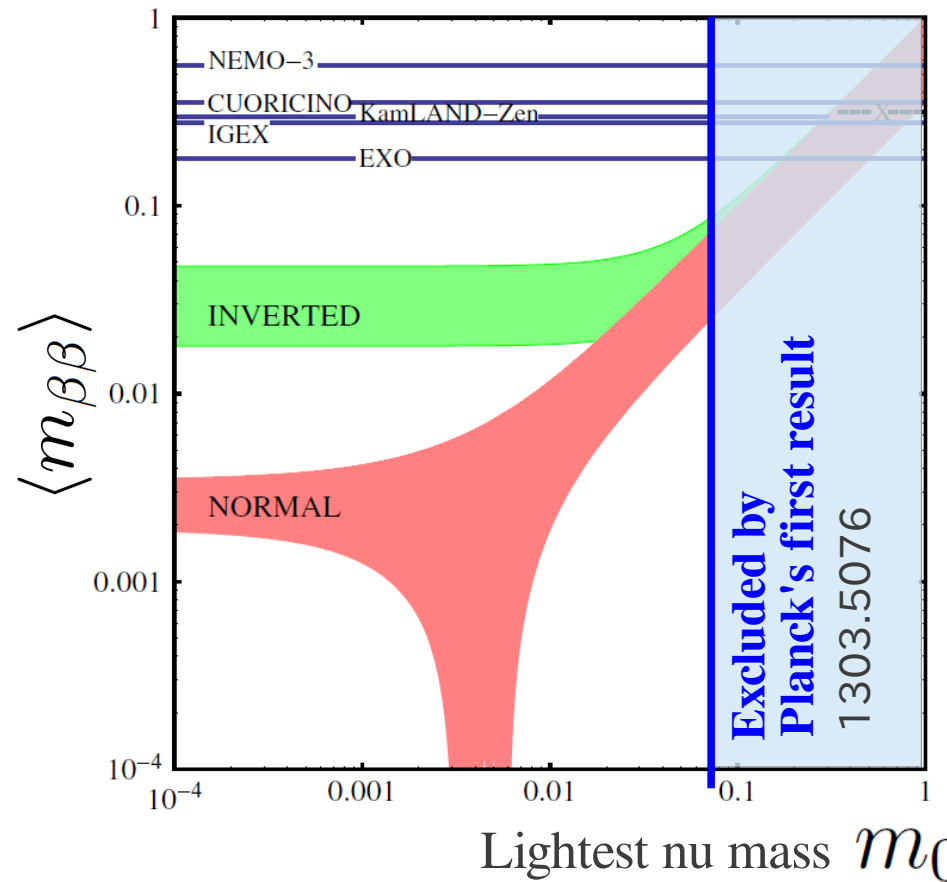


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**WMAP9** (combined)

1212.5226

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**SPT** reports  
non-zero  $m_{\text{Nu}}$ ?

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Talk by I. Shimizu  
(Apr)

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PRL110 (2013) 062502

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### EXO-200

PRL109 (2012) 032505

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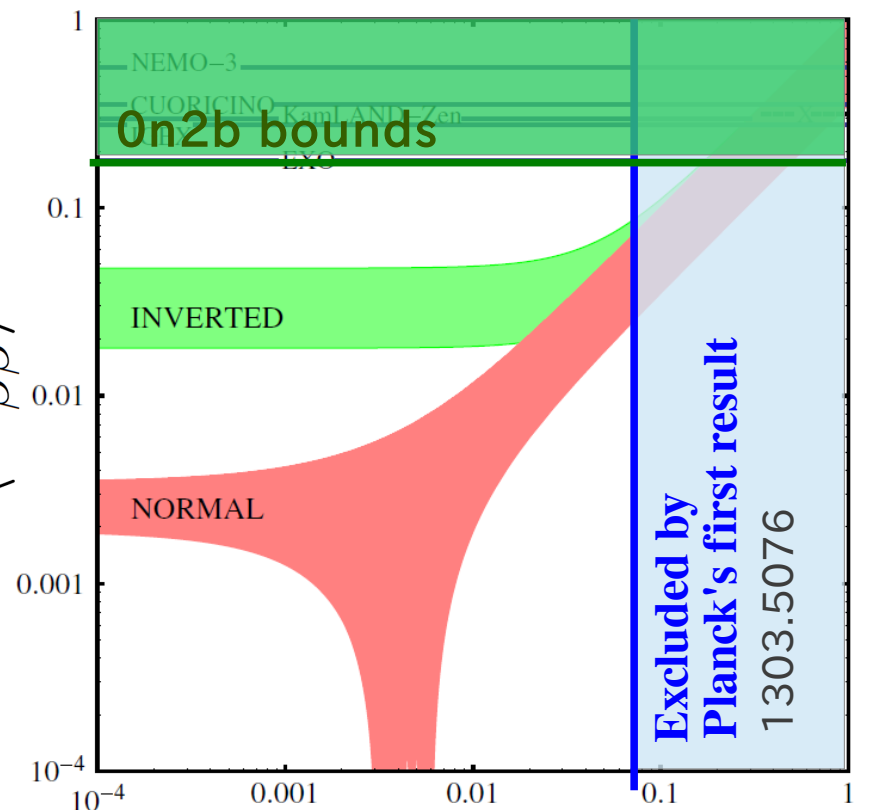
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1307.4720

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→ 0.01 eV  
In future  
Standard 3nu parameter space

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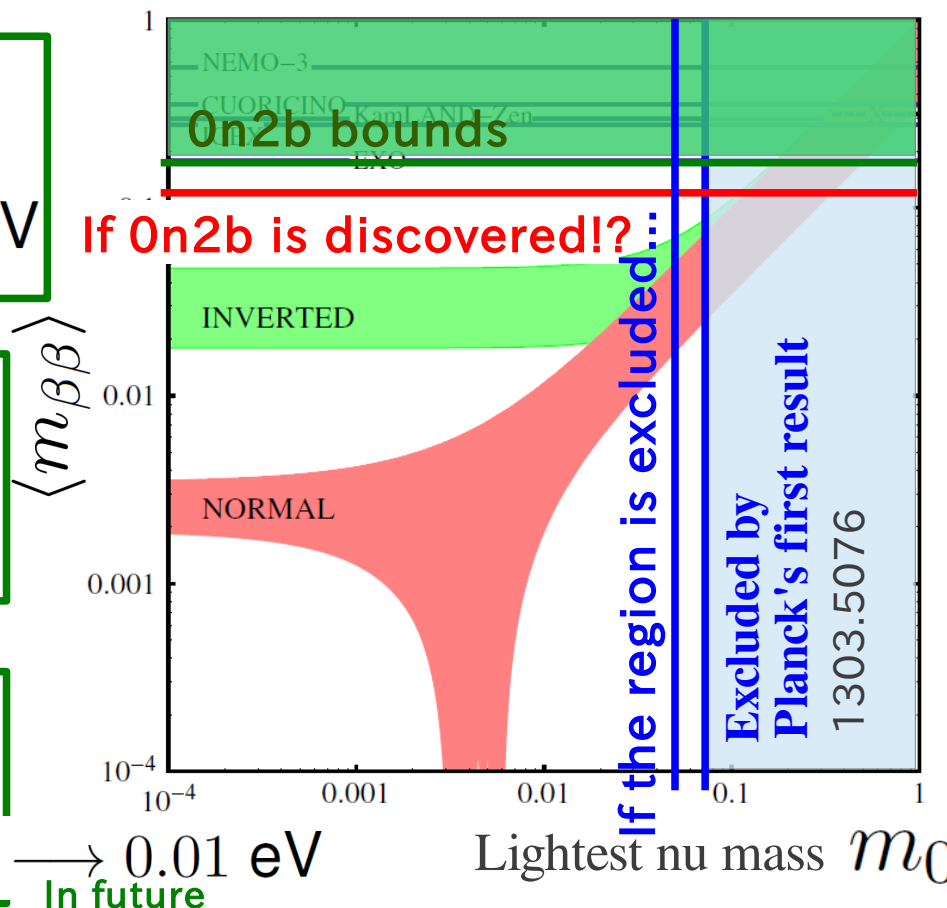
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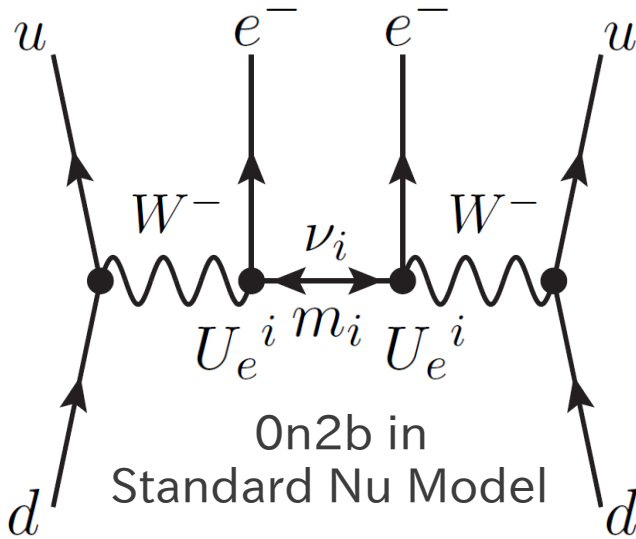
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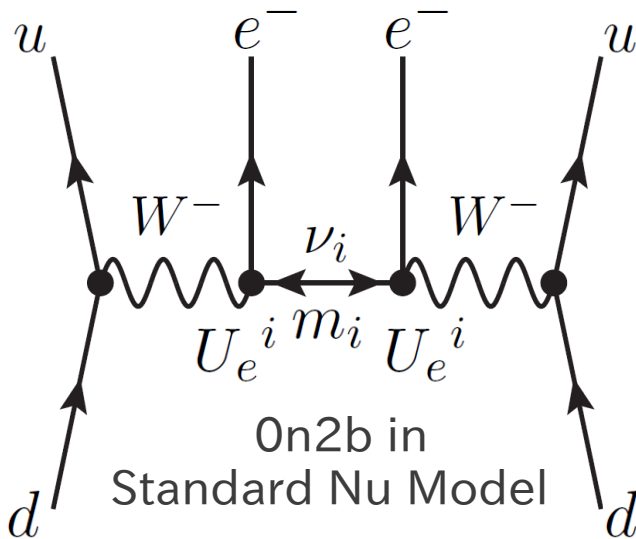
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**Q:** If, in future, they will conflict with each other, what can we learn from them?

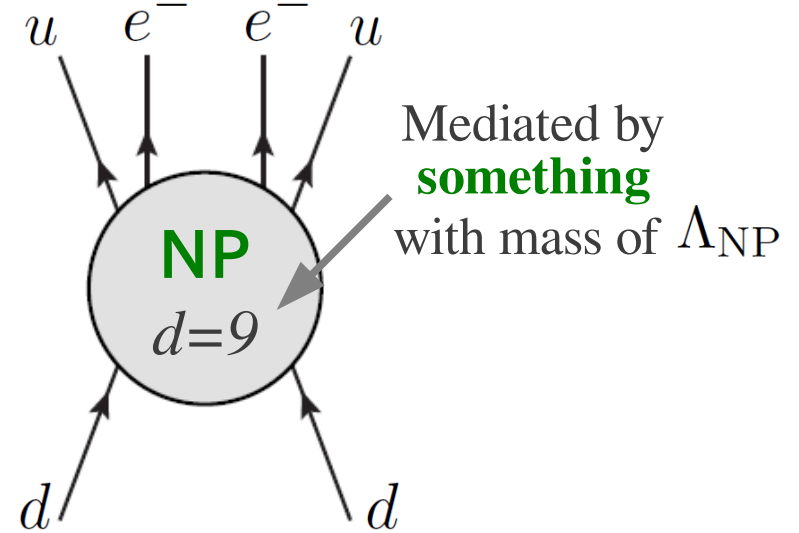
- If we have an additional **New Physics** contribution to  $0\nu 2b$ ...



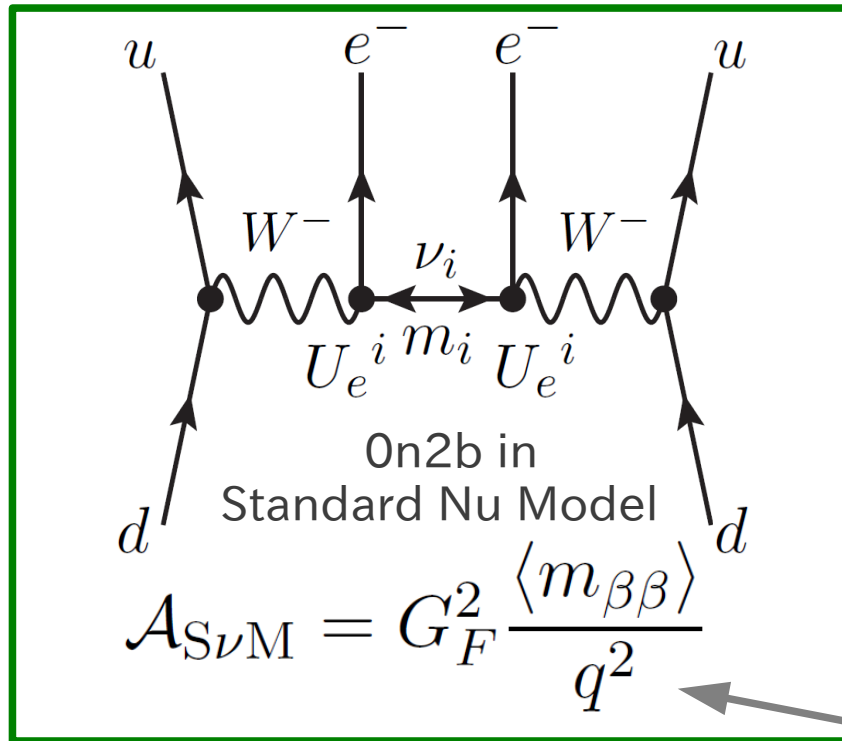
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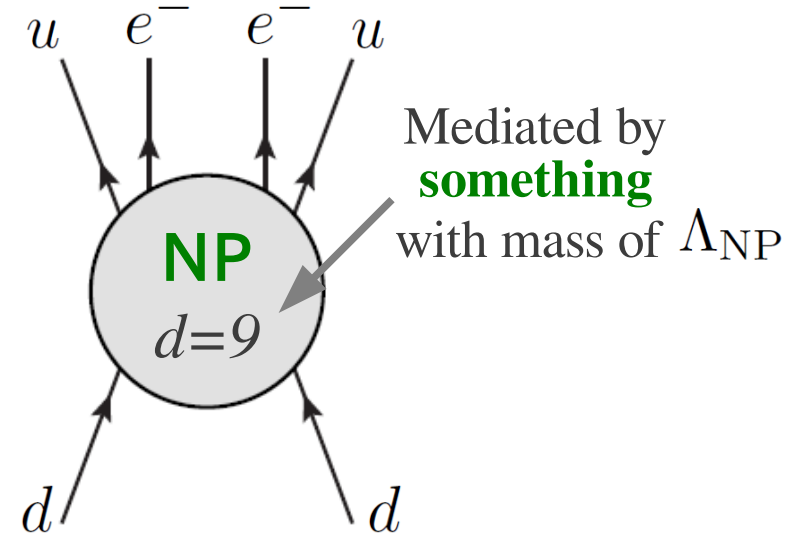
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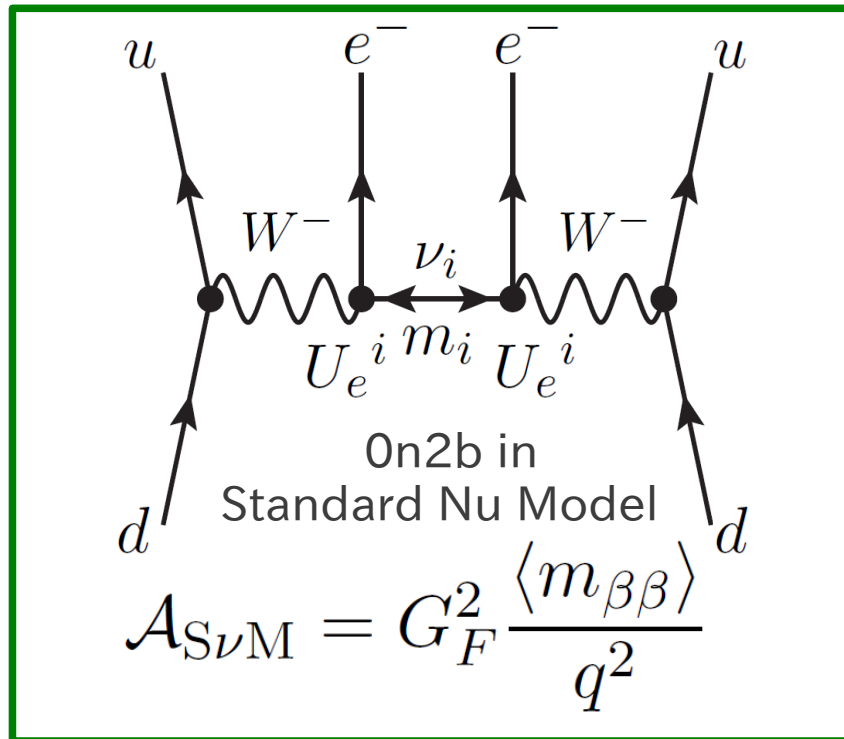
~100 MeV

Current exp. limit

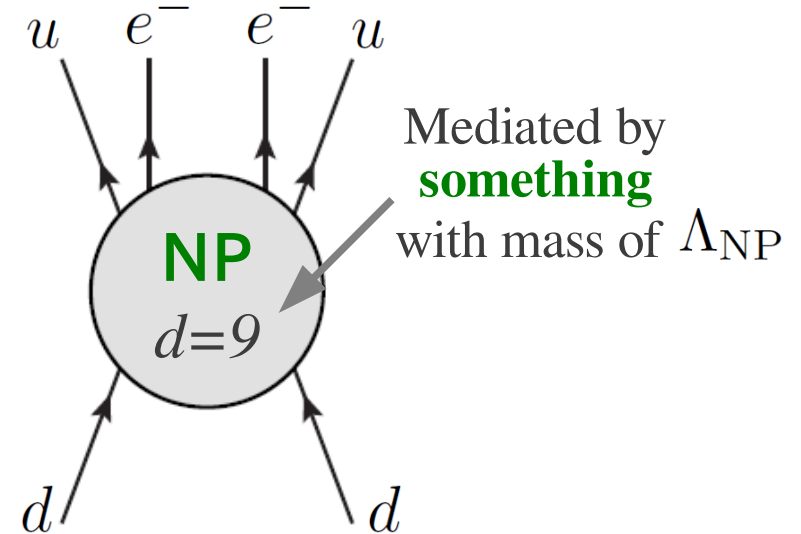
$$10^{25} [\text{yr}] < T_{1/2}^{0\nu 2\beta} \propto 1/|\mathcal{A}_{S\nu M}|^2$$

A typical size of momentum that neutrino propagating in nucleus has

- If we have an additional **New Physics** contribution to 0n2b...



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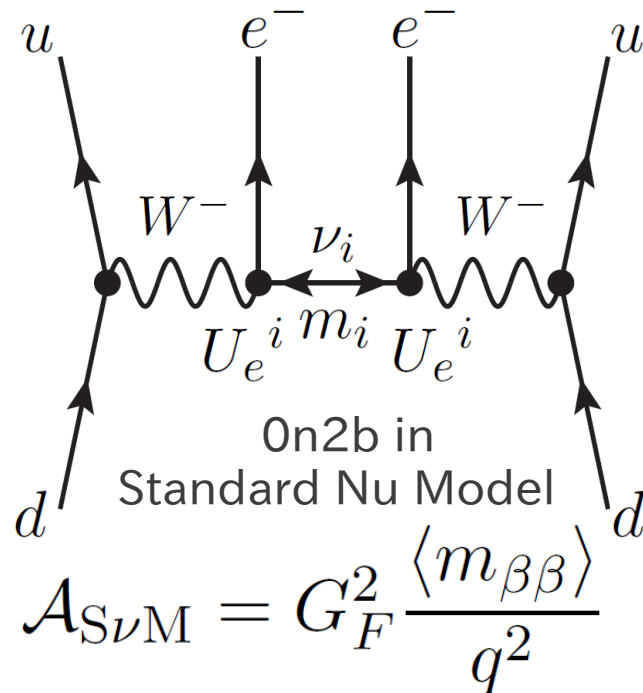
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$$10^{25} [\text{yr}] < T_{1/2}^{0\nu 2\beta} \propto 1/|\mathcal{A}_{S\nu M}|^2 \Rightarrow \langle m_{\beta\beta} \rangle < 0.3 [\text{eV}]$$

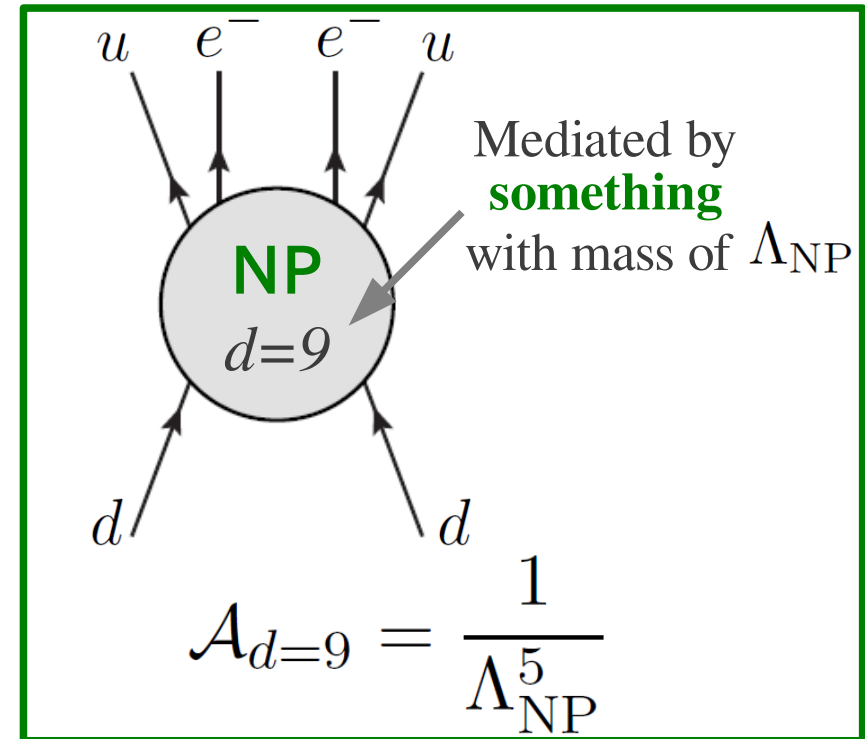
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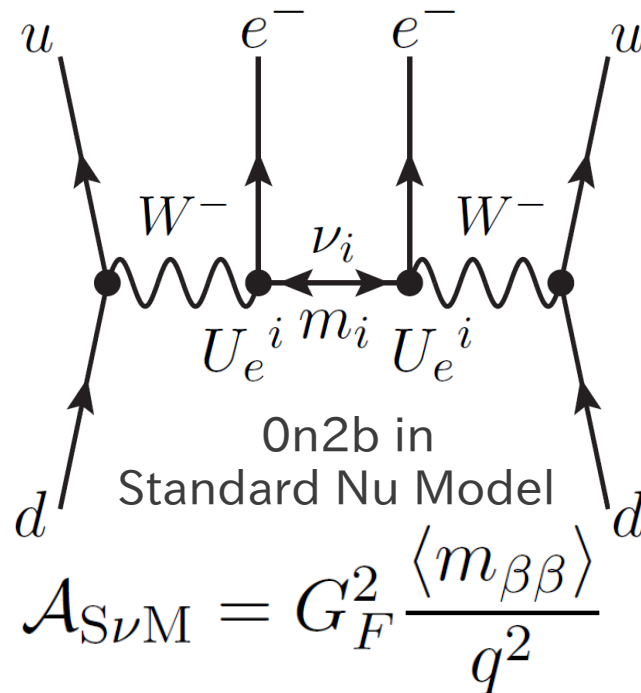
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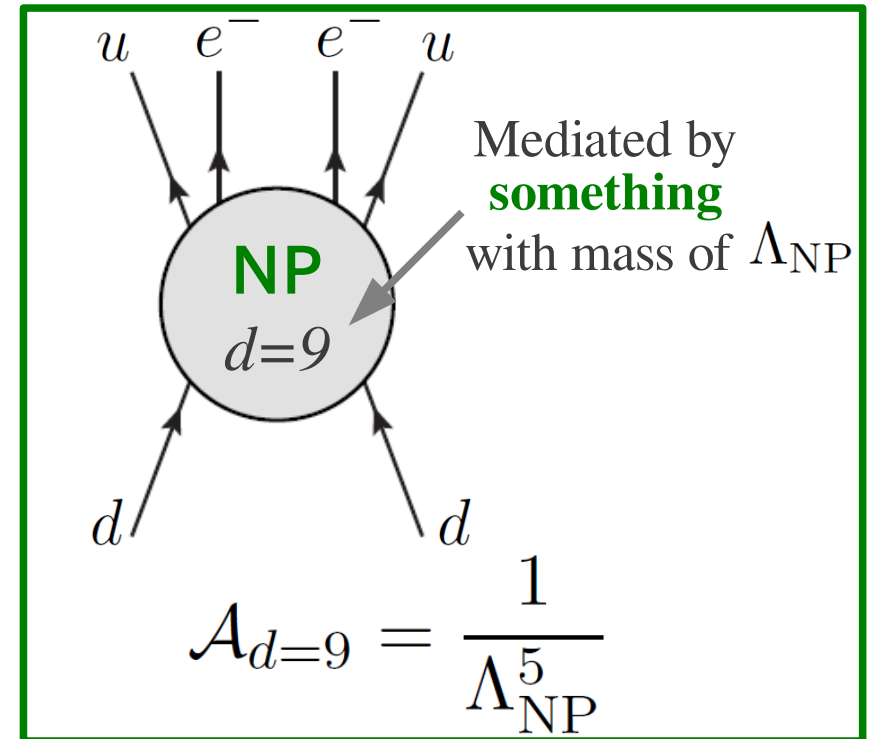
Sensitive to

$$\propto 1/|\mathcal{A}_{d=9}|^2$$

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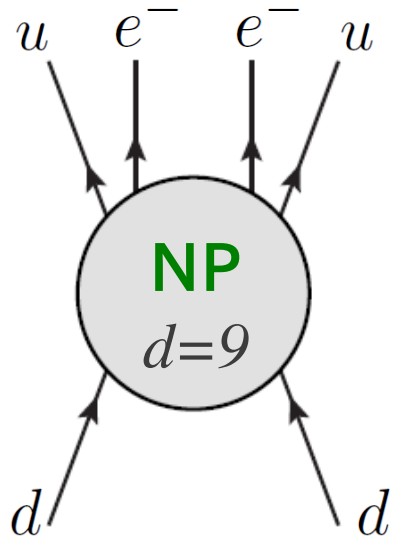
Current exp. limit

$$10^{25} [\text{yr}] < T_{1/2}^{0\nu 2\beta} \propto 1/|\mathcal{A}_{S\nu M}|^2 \Rightarrow \langle m_{\beta\beta} \rangle < 0.3 [\text{eV}]$$

$$\propto 1/|\mathcal{A}_{d=9}|^2 \Rightarrow \Lambda_{NP} > \mathcal{O}(1) [\text{TeV}]$$

LHC range!

0n2b exps are sensitive to not only Majorana neutrino mass but also NP at TeV.



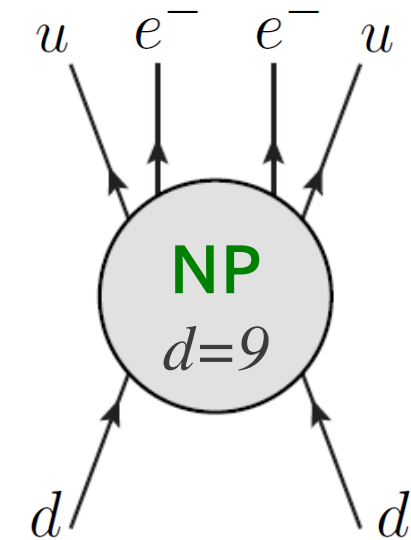
...falls into the following 5 types of effective ops.

$$\mathcal{L}_{d=9} = \frac{G_F^2}{2m_P} \left[ \sum_{i=1}^3 \epsilon_i^{\{XY\}Z} (\mathcal{O}_i)_{\{XY\}Z} + \sum_{i=5}^4 \epsilon_i^{XY} (\mathcal{O}_i)_{XY} \right],$$

$$(\mathcal{O}_1) \equiv J_X J_Y j_Z, \quad (\mathcal{O}_4) \equiv (J_X)^{\mu\nu} (J_Y)_\mu (j)_\nu, \quad J_X = \bar{u} \Gamma P_X d$$

$$(\mathcal{O}_2) \equiv (J_X)^{\mu\nu} (J_Y)_{\mu\nu} j_Z, \quad (\mathcal{O}_5) \equiv J_X (J_Y)_\mu (j)_\mu \quad j_X = \bar{e} \Gamma P_X e^c$$

$$(\mathcal{O}_3) \equiv (J_X)^\mu (J_Y)_\mu j_Z,$$



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$$\mathcal{L}_{d=9} = \frac{G_F^2}{2m_P} \left[ \sum_{i=1}^3 \boxed{\epsilon_i^{\{XY\}Z}} (\mathcal{O}_i)_{\{XY\}Z} + \sum_{i=5}^4 \boxed{\epsilon_i^{XY}} (\mathcal{O}_i)_{XY} \right],$$

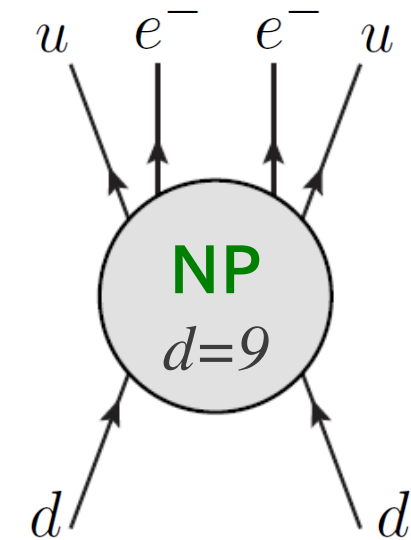
$$\begin{aligned} (\mathcal{O}_1) &\equiv J_X J_Y j_Z, & (\mathcal{O}_4) &\equiv (J_X)^{\mu\nu} (J_Y)_\mu (j)_\nu, & J_X &= \bar{u} \Gamma P_X d \\ (\mathcal{O}_2) &\equiv (J_X)^{\mu\nu} (J_Y)_{\mu\nu} j_Z, & (\mathcal{O}_5) &\equiv J_X (J_Y)_\mu (j)_\mu & j_X &= \bar{e} \Gamma P_X e^c \\ (\mathcal{O}_3) &\equiv (J_X)^\mu (J_Y)_\mu j_Z, \end{aligned}$$

● Nice (&compact) formula to calculate the half-life time: Paes et al. PLB498 (2001) 35

$$\left( T_{1/2}^{0\nu 2\beta} \right)_{d=9}^{-1} = G_1 \left| \sum_{i=1}^3 \boxed{\epsilon_i} \mathcal{M}_i \right|^2 + G_2 \left| \sum_{i=4}^5 \boxed{\epsilon_i} \mathcal{M}_i \right|^2 + G_3 \text{Re} \left[ \left( \sum_{i=1}^3 \boxed{\epsilon_i} \mathcal{M}_i \right) \left( \sum_{i=4}^5 \boxed{\epsilon_i} \mathcal{M}_i \right)^* \right]$$

$$\left( T_{1/2}^{0\nu 2\beta} \right)_{S\nu M}^{-1} = G_1 \left| \frac{\langle m_{\beta\beta} \rangle}{m_e} \left[ \mathcal{M}_{GT} - \frac{g_V^2}{g_A^2} \mathcal{M}_F \right] \right|^2$$

$\mathcal{M}_i$  Nuclear matrix elements  
 $G_i$  Phase space factors



...falls into the following 5 types of effective ops.

$$\mathcal{L}_{d=9} = \frac{G_F^2}{2m_P} \left[ \sum_{i=1}^3 \epsilon_i^{\{XY\}Z} (\mathcal{O}_i)_{\{XY\}Z} + \sum_{i=5}^4 \epsilon_i^{XY} (\mathcal{O}_i)_{XY} \right],$$

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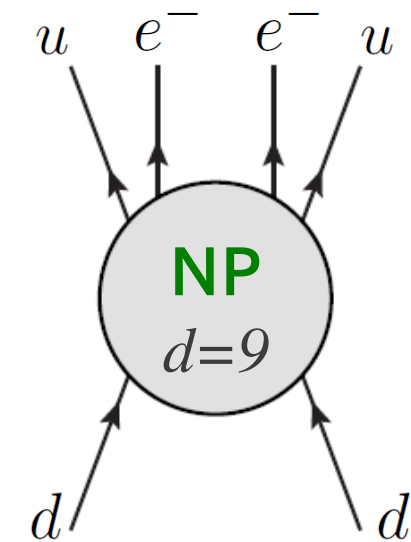
● Nice (&compact) formula to calculate the half-life time: Paes et al. PLB498 (2001) 35

$$\begin{aligned} \left( T_{1/2}^{0\nu 2\beta} \right)_{d=9}^{-1} &= G_1 \left| \sum_{i=1}^3 \epsilon_i \mathcal{M}_i \right|^2 + G_2 \left| \sum_{i=4}^5 \epsilon_i \mathcal{M}_i \right|^2 + G_3 \text{Re} \left[ \left( \sum_{i=1}^3 \epsilon_i \mathcal{M}_i \right) \left( \sum_{i=4}^5 \epsilon_i \mathcal{M}_i \right)^* \right] \\ \left( T_{1/2}^{0\nu 2\beta} \right)_{S\nu M}^{-1} &= G_1 \left| \frac{\langle m_{\beta\beta} \rangle}{m_e} \left[ \mathcal{M}_{GT} - \frac{g_V^2}{g_A^2} \mathcal{M}_F \right] \right|^2 \end{aligned}$$

$\mathcal{M}_i$  Nuclear matrix elements  
 $G_i$  Phase space factors

Q: What is the high  $E$  (TeV) origin of these  $d=9$  effective ops?

$d=9$  ops.



...falls into the following 5 types of effective ops.

$$\mathcal{L}_{d=9} = \frac{G_F^2}{2m_P} \left[ \sum_{i=1}^3 \epsilon_i^{\{XY\}Z} (\mathcal{O}_i)_{\{XY\}Z} + \sum_{i=5}^4 \epsilon_i^{XY} (\mathcal{O}_i)_{XY} \right],$$

$$\begin{aligned} (\mathcal{O}_1) &\equiv J_X J_Y j_Z, & (\mathcal{O}_4) &\equiv (J_X)^{\mu\nu} (J_Y)_\mu (j)_\nu, & J_X &= \bar{u} \Gamma P_X d \\ (\mathcal{O}_2) &\equiv (J_X)^{\mu\nu} (J_Y)_{\mu\nu} j_Z, & (\mathcal{O}_5) &\equiv J_X (J_Y)_\mu (j)_\mu & j_X &= \bar{e} \Gamma P_X e^c \\ (\mathcal{O}_3) &\equiv (J_X)^\mu (J_Y)_\mu j_Z, \end{aligned}$$

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Q: What is the high  $E$  (TeV) origin of these  $d=9$  effective ops?

$d=9$  ops. **bottom-up**  $\rightarrow$  List high  $E$  (TeV) completions  $\rightarrow$  complementarity with LHC

# Outline

New Physics ( $d=9$ ) contributions in neutrinoless double beta decay ( $0\nu 2b$ )

## 1 *Motivation: Why $0\nu 2b$ ? Why $dim=9$ ops?*

$d=9$  ops  $\rightarrow$  half-life time of  $0\nu 2b$  processes

*“How sensitive  $0\nu 2b$  experiments to the  $d=9$  ops?”*

## 2 *What do the $d=9$ ops suggest to TeV scale physics?*

$d=9$  ops  $\rightarrow$  decompose them to the fundamental ints.

$\rightarrow$  list the TeV signatures of each completion

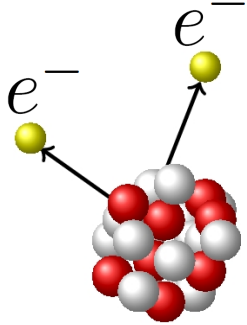
*“The list helps us to discriminate the models”*

## 3 *Seeking a relation to the models at the TeV scale*

TeV scale models with LNV  $\rightarrow$  *Models for radiative neutrino masses*

## ● Exhaustive bottom-up approach

0n2b experiments



Discover!

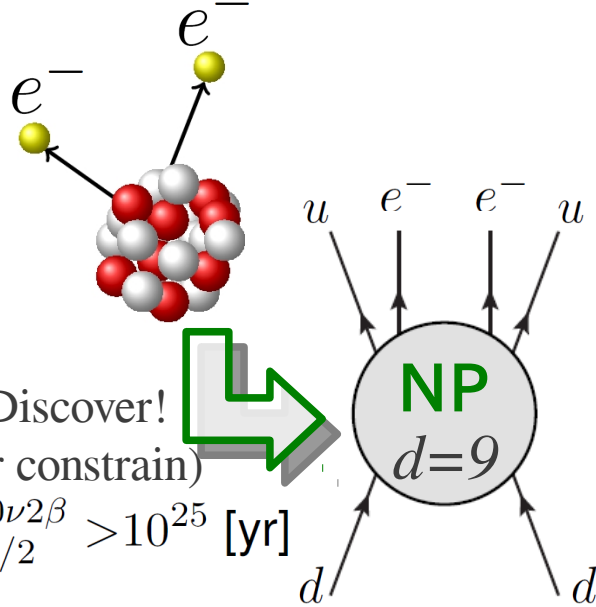
(or constrain)

$$T_{1/2}^{0\nu 2\beta} > 10^{25} \text{ [yr]}$$



## Exhaustive bottom-up approach

On2b experiments



Discover!

(or constrain)

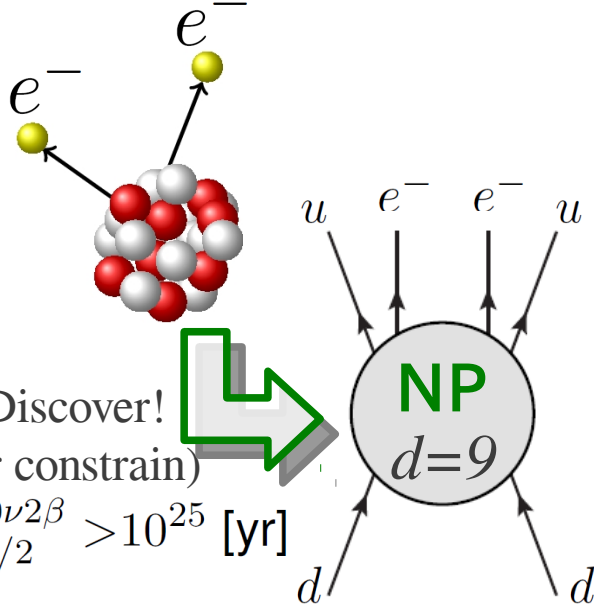
$$T_{1/2}^{0\nu 2\beta} > 10^{25} \text{ [yr]}$$

$$\mathcal{L}_{d=9} = \frac{1}{\Lambda_{\text{NP}}^5} \mathcal{O}_{d=9}^{\text{tree}} @ \Lambda_{\text{EW}}$$

$$\Lambda_{\text{NP}} > \mathcal{O}(1) \text{ [TeV]}$$

## Exhaustive bottom-up approach

On2b experiments



Discover!

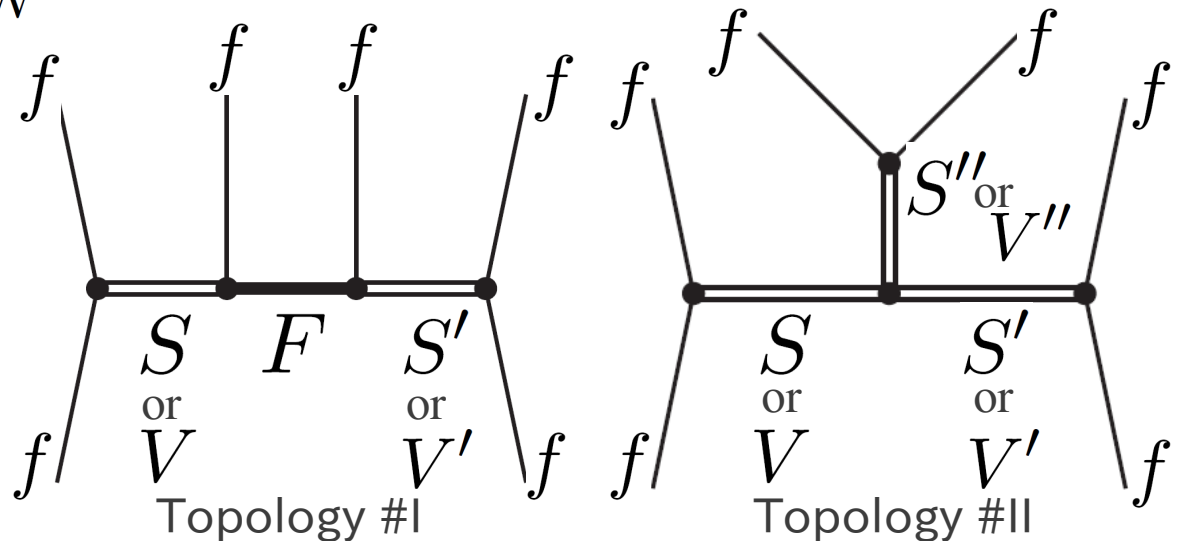
(or constrain)

$$T_{1/2}^{0\nu 2\beta} > 10^{25} \text{ [yr]}$$

$$\mathcal{L}_{d=9} = \frac{1}{\Lambda_{\text{NP}}^5} \mathcal{O}_{d=9}^{\text{tree}} @ \Lambda_{\text{EW}}$$

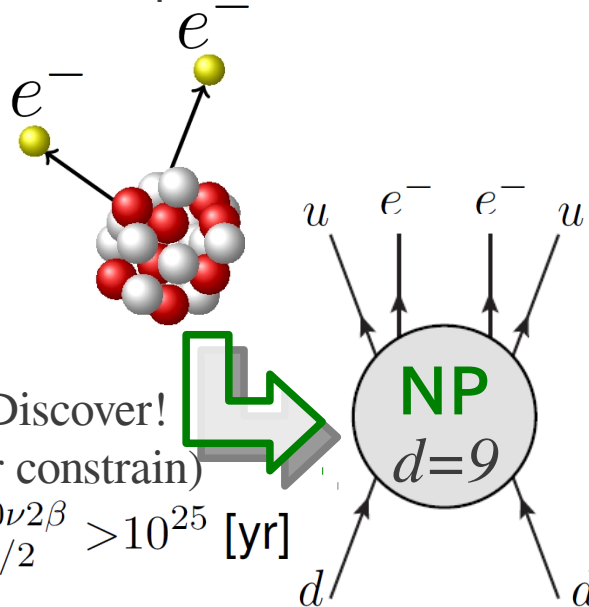
$$\Lambda_{\text{NP}} > \mathcal{O}(1) \text{ [TeV]}$$

**Decompose**  
**Eff.  $d=9$  ops**  
**to tree diagrams**



## Exhaustive bottom-up approach

On2b experiments



Discover!

(or constrain)

$$T_{1/2}^{0\nu 2\beta} > 10^{25} \text{ [yr]}$$

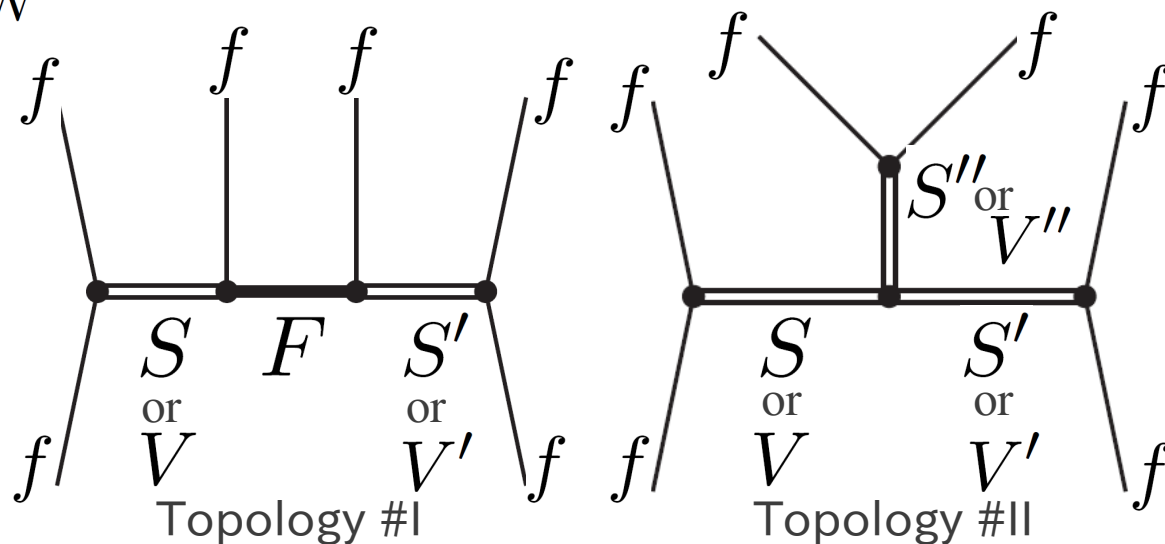
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$$\Lambda_{\text{NP}} > \mathcal{O}(1) \text{ [TeV]}$$

Decompose  
Eff.  $d=9$  ops  
to tree diagrams

How to decompose		Necessary Mediators				
	BL op.	$S$	$F$	$S'$	Basis operators	
2-i-a	$(\overline{u_L} d_R)(d_R)(\overline{e_L})(\overline{u_L} e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u_L} d_R)(d_R)(\overline{e_L})(\overline{u_R} e_R)$	#19	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_R (J_R)^\rho (j)_\rho$
	$(\overline{u_R} d_L)(d_R)(\overline{e_L})(\overline{u_L} e_L)$	#14	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_L J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u_R} d_L)(d_R)(\overline{e_L})(\overline{u_R} e_R)$	#20	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_L (J_R)^\rho (j)_\rho$
2-i-b	$(\overline{u_L} d_R)(\overline{e_L})(d_R)(\overline{u_L} e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{1})_0$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
	$\vdots$		$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{3})_0$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	

List of high  $E$  completions @  $\Lambda_{\text{NP}}$

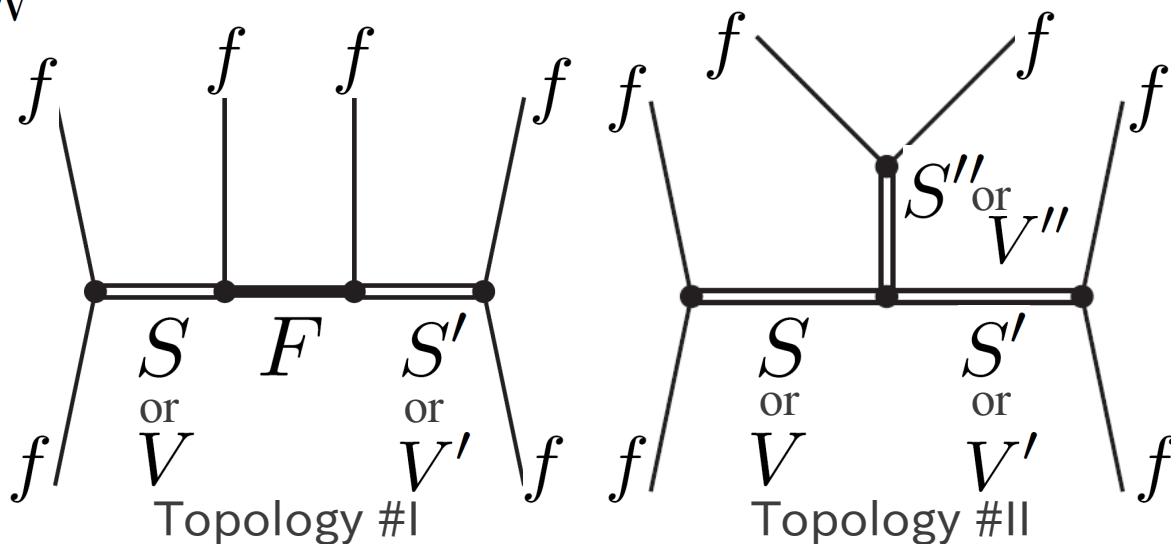


● Exhaustive bottom-up approach

How to decompose		Necessary Mediators				
	BL op.	$S$	$F$	$S'$	Basis operators	
2-i-a	$(\overline{u_L}d_R)(d_R)(\overline{e_L})(\overline{u_L}e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2}J_RJ_Rj_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u_L}d_R)(d_R)(\overline{e_L})(\overline{u_R}e_R)$	#19	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2}J_R(J_R)^\rho(j)_\rho$
	$(\overline{u_R}d_L)(d_R)(\overline{e_L})(\overline{u_L}e_L)$	#14	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2}J_LJ_Rj_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u_R}d_L)(d_R)(\overline{e_L})(\overline{u_R}e_R)$	#20	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2}J_L(J_R)^\rho(j)_\rho$
2-i-b	$(\overline{u_L}d_R)(\overline{e_L})(d_R)(\overline{u_L}e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{1})_0$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2}J_RJ_Rj_R$
	$\vdots$		$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{3})_0$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	

List of high  $E$  completions @  $\Lambda_{NP}$

@  $\Lambda_{EW}$



● Exhaustive bottom-up approach

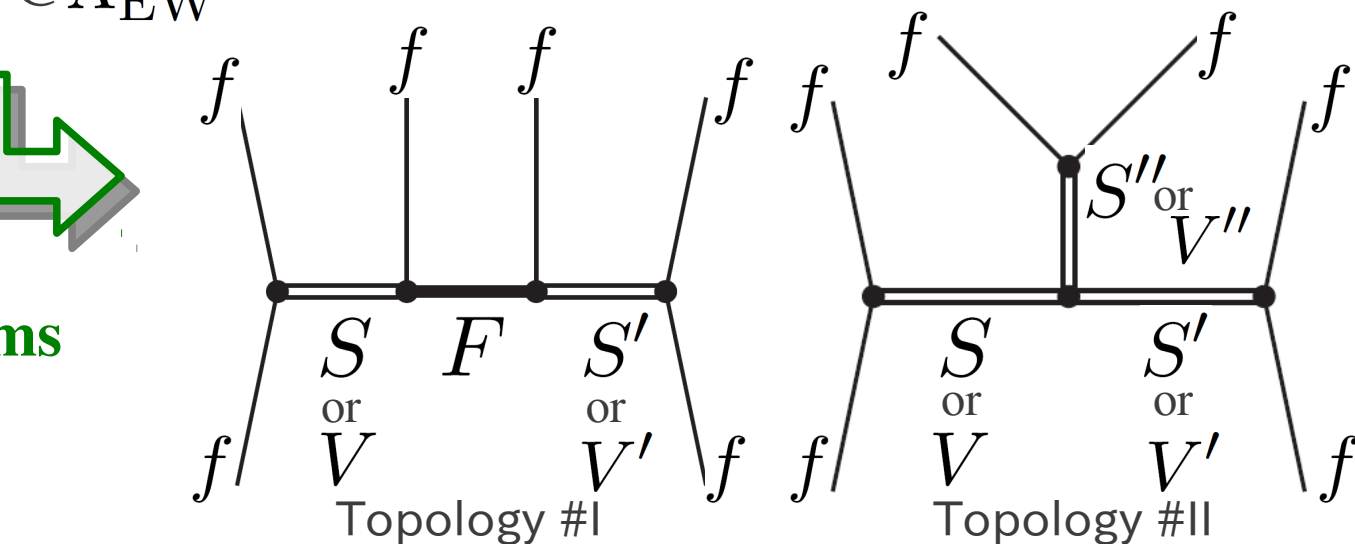
Re-integrate out the Mediators

Effective theories @  $\Lambda_{EW}$

How to decompose		Necessary Mediators				
	BL op.	$S$	$F$	$S'$	Basis operators	
2-i-a	$(\overline{u}_L d_R)(d_R)(\overline{e}_L)(\overline{u}_L e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u}_L d_R)(d_R)(\overline{e}_L)(\overline{u}_R e_R)$	#19	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_R (J_R)^\rho (j)_\rho$
	$(\overline{u}_R d_L)(d_R)(\overline{e}_L)(\overline{u}_L e_L)$	#14	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_L J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u}_R d_L)(d_R)(\overline{e}_L)(\overline{u}_R e_R)$	#20	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_L (J_R)^\rho (j)_\rho$
2-i-b	$(\overline{u}_L d_R)(\overline{e}_L)(d_R)(\overline{u}_L e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{1})_0$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
	$\vdots$		$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{3})_0$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	

List of high  $E$  completions @  $\Lambda_{NP}$

@  $\Lambda_{EW}$



● Exhaustive bottom-up approach

Re-integrate out the Mediators

How to decompose		Necessary Mediators				
	BL op.	$S$	$F$	$S'$	Basis operators	
2-i-a	$(\overline{u}_L d_R)(d_R)(\overline{e}_L)(\overline{u}_L e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u}_L d_R)(d_R)(\overline{e}_L)(\overline{u}_R e_R)$	#19	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_R (J_R)^\rho (j)_\rho$
	$(\overline{u}_R d_L)(d_R)(\overline{e}_L)(\overline{u}_L e_L)$	#14	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_L J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u}_R d_L)(d_R)(\overline{e}_L)(\overline{u}_R e_R)$	#20	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_L (J_R)^\rho (j)_\rho$
2-i-b	$(\overline{u}_L d_R)(\overline{e}_L)(d_R)(\overline{u}_L e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{1})_0$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
	$\vdots$		$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{3})_0$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	

Effective theories @  $\Lambda_{EW}$

$$\mathcal{L}_{d=9} = \frac{1}{\Lambda_{NP}^5} \mathcal{O}_{d=9}^{\text{tree}}$$

Low  $E$  pheno #1

Low  $E$  pheno #2

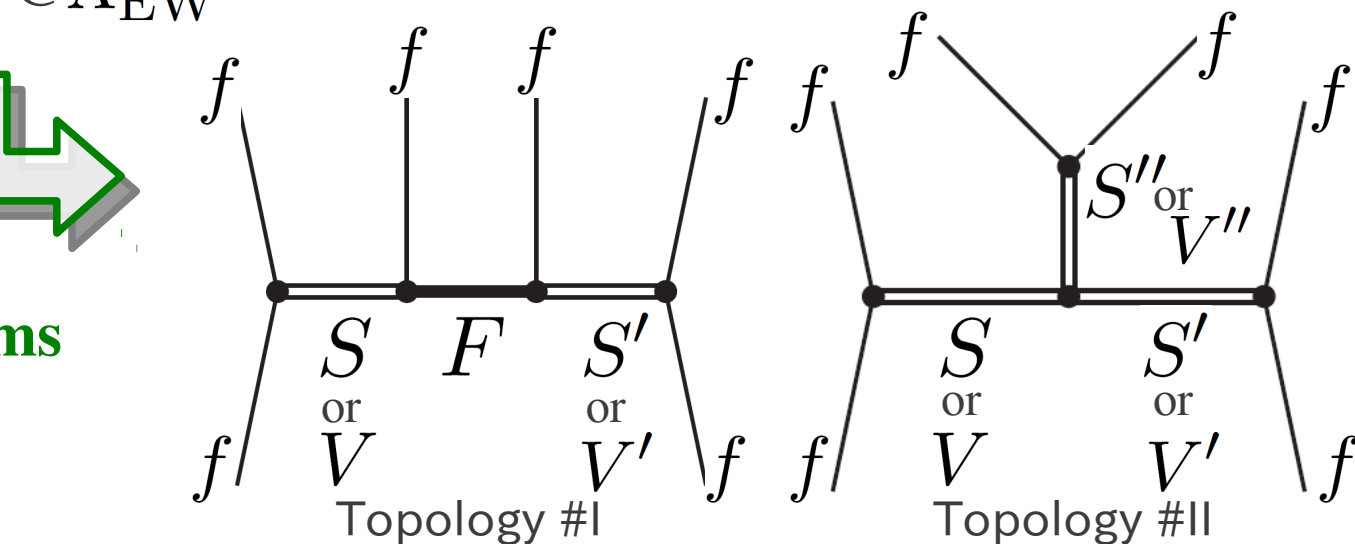
Low  $E$  pheno #3

Low  $E$  pheno #4

$\vdots$

List of high  $E$  completions @  $\Lambda_{NP}$

@  $\Lambda_{EW}$



● Exhaustive bottom-up approach

Re-integrate out the Mediators

How to decompose		Necessary Mediators				
	BL op.	$S$	$F$	$S'$	Basis operators	
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			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u}_L d_R)(d_R)(\overline{e}_L)(\overline{u}_R e_R)$	#19	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_R (J_R)^\rho (j)_\rho$
	$(\overline{u}_R d_L)(d_R)(\overline{e}_L)(\overline{u}_L e_L)$	#14	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_L J_R j_R$
			$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	
	$(\overline{u}_R d_L)(d_R)(\overline{e}_L)(\overline{u}_R e_R)$	#20	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\overline{\mathbf{3}}, \mathbf{2})_{+5/6}$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$\frac{1}{2} J_L (J_R)^\rho (j)_\rho$
2-i-b	$(\overline{u}_L d_R)(\overline{e}_L)(d_R)(\overline{u}_L e_L)$	#11	$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{1})_0$	$(\overline{\mathbf{3}}, \mathbf{1})_{+1/3}$	$-\frac{1}{2} J_R J_R j_R$
	$\vdots$		$(\mathbf{1}, \mathbf{2})_{+1/2}$	$(\mathbf{1}, \mathbf{3})_0$	$(\overline{\mathbf{3}}, \mathbf{3})_{+1/3}$	

Effective theories @  $\Lambda_{EW}$

$$\mathcal{L}_{d=9} = \frac{1}{\Lambda_{NP}^5} \mathcal{O}_{d=9}^{\text{tree}}$$

Low  $E$  pheno #1

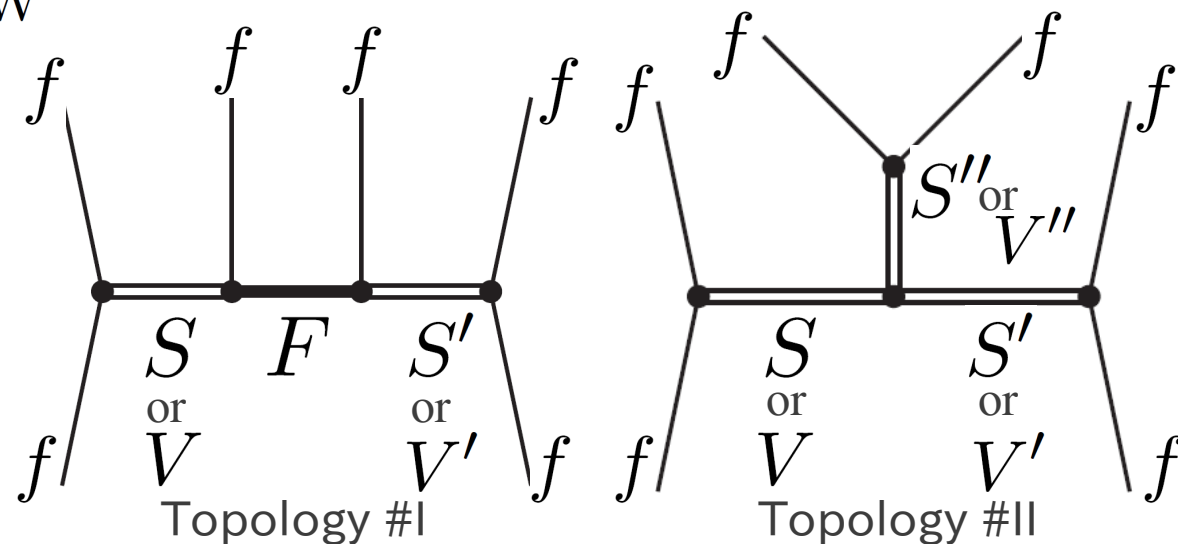
Low  $E$  pheno #2

Low  $E$  pheno #3

Low  $E$  pheno #4

List of high  $E$  completions @  $\Lambda_{NP}$

@  $\Lambda_{EW}$

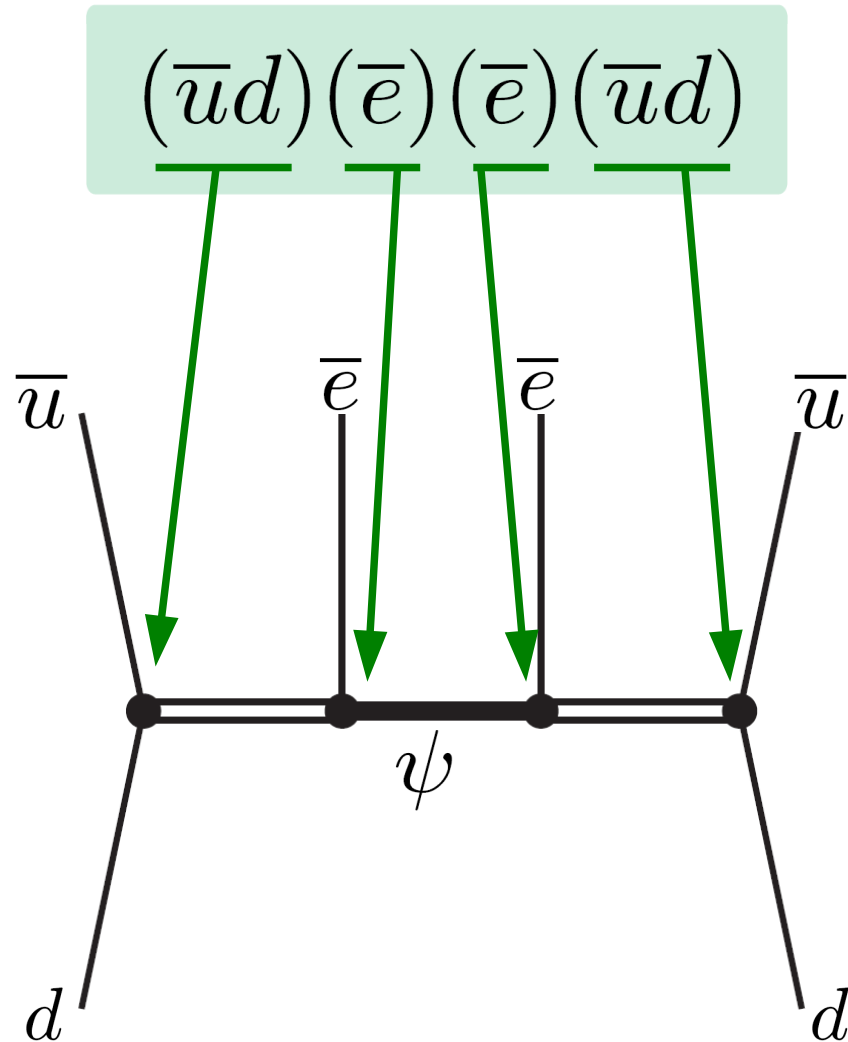


Testing phenos,  
we can identify  
the models @  $\Lambda_{NP}$

We can explore  
high  $E$  models relating to  
 $\mathcal{O}_{d=9}$ , systematically.



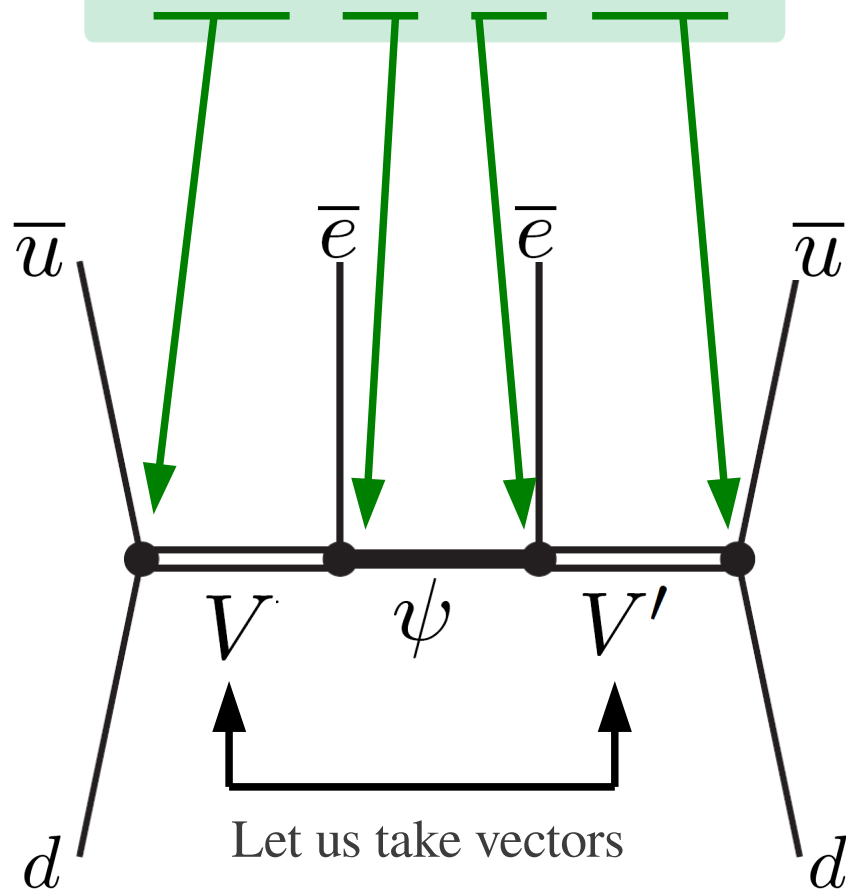
- An example,  
Taking Topology #1  
let us decompose  $d=9$  op as





- An example,  
Taking Topology #1  
let us decompose  $d=9$  op as

$$(\overline{u}d)(\overline{e})(\overline{e})(\overline{u}d)$$



- An example,  
Taking Topology #1  
let us decompose  $d=9$  op as

$$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$$

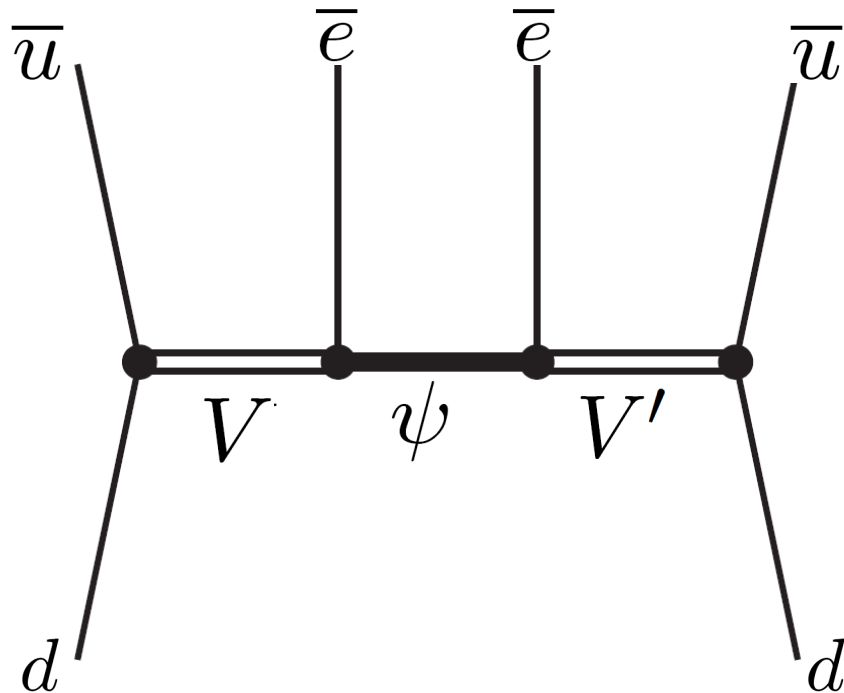
Necessary mediators

$$V(+1, \mathbf{1})$$

$$V'(-1, \mathbf{1})$$

$$\psi(0, \mathbf{1})$$

where  $(U(1)_{\text{em}}, SU(3)_c)$



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Taking Topology #1  
let us decompose  $d=9$  op as

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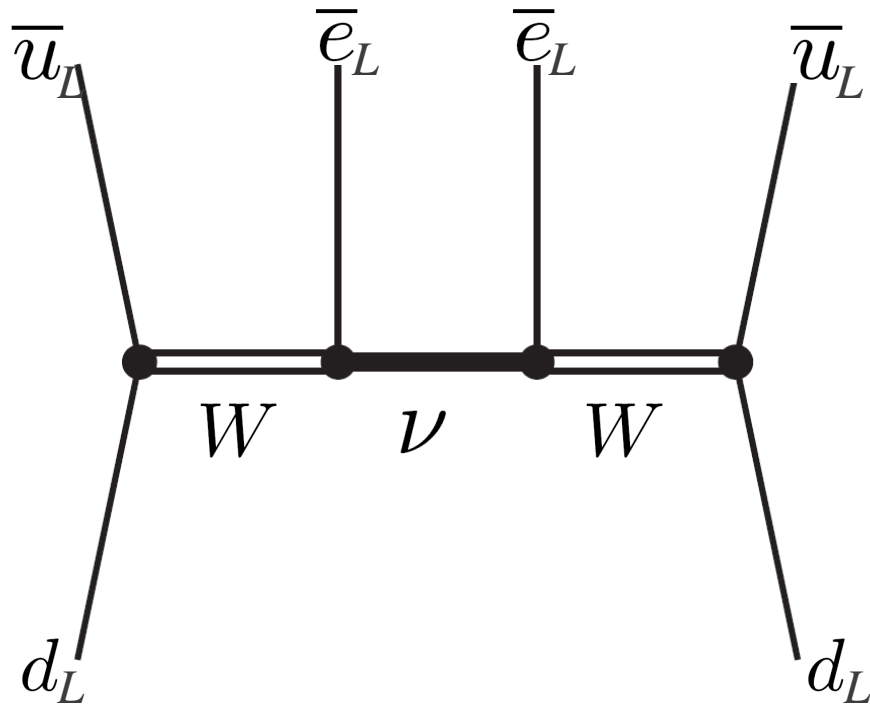
Necessary mediators

$V(+1, \mathbf{1})$	$W^+$
$V'(-1, \mathbf{1})$	$W^-$
$\psi(0, \mathbf{1})$	$\nu$

where  $(U(1)_{\text{em}}, SU(3)_c)$

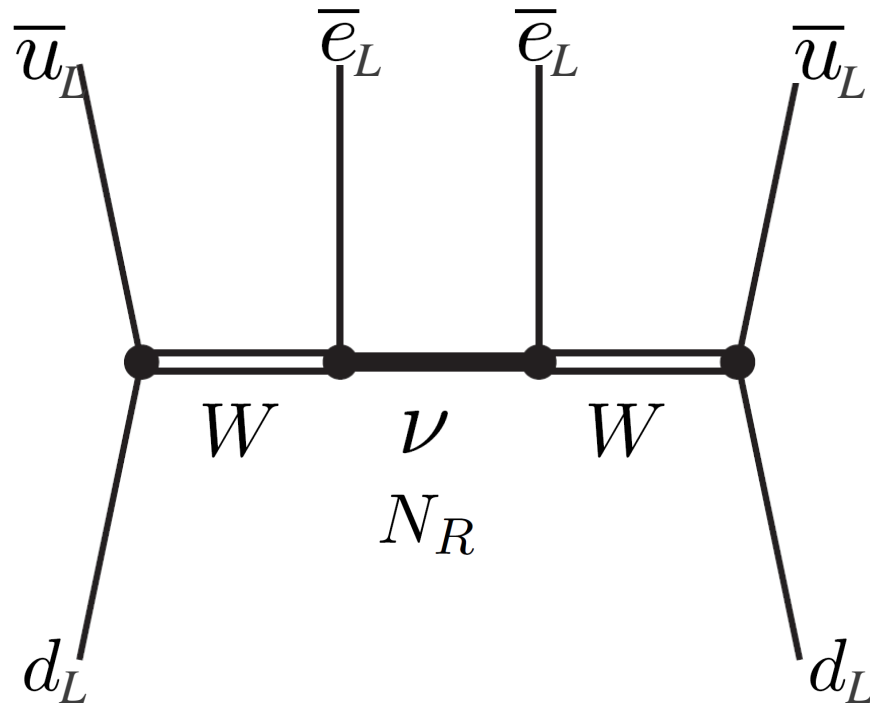
***Rediscovery of the standard neutrino  
mass contribution***

All the outer fermions must be left-handed



- An example,  
Taking Topology #1  
let us decompose  $d=9$  op as

$$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$$



Necessary mediators

$$\begin{array}{ll} V(+1, \mathbf{1}) & W^+ \\ V'(-1, \mathbf{1}) & W^- \\ \psi(0, \mathbf{1}) & \nu \quad N_R \end{array}$$

where  $(U(1)_{\text{em}}, SU(3)_c)$

***Rediscovery of the standard neutrino mass contribution***

All the outer fermions must be left-handed

In Seesaw model,  
right-handed neutrinos (sterile neutrinos)  
can also mediate this diagram.

- Another example,

Decomposition

$$(\bar{u}d)(\bar{e})(d)(\bar{u}e)$$

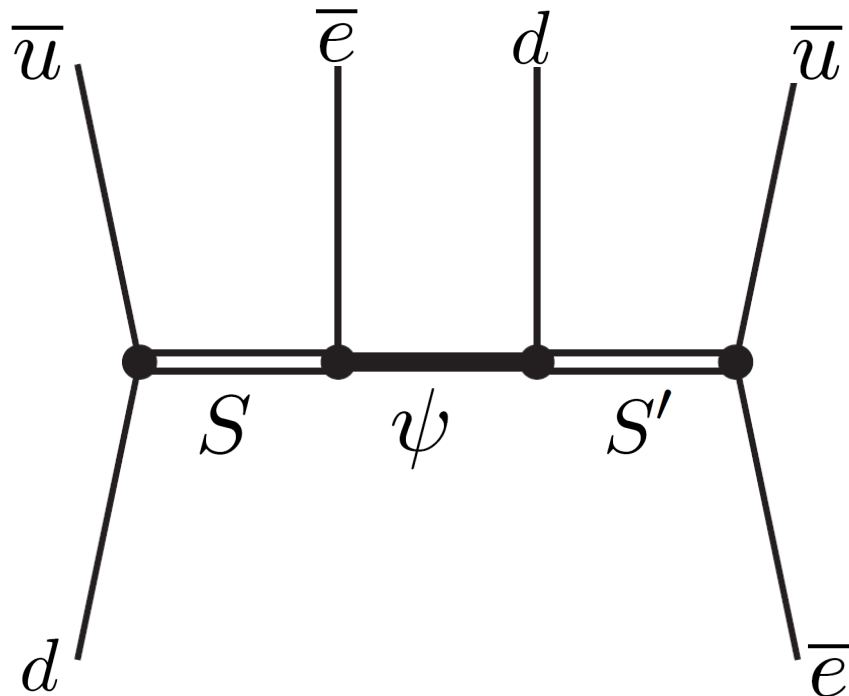
Necessary mediators

$$S(1, 1)$$

$$S'(+1/3, \bar{\mathbf{3}})$$

$$\psi(0, 1)$$

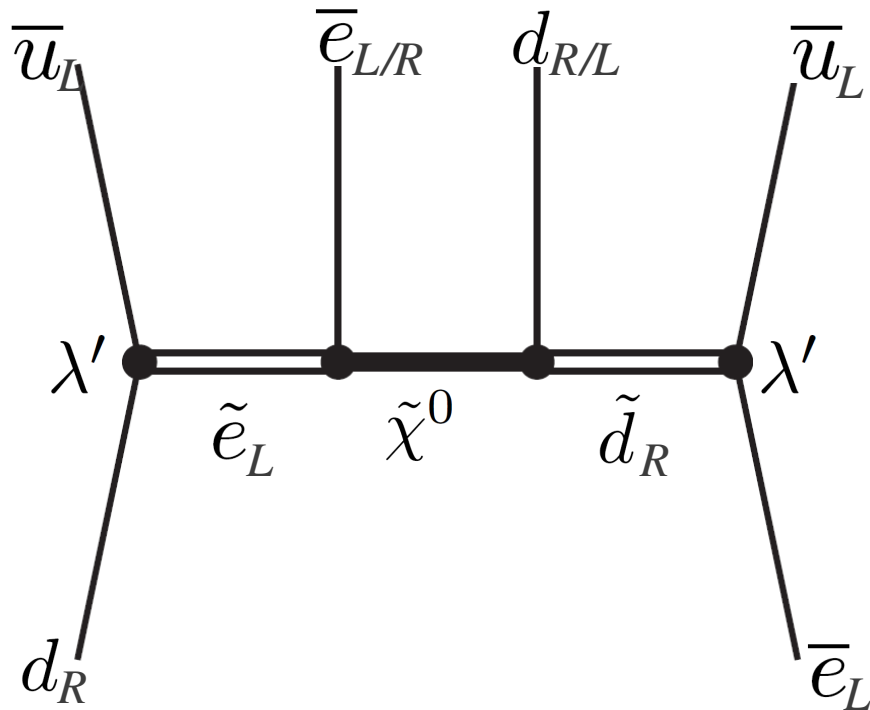
where  $(U(1)_{\text{em}}, SU(3)_c)$



- Another example,

Decomposition

$$(\bar{u}d)(\bar{e})(d)(\bar{u}e)$$



Necessary mediators

$$\begin{array}{ll} S(1, \mathbf{1}) & \tilde{e}^* \\ S'(+1/3, \bar{\mathbf{3}}) & \tilde{d}^* \\ \psi(0, \mathbf{1}) & \tilde{\chi}^0 \end{array}$$

where  $(U(1)_{\text{em}}, SU(3)_c)$

*R-parity violating SUSY models*

$$\mathcal{W}_R \ni \lambda' \hat{L} \hat{Q} \hat{D}^c$$

Hirsch Klapdor-Kleingrothaus Kovalenko,  
PLB378 (1996) 17, PRD54 (1996) 4207

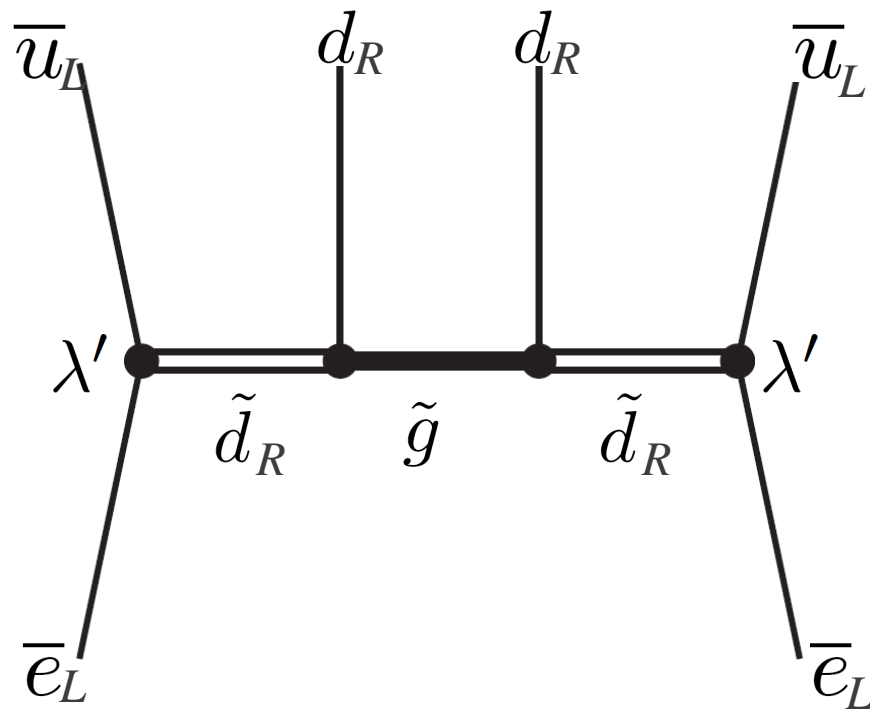
SUSY (Rp-conserved) search at LHC

1<sup>st</sup> generation squarks and gluino  
should be heavier than 1TeV

- Another example,

Decomposition

$$(\overline{u}e)(d)(d)(\overline{u}e)$$



Necessary mediators

$$\begin{array}{ll} S(-1/3, \mathbf{3}) & \tilde{d} \\ S'(+1/3, \overline{\mathbf{3}}) & \tilde{d}^* \\ \psi(0, \mathbf{8}) & \tilde{g} \end{array}$$

where  $(U(1)_{\text{em}}, SU(3)_c)$

*R-parity violating SUSY models*

$$\mathcal{W}_R \ni \lambda' \hat{L} \hat{Q} \hat{D}^c$$

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SUSY (Rp-conserved) search at LHC

1<sup>st</sup> generation squarks and gluino  
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Another diagram in

#	Decomposition	Long Range?	Mediator ( $U(1)_{\text{em}}, SU(3)_c$ )	$S$ or $V$	$\psi$	$S'$ or $V'$	Models/Refs./Comments
1-i	$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$	(a)	$(+1, 1)$	$(0, 1)$	$(-1, 1)$		Mass mechan., RPV [58–60], LR-symmetric models [39], Mass mechanism with $\nu_S$ [61] TeV scale seesaw, e.g., [62, 63] [64]
1-ii-a	$(\bar{u}d)(\bar{u})(d)(\bar{e}\bar{e})$		$(+1, 1)$	$(+5/3, 3)$	$(+2, 1)$		
1-ii-b	$(\bar{u}d)(d)(\bar{u})(\bar{e}\bar{e})$		$(+1, 1)$	$(+4/3, \bar{3})$	$(+2, 1)$		
2-i-a	$(\bar{u}d)(d)(\bar{e})(\bar{u}\bar{e})$		$(+1, 1)$	$(+4/3, \bar{3})$	$(+1/3, \bar{3})$		
2-i-b	$(\bar{u}d)(\bar{e})(d)(\bar{u}\bar{e})$	(b)	$(+1, 1)$	$(0, 1)$	$(+1/3, \bar{3})$		RPV [58–60], LQ [65, 66]
2-ii-a	$(\bar{u}d)(\bar{u})(\bar{e})(d\bar{e})$		$(+1, 1)$	$(+5/3, 3)$	$(+2/3, 3)$		
2-ii-b	$(\bar{u}d)(\bar{e})(\bar{u})(d\bar{e})$	(b)	$(+1, 1)$	$(0, 1)$	$(+2/3, 3)$		RPV [58–60], LQ [65, 66]
2-iii-a	$(d\bar{e})(\bar{u})(d)(\bar{u}\bar{e})$	(c)	$(-2/3, \bar{3})$	$(0, 1)$	$(+1/3, \bar{3})$		RPV [58–60]
2-iii-b	$(d\bar{e})(d)(\bar{u})(\bar{u}\bar{e})$		$(-2/3, \bar{3})$	$(-1/3, 3)$	$(+1/3, \bar{3})$		RPV [58–60]
3-i	$(\bar{u}\bar{u})(\bar{e})(\bar{e})(d\bar{d})$		$(+4/3, \bar{3})$	$(+1/3, \bar{3})$	$(-2/3, 3)$		only with $V_\rho$ and $V'_\rho$
3-ii	$(\bar{u}\bar{u})(d)(d)(\bar{e}\bar{e})$		$(+4/3, \bar{3})$	$(+5/3, 3)$	$(+2, 1)$		only with $V_\rho$
3-iii	$(d\bar{d})(\bar{u})(\bar{u})(\bar{e}\bar{e})$		$(+2/3, 3)$	$(+4/3, \bar{3})$	$(+2, 1)$		only with $V_\rho$
4-i	$(d\bar{e})(\bar{u})(\bar{u})(d\bar{e})$	(c)	$(-2/3, \bar{3})$	$(0, 1)$	$(+2/3, 3)$		RPV [58–60]
4-ii-a	$(\bar{u}\bar{u})(d)(\bar{e})(d\bar{e})$		$(+4/3, \bar{3})$	$(+5/3, 3)$	$(+2/3, 3)$		only with $V_\rho$
4-ii-b	$(\bar{u}\bar{u})(\bar{e})(d)(d\bar{e})$		$(+4/3, \bar{3})$	$(+1/3, \bar{3})$	$(+2/3, 3)$		only with $V_\rho$
5-i	$(\bar{u}\bar{e})(d)(d)(\bar{u}\bar{e})$	(c)	$(-1/3, 3)$	$(0, 1)$	$(+1/3, \bar{3})$		RPV [58–60]
5-ii-a	$(\bar{u}\bar{e})(\bar{u})(\bar{e})(d\bar{d})$		$(-1/3, 3)$	$(+1/3, \bar{3})$	$(-2/3, 3)$		only with $V'_\rho$
5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(d\bar{d})$		$(-1/3, 3)$	$(-4/3, 3)$	$(-2/3, \bar{3})$		only with $V'_\rho$

SnuM  
Seesaw

*Possible decompositions  
and  
Necessary mediators*

(only Topology #I)

- 4 possibilities for each decom.  
 $S$ - $F$ - $S$ ,  $V$ - $F$ - $V$ ,  $S$ - $F$ - $V$ ,  
and  $V$ - $F$ - $S$

- Mediators are specified with  
 $U(1)$  EM charge  
 $SU(3)$  colour charge

- Here, we do not specify the  
chiralities of outer fermions  
( $SU(2)_L$  and  $U(1)_Y$ )

→ Decom of chirality-specified ops  
Bonnet Hirsch O Winter  
JHEP1303 (2013) 055

RPV

- Long Range?

Decomposition which can  
contain neutrino propagation



### Possible decompositions and Necessary mediators

(only Topology #I)

- 4 possibilities for each decomp.

$S$ - $F$ - $S$ ,  $V$ - $F$ - $V$ ,  $S$ - $F$ - $V$ ,  
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- Long Range?

Decomposition which can  
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#	Decomposition	Long Range?	Mediator ( $U(1)_{em}, SU(3)_c$ ) $S$ or $V_\rho$ $\psi$ $S'$ or $V'_\rho$	Models/Refs./Comments
1-i	$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$	(a)	$(+1, 1)$ $(0, 1)$ $(-1, 1)$	Mass mechan., RPV [58–60], LR-symmetric models [39], Mass mechanism with $\nu_S$ [61], TeV scale seesaw, e.g., [62, 63] [64]
1-ii-a	$(\bar{u}d)(\bar{u})(d)(\bar{e}\bar{e})$		$(+1, 8)$ $(0, 8)$ $(-1, 8)$ $(+1, 1)$ $(+5/3, 3)$ $(+2, 1)$ $(+1, 8)$ $(+5/3, 3)$ $(+2, 1)$	
1-ii-b	$(\bar{u}d)(d)(\bar{u})(\bar{e}\bar{e})$		$(+1, 1)$ $(+4/3, \bar{3})$ $(+2, 1)$ $(+1, 8)$ $(+4/3, \bar{3})$ $(+2, 1)$	
2-i-a	$(\bar{u}d)(d)(\bar{e})(\bar{u}\bar{e})$		$(+1, 1)$ $(+4/3, \bar{3})$ $(+1/3, \bar{3})$ $(+1, 8)$ $(+4/3, \bar{3})$ $(+1/3, \bar{3})$	
2-i-b	$(\bar{u}d)(\bar{e})(d)(\bar{u}\bar{e})$	(b)	$(+1, 1)$ $(0, 1)$ $(+1/3, \bar{3})$ $(+1, 8)$ $(0, 8)$ $(+1/3, \bar{3})$	RPV [58–60], LQ [65, 66]
2-ii-a	$(\bar{u}d)(\bar{u})(\bar{e})(d\bar{e})$		$(+1, 1)$ $(+5/3, 3)$ $(+2/3, 3)$ $(+1, 8)$ $(+5/3, 3)$ $(+2/3, 3)$	
2-ii-b	$(\bar{u}d)(\bar{e})(\bar{u})(d\bar{e})$	(b)	$(+1, 1)$ $(0, 1)$ $(+2/3, 3)$ $(+1, 8)$ $(0, 8)$ $(+2/3, 3)$	RPV [58–60], LQ [65, 66]
2-iii-a	$(d\bar{e})(\bar{u})(d)(\bar{u}\bar{e})$	(c)	$(-2/3, \bar{3})$ $(0, 1)$ $(+1/3, \bar{3})$ $(-2/3, \bar{3})$ $(0, 8)$ $(+1/3, \bar{3})$	RPV [58–60] RPV [58–60]
2-iii-b	$(d\bar{e})(d)(\bar{u})(\bar{u}\bar{e})$		$(-2/3, \bar{3})$ $(-1/3, 3)$ $(+1/3, \bar{3})$ $(-2/3, \bar{3})$ $(-1/3, \bar{6})$ $(+1/3, \bar{3})$	
3-i	$(\bar{u}\bar{u})(\bar{e})(\bar{e})(d\bar{d})$		$(+4/3, 3)$ $(+1/3, \bar{3})$ $(-2/3, 3)$ $(+4/3, 6)$ $(+1/3, 6)$ $(-2/3, 6)$	only with $V_\rho$ and $V'_\rho$
3-ii	$(\bar{u}\bar{u})(d)(d)(\bar{e}\bar{e})$		$(+4/3, \bar{3})$ $(+5/3, 3)$ $(+2, 1)$ $(+4/3, 6)$ $(+5/3, 3)$ $(+2, 1)$	only with $V_\rho$
3-iii	$(d\bar{d})(\bar{u})(\bar{u})(\bar{e}\bar{e})$		$(+2/3, 3)$ $(+4/3, \bar{3})$ $(+2, 1)$ $(+2/3, \bar{6})$ $(+4/3, \bar{3})$ $(+2, 1)$	only with $V_\rho$
4-i	$(d\bar{e})(\bar{u})(\bar{u})(d\bar{e})$	(c)	$(-2/3, \bar{3})$ $(0, 1)$ $(+2/3, 3)$ $(-2/3, \bar{3})$ $(0, 8)$ $(+2/3, 3)$	RPV [58–60] RPV [58–60]
4-ii-a	$(\bar{u}\bar{u})(d)(\bar{e})(d\bar{e})$		$(+4/3, \bar{3})$ $(+5/3, 3)$ $(+2/3, 3)$ $(+4/3, 6)$ $(+5/3, 3)$ $(+2/3, 3)$	only with $V_\rho$ see Sec. 4 (this work)
4-ii-b	$(\bar{u}\bar{u})(\bar{e})(d)(d\bar{e})$		$(+4/3, \bar{3})$ $(+1/3, \bar{3})$ $(+2/3, 3)$ $(+4/3, 6)$ $(+1/3, 6)$ $(+2/3, 3)$	only with $V_\rho$
5-i	$(\bar{u}\bar{e})(d)(d)(\bar{u}\bar{e})$	(c)	$(-1/3, 3)$ $(0, 1)$ $(+1/3, \bar{3})$ $(-1/3, 3)$ $(0, 8)$ $(+1/3, \bar{3})$	RPV [58–60] RPV [58–60]
5-ii-a	$(\bar{u}\bar{e})(\bar{u})(\bar{e})(d\bar{d})$		$(-1/3, 3)$ $(+1/3, \bar{3})$ $(-2/3, \bar{3})$ $(-1/3, 3)$ $(+1/3, 6)$ $(-2/3, 6)$	only with $V'_\rho$
5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(d\bar{d})$		$(-1/3, 3)$ $(-4/3, 3)$ $(-2/3, \bar{3})$ $(-1/3, 3)$ $(-4/3, 3)$ $(-2/3, 6)$	only with $V'_\rho$

### Possible decompositions and Necessary mediators

(only Topology #I)

- 4 possibilities for each decom.

$S$ - $F$ - $S$ ,  $V$ - $F$ - $V$ ,  $S$ - $F$ - $V$ ,  
and  $V$ - $F$ - $S$

- Mediators are specified with  
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- Long Range?

Decomposition which can  
contain neutrino propagation

#	Decomposition	Long Range?	Mediator ( $U(1)_{em}, SU(3)_c$ )			Models/Refs./Comments
			$S$ or $V_\rho$	$\psi$	$S'$ or $V'_\rho$	
1-i	$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$	(a)	(+1, 1)	(0, 1)	(-1, 1)	Mass mechan., RPV [58–60], LR-symmetric models [39], Mass mechanism with $\nu_S$ [61], TeV scale seesaw, e.g., [62, 63] [64]
1-ii-a	$(\bar{u}d)(\bar{u})(d)(\bar{e}\bar{e})$		(+1, 8) (+1, 1) (+1, 8)	(0, 8) (+5/3, 3) (+5/3, 3)	(-1, 8) (+2, 1) (+2, 1)	
1-ii-b	$(\bar{u}d)(d)(\bar{u})(\bar{e}\bar{e})$		(+1, 1) (+1, 8)	(+4/3, 3) (+4/3, 3)	(+2, 1) (+2, 1)	
2-i-a	$(\bar{u}d)(d)(\bar{e})(\bar{u}\bar{e})$		(+1, 1) (+1, 8)	(+4/3, 3) (+4/3, 3)	(+1/3, 3) (+1/3, 3)	
2-i-b	$(\bar{u}d)(\bar{e})(d)(\bar{u}\bar{e})$	(b)	(+1, 1) (+1, 8)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60], LQ [65, 66]
2-ii-a	$(\bar{u}d)(\bar{u})(\bar{e})(d\bar{e})$		(+1, 1) (+1, 8)	(+5/3, 3) (+5/3, 3)	(+2/3, 3) (+2/3, 3)	
2-ii-b	$(\bar{u}d)(\bar{e})(\bar{u})(d\bar{e})$	(b)	(+1, 1) (+1, 8)	(0, 1) (0, 8)	(+2/3, 3) (+2/3, 3)	RPV [58–60], LQ [65, 66]
2-iii-a	$(d\bar{e})(\bar{u})(d)(\bar{u}\bar{e})$	(c)	(-2/3, 3) (-2/3, 3)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60] RPV [58–60]
2-iii-b	$(d\bar{e})(d)(\bar{u})(\bar{u}\bar{e})$		(-2/3, 3) (-2/3, 3)	(-1/3, 3) (-1/3, 6)	(+1/3, 3) (+1/3, 3)	
3-i	$(\bar{u}\bar{u})(\bar{e})(\bar{e})(d\bar{d})$		(+4/3, 3) (+4/3, 6)	(+1/3, 3) (+1/3, 6)	(-2/3, 3) (-2/3, 6)	only with $V_\rho$ and $V'_\rho$
3-ii	$(\bar{u}\bar{u})(d)(d)(\bar{e}\bar{e})$		(+4/3, 3) (+4/3, 6)	(+5/3, 3) (+5/3, 3)	(+2, 1) (+2, 1)	only with $V_\rho$
3-iii	$(d\bar{d})(\bar{u})(\bar{u})(\bar{e}\bar{e})$		(+2/3, 3) (+2/3, 6)	(+4/3, 3) (+4/3, 3)	(+2, 1) (+2, 1)	only with $V_\rho$
4-i	$(d\bar{e})(\bar{u})(\bar{u})(d\bar{e})$	(c)	(-2/3, 3) (-2/3, 3)	(0, 1) (0, 8)	(+2/3, 3) (+2/3, 3)	RPV [58–60] RPV [58–60]
4-ii-a	$(\bar{u}\bar{u})(d)(\bar{e})(d\bar{e})$		(+4/3, 3) (+4/3, 6)	(+5/3, 3) (+5/3, 3)	(+2/3, 3) (+2/3, 3)	only with $V_\rho$ see Sec. 4 (this work)
4-ii-b	$(\bar{u}\bar{u})(\bar{e})(d)(d\bar{e})$		(+4/3, 3) (+4/3, 6)	(+1/3, 3) (+1/3, 6)	(+2/3, 3) (+2/3, 3)	only with $V_\rho$
5-i	$(\bar{u}\bar{e})(d)(d)(\bar{u}\bar{e})$	(c)	(-1/3, 3) (-1/3, 3)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60] RPV [58–60]
5-ii-a	$(\bar{u}\bar{e})(\bar{u})(\bar{e})(d\bar{d})$		(-1/3, 3) (-1/3, 3)	(+1/3, 3) (+1/3, 6)	(-2/3, 3) (-2/3, 6)	only with $V'_\rho$
5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(d\bar{d})$		(-1/3, 3) (-1/3, 3)	(-4/3, 3) (-4/3, 3)	(-2/3, 3) (-2/3, 6)	only with $V'_\rho$

#	Decomposition	Long Range?	Mediator ( $U(1)_{em}, SU(3)_c$ )			Models/Refs./Comments
			$S$ or $V_\rho$	$\eta$	$S'$ or $V'_\rho$	
1-i	$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$	(a)	(+1, 1)	(0, 1)	(-1, 1)	Mass mechan., RPV [58–60], LR-symmetric models [39], Mass mechanism with $\nu_S$ [61], TeV scale seesaw, e.g., [62, 63] [64]
1-ii-a	$(\bar{u}d)(\bar{u})(d)(\bar{e}\bar{e})$		(+1, 8)	(0, 8)	(-1, 8)	
			(+1, 1)	(+5/3, 3)	(+2, 1)	
			(+1, 8)	(+5/3, 3)	(+2, 1)	
1-ii-b	$(\bar{u}d)(d)(\bar{u})(\bar{e}\bar{e})$		(+1, 1)	(+4/3, 3)	(+2, 1)	
			(+1, 8)	(+4/3, 3)	(+2, 1)	
2-i-a	$(\bar{u}d)(d)(\bar{e})(\bar{u}\bar{e})$		(+1, 1)	(+4/3, 3)	(+1/3, 3)	
			(+1, 8)	(+4/3, 3)	(+1/3, 3)	
2-i-b	$(\bar{u}d)(\bar{e})(d)(\bar{u}\bar{e})$	(b)	(+1, 1)	(0, 1)	(+1/3, 3)	RPV [58–60], LQ [65, 66]
			(+1, 8)	(0, 8)	(+1/3, 3)	
2-ii-a	$(\bar{u}d)(\bar{u})(\bar{e})(d\bar{e})$		(+1, 1)	(+5/3, 3)	(+2/3, 3)	
			(+1, 8)	(+5/3, 3)	(+2/3, 3)	
2-ii-b	$(\bar{u}d)(\bar{e})(\bar{u})(d\bar{e})$	(b)	(+1, 1)	(0, 1)	(+2/3, 3)	RPV [58–60], LQ [65, 66]
			(+1, 8)	(0, 8)	(+2/3, 3)	
2-iii-a	$(d\bar{e})(\bar{u})(d)(\bar{u}\bar{e})$	(c)	(-2/3, 3)	(0, 1)	(+1/3, 3)	RPV [58–60]
			(-2/3, 3)	(0, 8)	(+1/3, 3)	RPV [58–60]
2-iii-b	$(d\bar{e})(d)(\bar{u})(\bar{u}\bar{e})$		(-2/3, 3)	(-1/3, 3)	(+1/3, 3)	
			(-2/3, 3)	(-1/3, 6)	(+1/3, 3)	
3-i	$(\bar{u}\bar{u})(\bar{e})(\bar{e})(d\bar{d})$		(+4/3, 3)	(+1/3, 3)	(-2/3, 3)	only with $V_\rho$ and $V'_\rho$
			(+4/3, 6)	(+1/3, 6)	(-2/3, 6)	
3-ii	$(\bar{u}\bar{u})(d)(d)(\bar{e}\bar{e})$		(+4/3, 3)	(+5/3, 3)	(+2, 1)	only with $V_\rho$
			(+4/3, 6)	(+5/3, 3)	(+2, 1)	
3-iii	$(d\bar{d})(\bar{u})(\bar{u})(\bar{e}\bar{e})$		(+2/3, 3)	(+4/3, 3)	(+2, 1)	only with $V_\rho$
			(+2/3, 6)	(+4/3, 3)	(+2, 1)	
4-i	$(d\bar{e})(\bar{u})(\bar{u})(d\bar{e})$	(c)	(-2/3, 3)	(0, 1)	(+2/3, 3)	RPV [58–60]
			(-2/3, 3)	(0, 8)	(+2/3, 3)	RPV [58–60]
4-ii-a	$(\bar{u}\bar{u})(d)(\bar{e})(d\bar{e})$		(+4/3, 3)	(+5/3, 3)	(+2/3, 3)	only with $V_\rho$
			(+4/3, 6)	(+5/3, 3)	(+2/3, 3)	see Sec. 4 (this work)
4-ii-b	$(\bar{u}\bar{u})(\bar{e})(d)(d\bar{e})$		(+4/3, 3)	(+1/3, 3)	(+2/3, 3)	only with $V_\rho$
			(+4/3, 6)	(+1/3, 6)	(+2/3, 3)	
5-i	$(\bar{u}\bar{e})(d)(d)(\bar{u}\bar{e})$	(c)	(-1/3, 3)	(0, 1)	(+1/3, 3)	RPV [58–60]
			(-1/3, 3)	(0, 8)	(+1/3, 3)	RPV [58–60]
5-ii-a	$(\bar{u}\bar{e})(\bar{u})(\bar{e})(d\bar{d})$		(-1/3, 3)	(+1/3, 3)	(-2/3, 3)	only with $V'_\rho$
			(-1/3, 3)	(+1/3, 6)	(-2/3, 6)	
5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(d\bar{d})$		(-1/3, 3)	(-4/3, 3)	(-2/3, 3)	only with $V'_\rho$
			(-1/3, 3)	(-4/3, 3)	(-2/3, 6)	

### Possible decompositions and Necessary mediators

(only Topology #I)

- 4 possibilities for each decom.  
 $S$ - $F$ - $S$ ,  $V$ - $F$ - $V$ ,  $S$ - $F$ - $V$ ,  
and  $V$ - $F$ - $S$
- Mediators are specified with  
 $U(1)$  EM charge  
 $SU(3)$  colour charge
- Here, we do not specify the  
chiralities of outer fermions  
( $SU(2)_L$  and  $U(1)_Y$ )

→ Decom of chirality-specified ops  
Bonnet Hirsch O Winter  
IHEP1303 (2013) 055

- Long Range?  
Decomposition which can  
contain neutrino propagation



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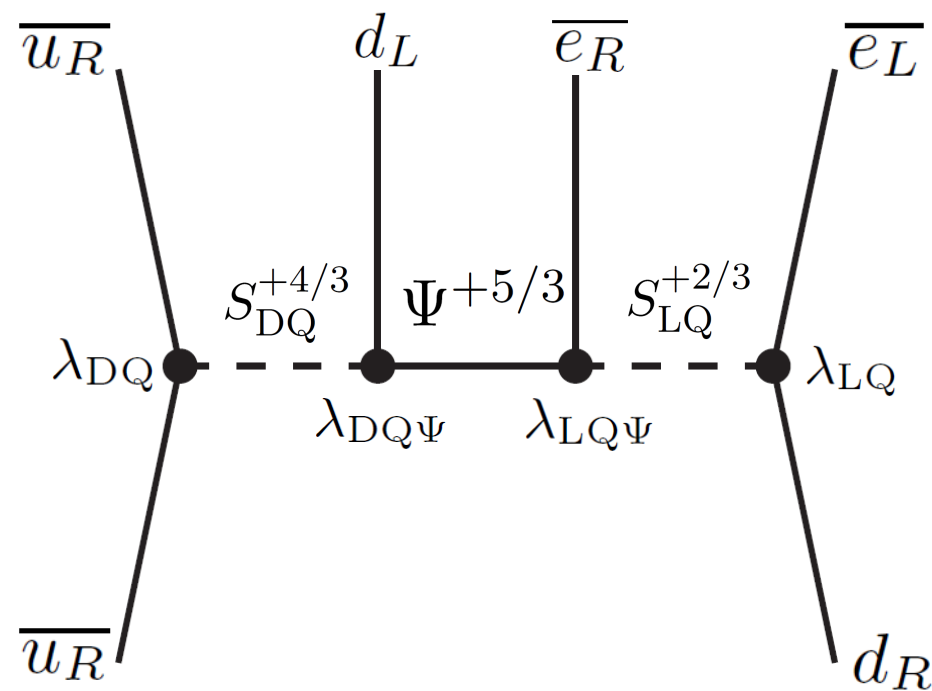
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- Long Range?

Decomposition which can  
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#	Decomposition	Long Range?	Mediator ( $U(1)_{em}, SU(3)_c$ )			Models/Refs./Comments
			$S$ or $V_\rho$	$\psi$	$S'$ or $V'_\rho$	
1-i	$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$	(a)	(+1, 1)	(0, 1)	(-1, 1)	Mass mechan., RPV [58–60], LR-symmetric models [39], Mass mechanism with $\nu_S$ [61], TeV scale seesaw, e.g., [62, 63] [64]
1-ii-a	$(\bar{u}d)(\bar{u})(d)(\bar{e}\bar{e})$		(+1, 8) (+1, 1)	(0, 8) (+5/3, 3)	(-1, 8) (+2, 1)	
1-ii-b	$(\bar{u}d)(d)(\bar{u})(\bar{e}\bar{e})$		(+1, 8) (+1, 1)	(+5/3, 3) (+4/3, 3)	(+2, 1) (+2, 1)	
2-i-a	$(\bar{u}d)(d)(\bar{e})(\bar{u}\bar{e})$		(+1, 8) (+1, 1)	(+4/3, 3) (+4/3, 3)	(+1/3, 3) (+1/3, 3)	
2-i-b	$(\bar{u}d)(\bar{e})(d)(\bar{u}\bar{e})$	(b)	(+1, 8) (+1, 1)	(0, 8) (0, 1)	(+1/3, 3) (+1/3, 3)	RPV [58–60], LQ [65, 66]
2-ii-a	$(\bar{u}d)(\bar{u})(\bar{e})(d\bar{e})$		(+1, 8) (+1, 1)	(+5/3, 3) (+5/3, 3)	(+2/3, 3) (+2/3, 3)	
2-ii-b	$(\bar{u}d)(\bar{e})(\bar{u})(d\bar{e})$	(b)	(+1, 8) (+1, 1)	(0, 8) (0, 1)	(+2/3, 3) (+2/3, 3)	RPV [58–60], LQ [65, 66]
2-iii-a	$(d\bar{e})(\bar{u})(d)(\bar{u}\bar{e})$	(c)	(-2/3, 3) (-2/3, 3)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60] RPV [58–60]
2-iii-b	$(d\bar{e})(d)(\bar{u})(\bar{u}\bar{e})$		(-2/3, 3) (-2/3, 3)	(-1/3, 3) (-1/3, 6)	(+1/3, 3) (+1/3, 3)	
3-i	$(\bar{u}\bar{u})(\bar{e})(\bar{e})(d\bar{d})$		(+4/3, 3) (+4/3, 6)	(+1/3, 3) (+1/3, 6)	(-2/3, 3) (-2/3, 6)	only with $V_\rho$ and $V'_\rho$
3-ii	$(\bar{u}\bar{u})(d)(d)(\bar{e}\bar{e})$		(+4/3, 3) (+4/3, 6)	(+5/3, 3) (+5/3, 3)	(+2, 1) (+2, 1)	only with $V_\rho$
3-iii	$(d\bar{d})(\bar{u})(\bar{u})(\bar{e}\bar{e})$		(+2/3, 3) (+2/3, 6)	(+4/3, 3) (+4/3, 3)	(+2, 1) (+2, 1)	
4-i	$(d\bar{e})(\bar{u})(\bar{u})(d\bar{e})$	(c)	(-2/3, 3) (-2/3, 3)	(0, 1) (0, 8)	(+2/3, 3) (+2/3, 3)	RPV [58–60] RPV [58–60]
4-ii-a	$(\bar{u}\bar{u})(d)(\bar{e})(d\bar{e})$		(+4/3, 3) (+4/3, 6)	(+5/3, 3) (+5/3, 3)	(+2/3, 3) (+2/3, 3)	only with $V_\rho$ see Sec. 4 (this work)
4-ii-b	$(\bar{u}\bar{u})(\bar{e})(d)(d\bar{e})$		(+4/3, 3) (+4/3, 6)	(+1/3, 3) (+1/3, 6)	(+2/3, 3) (+2/3, 3)	only with $V_\rho$
5-i	$(\bar{u}\bar{e})(d)(d)(\bar{u}\bar{e})$	(c)	(-1/3, 3) (-1/3, 3)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60] RPV [58–60]
5-ii-a	$(\bar{u}\bar{e})(\bar{u})(\bar{e})(d\bar{d})$		(-1/3, 3) (-1/3, 3)	(+1/3, 3) (+1/3, 6)	(-2/3, 3) (-2/3, 6)	only with $V'_\rho$
5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(d\bar{d})$		(-1/3, 3) (-1/3, 3)	(-4/3, 3) (-4/3, 3)	(-2/3, 3) (-2/3, 6)	only with $V'_\rho$

Let us have a closer look  
at this example.



$$(\overline{u}_R u_R)(Q)(\overline{e}_R)(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

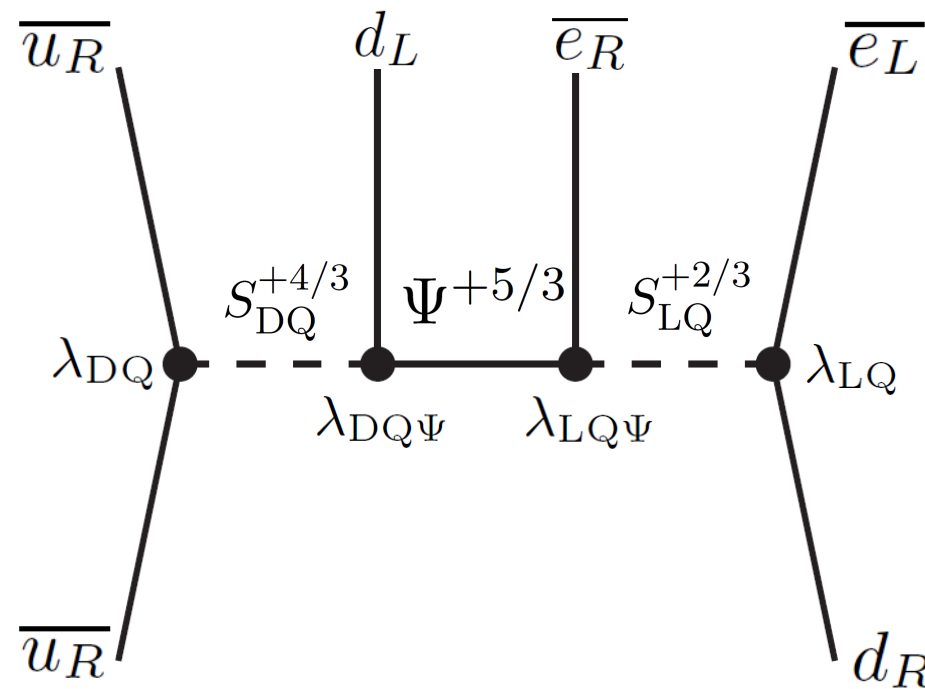
Necessary mediators

$$(S_{DQ}^{+4/3})_X$$

$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia}, \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$



$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

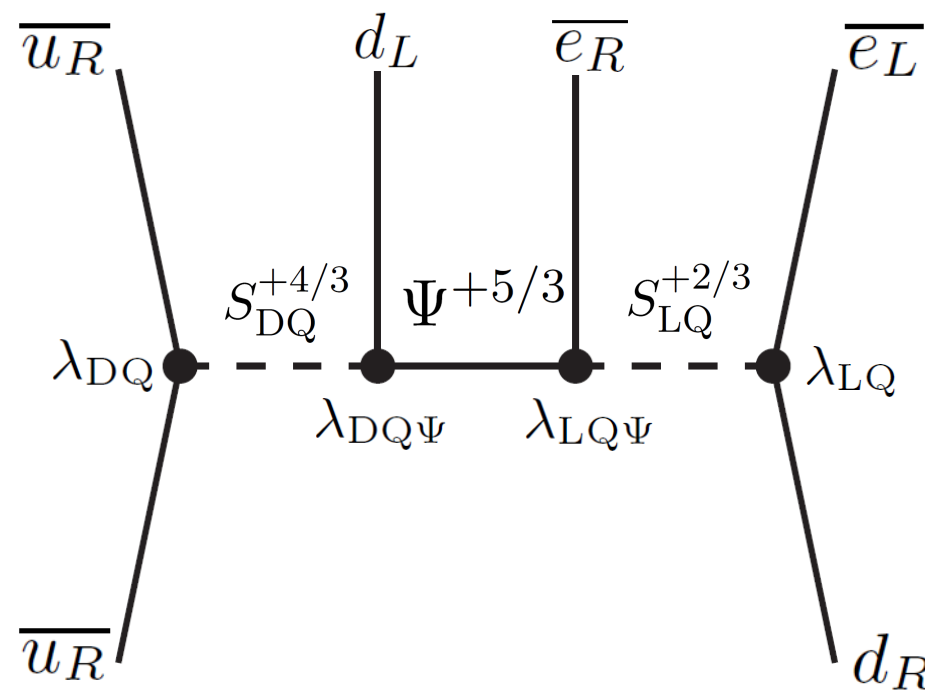
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$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia}, \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

$$= \frac{\lambda_{DQ} \lambda_{DQ\Psi} \lambda_{LQ\Psi} \lambda_{LQ}}{m_{DQ}^2 m_{LQ}^2 m_{\Psi}} \left[ (\overline{u_R})^{I'a} (T_{\overline{\mathbf{6}}})_{I'J'}^X (u_R^c)_a^{J'} \right] \left[ (\overline{d_L}^c)_I^b (T_{\mathbf{6}})_{XJ}^{IJ} (e_R^c)_b \right] \left[ (\overline{e_L})_{\dot{c}} (d_R)_{\dot{J}}^{\dot{c}} \right]$$



$$(\overline{u}_R u_R)(Q)(\overline{e}_R)(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

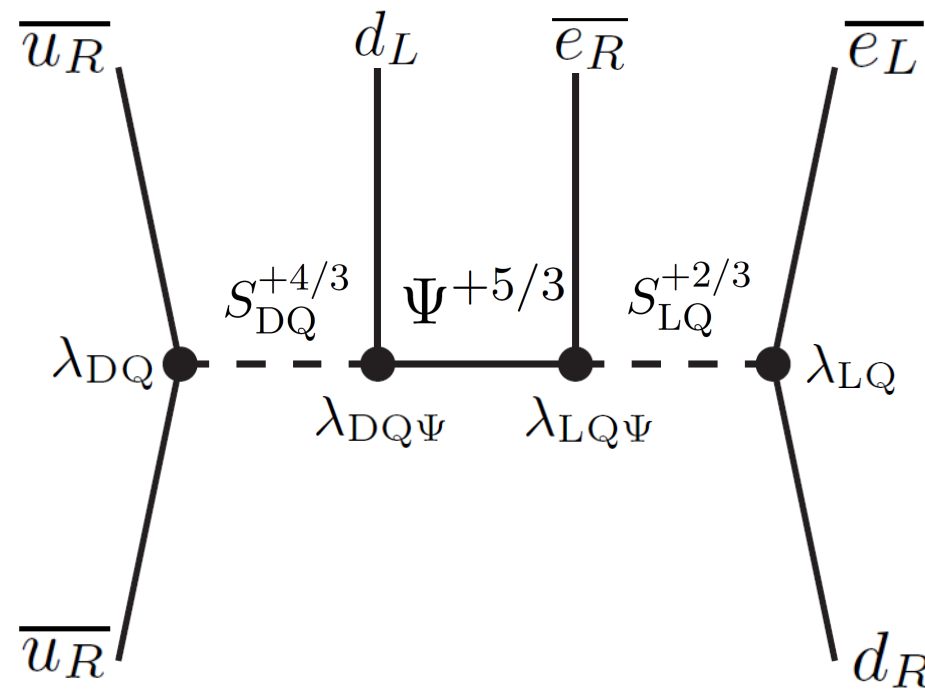
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$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

$$= \frac{\lambda_{DQ} \lambda_{DQ\Psi} \lambda_{LQ\Psi} \lambda_{LQ}}{m_{DQ}^2 m_{LQ}^2 m_{\Psi}} \frac{1}{32} [i(\mathcal{O}_4)_{LR} - (\mathcal{O}_5)_{LR}]$$



$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

$$(S_{DQ}^{+4/3})_X$$

$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

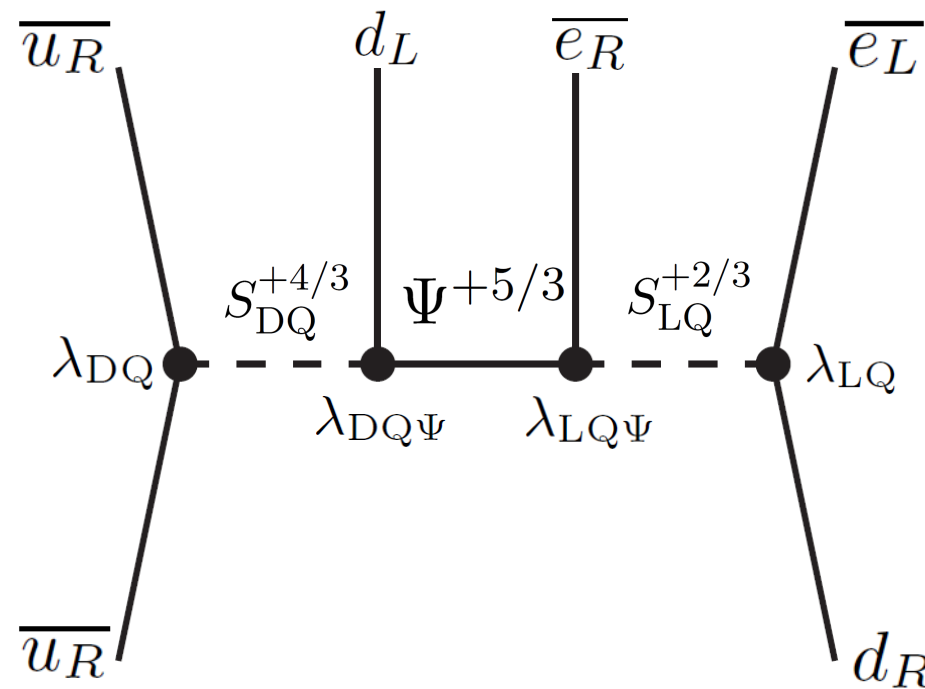
$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia} \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

$$= \frac{\lambda_{DQ} \lambda_{DQ\Psi} \lambda_{LQ\Psi} \lambda_{LQ}}{m_{DQ}^2 m_{LQ}^2 m_{\Psi}} \frac{1}{32} [i(\mathcal{O}_4)_{LR} - (\mathcal{O}_5)_{LR}] \quad \text{Take } \lambda\text{'s}=1, m=\Lambda$$

$$\text{On2b half-life: } \left( T_{1/2}^{0\nu 2\beta} \right)^{-1} = G_2 \left| \frac{2m_P}{G_F^2} \frac{1}{32} \frac{1}{\Lambda^5} [i\mathcal{M}_4 - \mathcal{M}_5] \right|^2$$





$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

$$(S_{DQ}^{+4/3})_X$$

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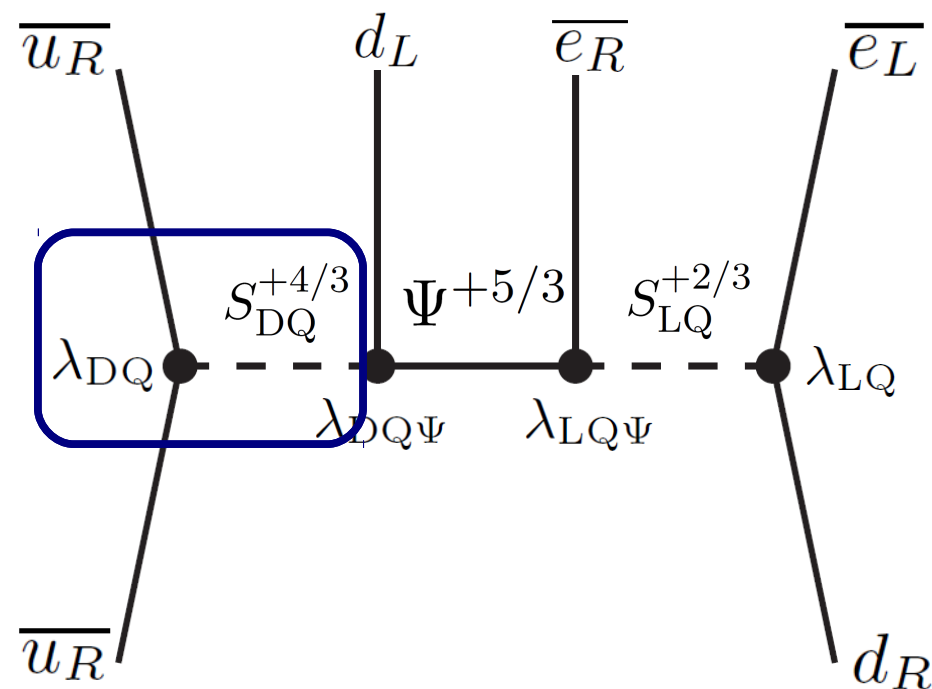
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$$\text{0n2b half-life: } \left( T_{1/2}^{0\nu 2\beta} \right)^{-1} = G_2 \left| \frac{2m_P}{G_F^2} \frac{1}{32} \frac{1}{\Lambda^5} [i\mathcal{M}_4 - \mathcal{M}_5] \right|^2$$

$$\text{Exp. bound: } T_{1/2}^{0\nu 2\beta}({}^{136}\text{Xe}) > 1.6 \cdot 10^{25} [\text{yr}] \longrightarrow \Lambda > 2.0 [\text{TeV}]$$

Q: What does this model suggest to LHC observables?



$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

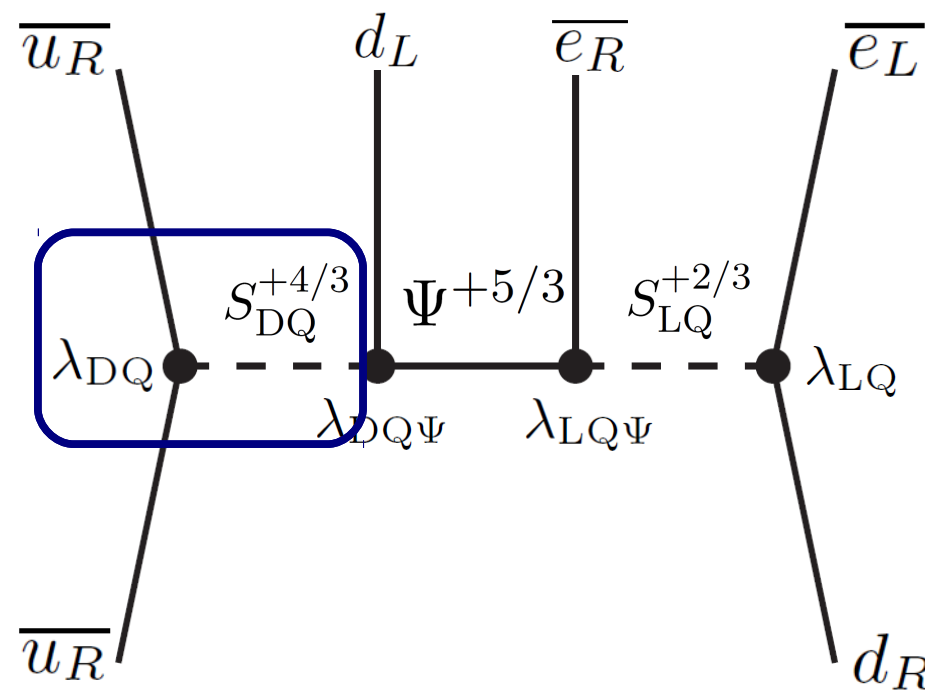
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$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

● Diquark (DQ):



$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

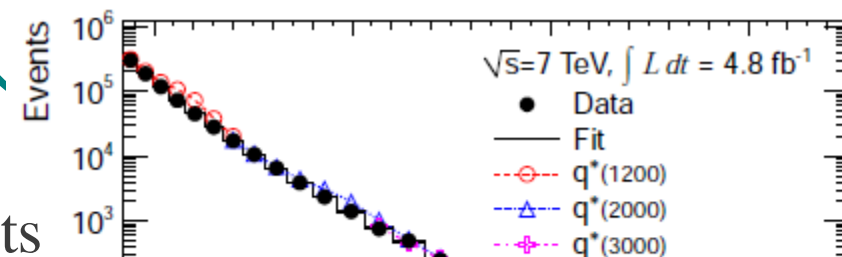
Take scalar mediators  
Specify the chiralities

Necessary mediators

$$(S_{DQ}^{+4/3})_X$$

$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

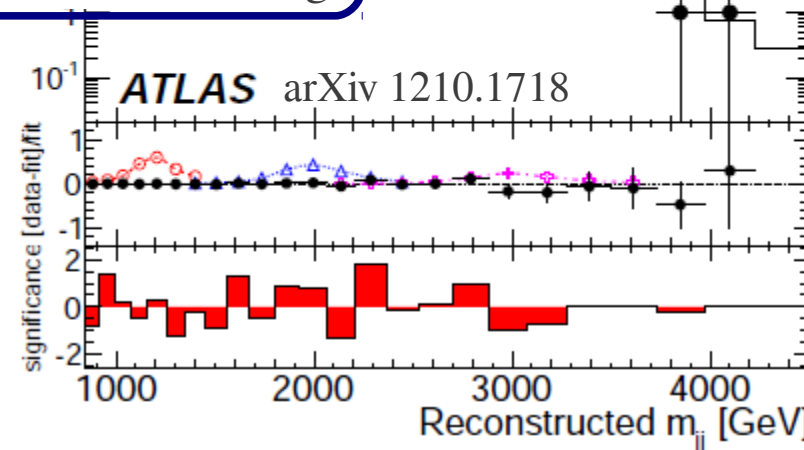
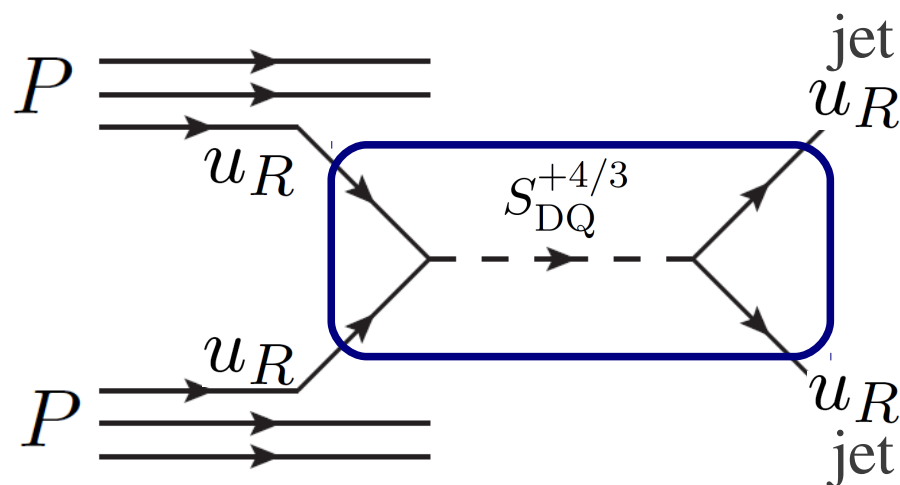
$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia} \right)^T$$

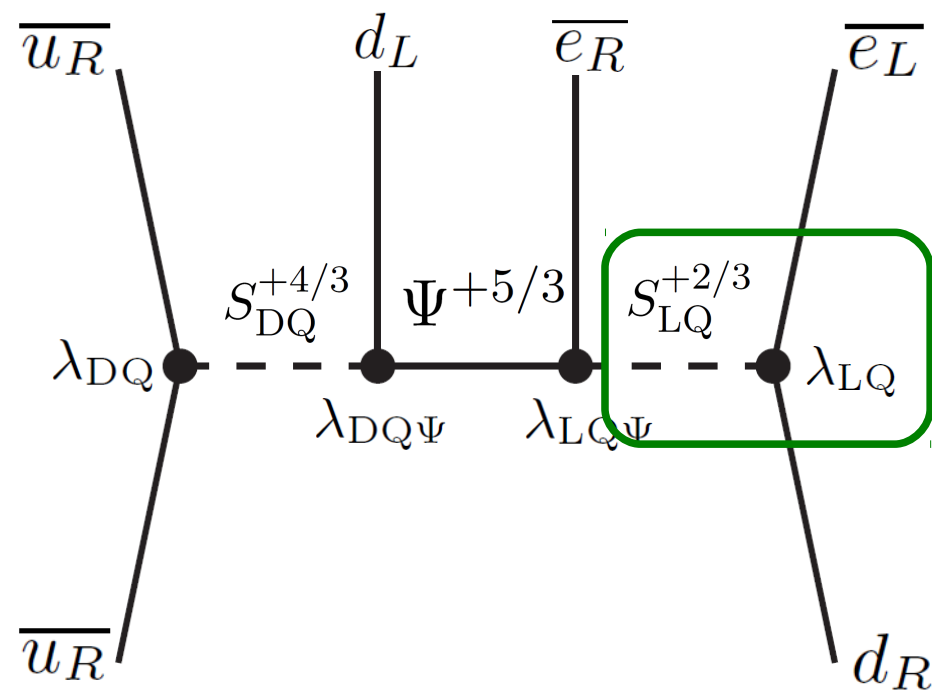


$$\lambda_{DQ} \lesssim 0.2$$

over this mass range

● **Diquark (DQ):** Search for a resonance in 2-jets





$$(\overline{u}_R u_R)(Q)(\overline{e}_R)(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

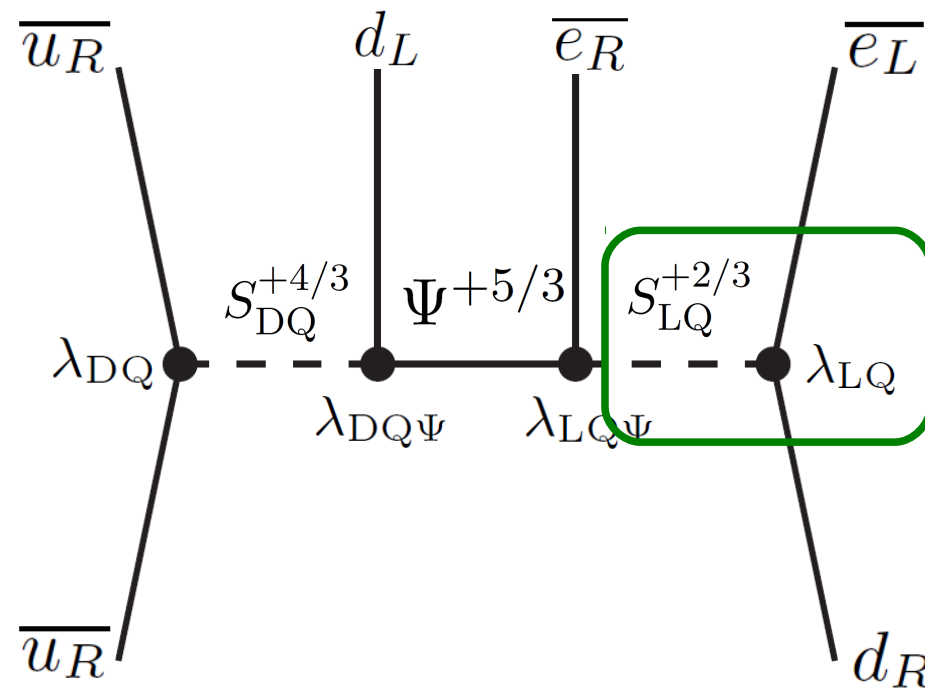
$$(S_{DQ}^{+4/3})_X$$

$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia}, \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

● **Leptoquark (LQ):**



$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

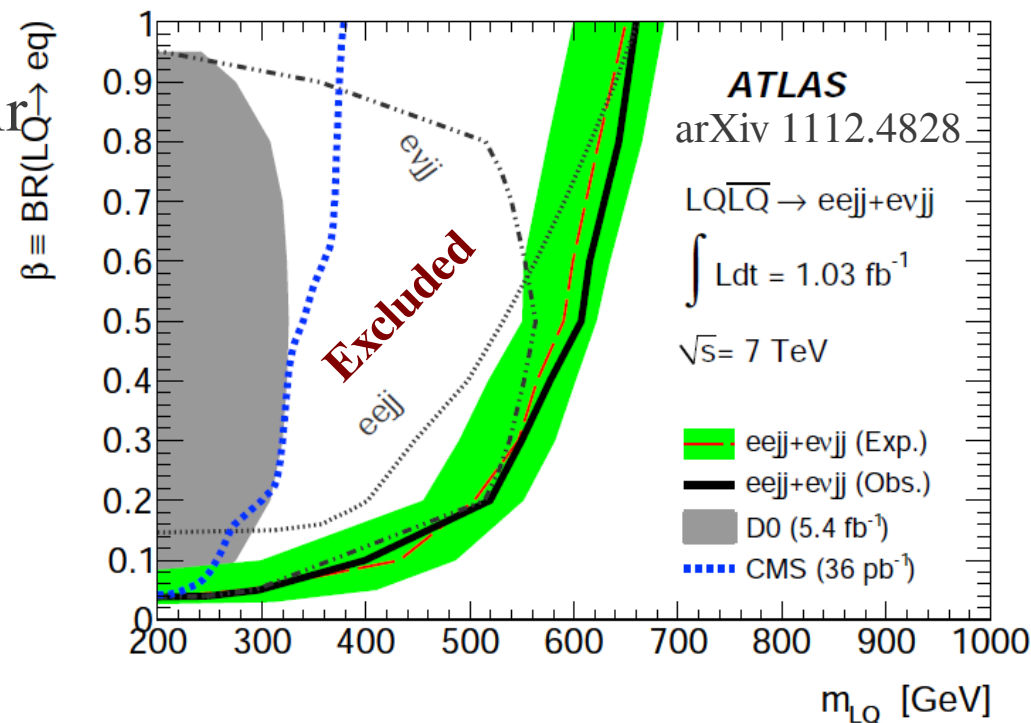
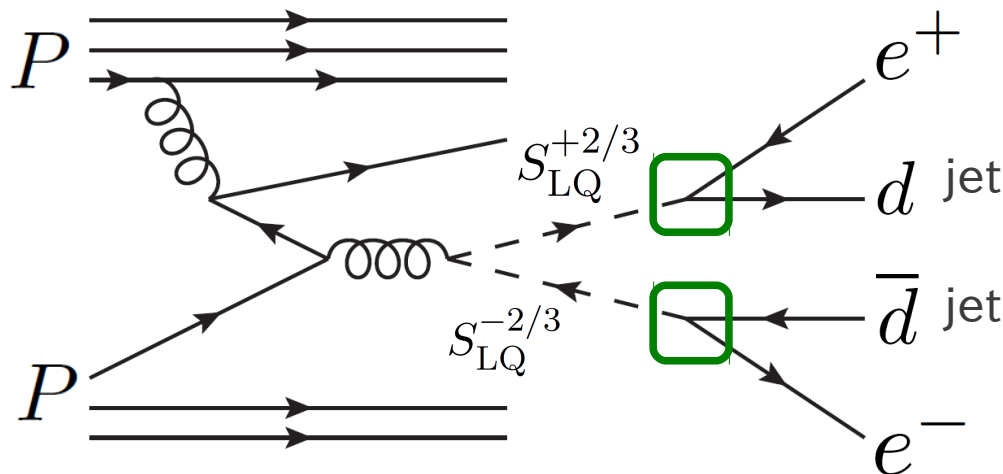
$$(S_{DQ}^{+4/3})_X$$

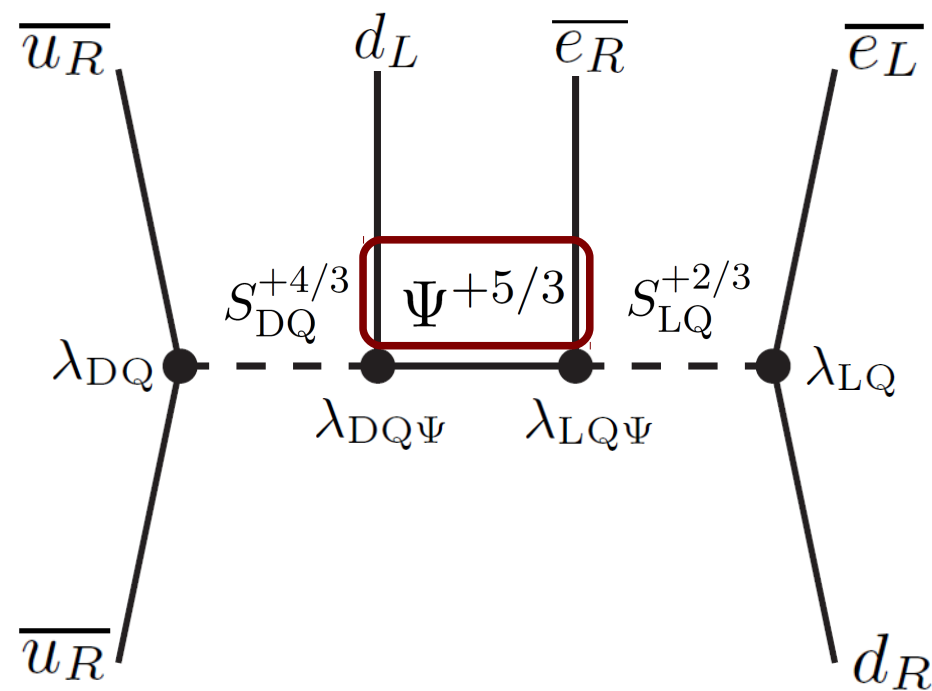
$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia}, \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

● **Leptoquark (LQ):** Search for a  $(eq)$ -pair





$$(\overline{u}_R u_R)(Q)(\overline{e}_R)(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

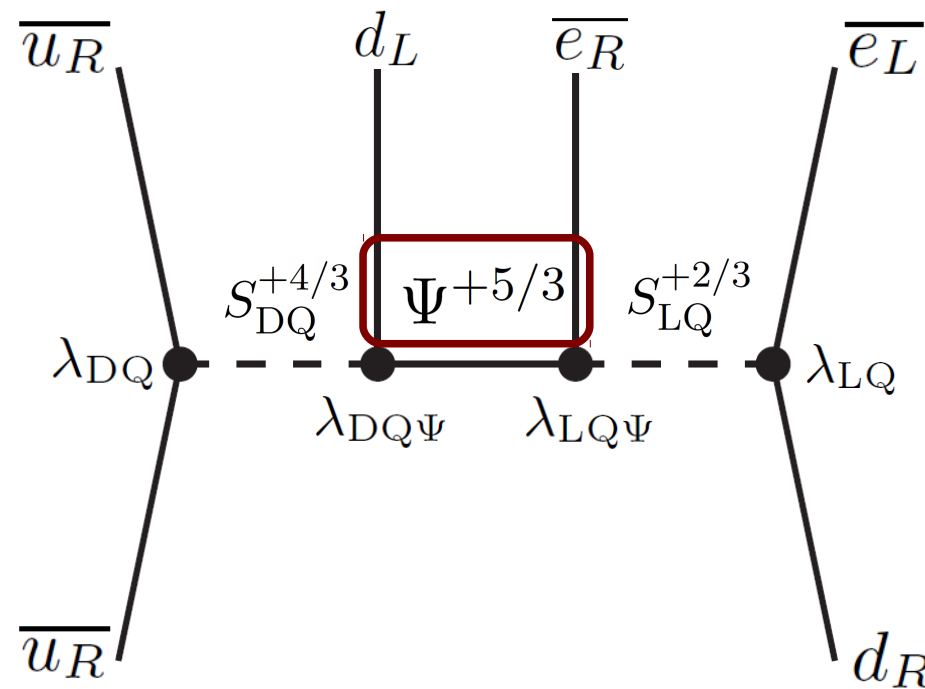
$$(S_{DQ}^{+4/3})_X$$

$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia}, \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

● Vector-like Quark (VLQ):



$$(\overline{u_R u_R})(Q)(\overline{e_R})(\overline{L} d_R)$$

Take scalar mediators  
Specify the chiralities

Necessary mediators

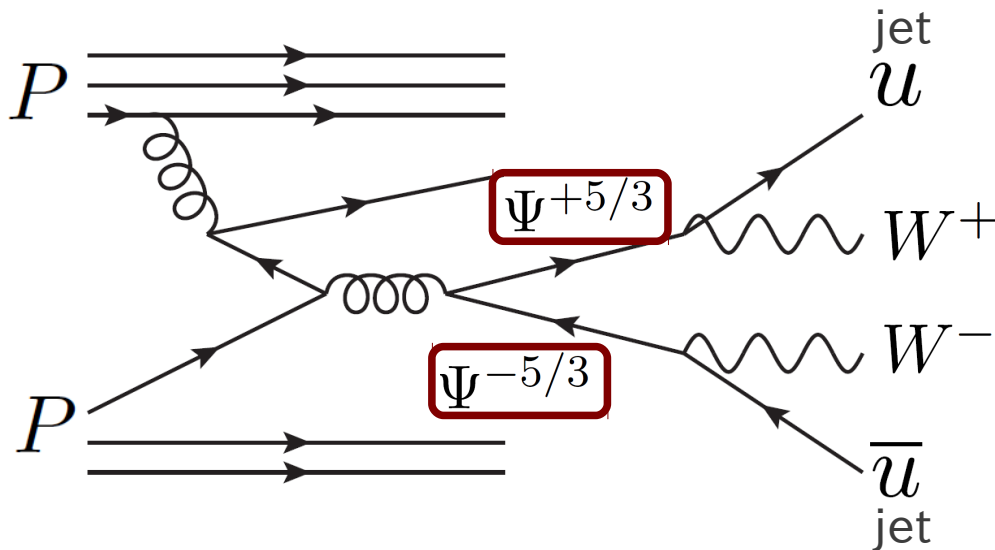
$$(S_{DQ}^{+4/3})_X$$

$$(S_{LQ})_{Ii} = \left( (S_{LQ}^{+2/3})_I, (S_{LQ}^{-1/3})_I \right)^T$$

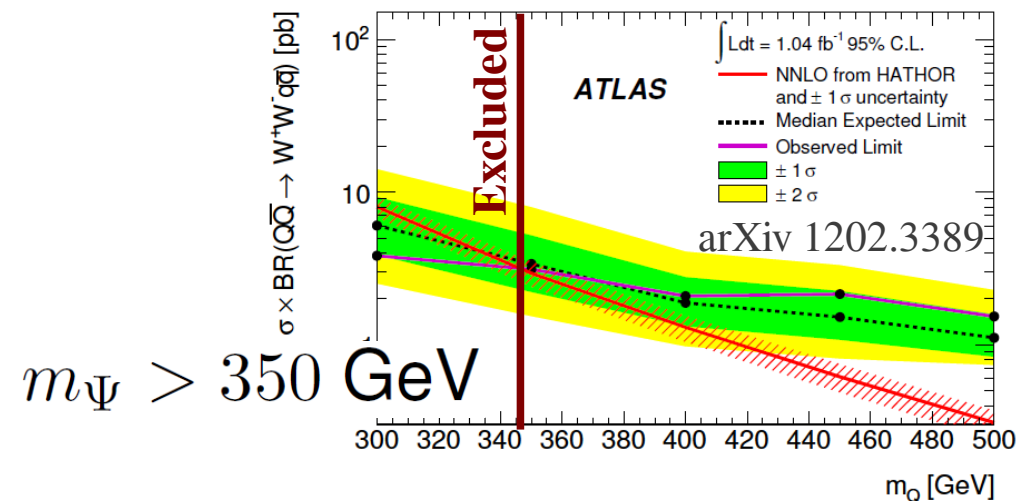
$$(\Psi_L)_{Iia} = \left( (\Psi_L^{+5/3})_{Ia}, (\Psi_L^{+2/3})_{Ia}, \right)^T$$

$$\text{and } (\Psi_R)_{Ii}^{\dot{a}}$$

● **Vector-like Quark (VLQ):** Search for a  $(qW)$ -pair



$$\mathcal{L}_{VLQ} = \lambda^\alpha (\overline{\Psi}_L)_{\dot{a}}^{Ii} (u_{R\alpha})_{\dot{I}}^{\dot{a}} H_i + \text{H.c.}$$



# Outline

New Physics ( $d=9$ ) contributions in neutrinoless double beta decay ( $0\nu 2b$ )

## 1 *Motivation: Why $0\nu 2b$ ? Why $dim=9$ ops?*

$d=9$  ops  $\rightarrow$  half-life time of  $0\nu 2b$  processes

“How sensitive  $0\nu 2b$  experiments to the  $d=9$  ops?”

## 2 *What do the $d=9$ ops suggest to TeV scale physics?*

$d=9$  ops  $\rightarrow$  decompose them to the fundamental ints.

**Summary**

$\rightarrow$  list the TeV signatures of each completion

$\rightarrow$  The list helps us to discriminate the models

---

## 3 *Seeking a relation to the models at the TeV scale*

TeV scale models with LNV  $\rightarrow$  Models for radiative neutrino masses



What can we learn from this table?

If 0n2b conflicts with  
cosmological obs.,

It could be a large  $d=9$  contribution

#	Decomposition	Long Range?	Mediator ( $U(1)_{em}, SU(3)_c$ )			Models/Refs./Comments
			$S$ or $V_\rho$	$\psi$	$S'$ or $V'_\rho$	
1-i	$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$	(a)	(+1, 1)	(0, 1)	(-1, 1)	Mass mechan., RPV [58–60], LR-symmetric models [39], Mass mechanism with $\nu_S$ [61] TeV scale seesaw, e.g., [62, 63] [64]
1-ii-a	$(\bar{u}d)(\bar{u})(d)(\bar{e}\bar{e})$		(+1, 8) (+1, 1) (+1, 8)	(0, 8) (+5/3, 3) (+5/3, 3)	(-1, 8) (+2, 1) (+2, 1)	
1-ii-b	$(\bar{u}d)(d)(\bar{u})(\bar{e}\bar{e})$		(+1, 1) (+1, 8)	(+4/3, 3) (+4/3, 3)	(+2, 1) (+2, 1)	
2-i-a	$(\bar{u}d)(d)(\bar{e})(\bar{u}\bar{e})$		(+1, 1) (+1, 8)	(+4/3, 3) (+4/3, 3)	(+1/3, 3) (+1/3, 3)	
2-i-b	$(\bar{u}d)(\bar{e})(d)(\bar{u}\bar{e})$	(b)	(+1, 1) (+1, 8)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60], LQ [65, 66]
2-ii-a	$(\bar{u}d)(\bar{u})(\bar{e})(d\bar{e})$		(+1, 1) (+1, 8)	(+5/3, 3) (+5/3, 3)	(+2/3, 3) (+2/3, 3)	
2-ii-b	$(\bar{u}d)(\bar{e})(\bar{u})(d\bar{e})$	(b)	(+1, 1) (+1, 8)	(0, 1) (0, 8)	(+2/3, 3) (+2/3, 3)	RPV [58–60], LQ [65, 66]
2-iii-a	$(d\bar{e})(\bar{u})(d)(\bar{u}\bar{e})$	(c)	(-2/3, 3) (-2/3, 3)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60] RPV [58–60]
2-iii-b	$(d\bar{e})(d)(\bar{u})(\bar{u}\bar{e})$		(-2/3, 3) (-2/3, 3)	(-1/3, 3) (-1/3, 6)	(+1/3, 3) (+1/3, 3)	
3-i	$(\bar{u}\bar{u})(\bar{e})(\bar{e})(dd)$		(+4/3, 3) (+4/3, 6)	(+1/3, 3) (+1/3, 6)	(-2/3, 3) (-2/3, 6)	only with $V_\rho$ and $V'_\rho$
3-ii	$(\bar{u}\bar{u})(d)(d)(\bar{e}\bar{e})$		(+4/3, 3) (+4/3, 6)	(+5/3, 3) (+5/3, 3)	(+2, 1) (+2, 1)	only with $V_\rho$
3-iii	$(dd)(\bar{u})(\bar{u})(\bar{e}\bar{e})$		(+2/3, 3) (+2/3, 6)	(+4/3, 3) (+4/3, 3)	(+2, 1) (+2, 1)	only with $V_\rho$
4-i	$(d\bar{e})(\bar{u})(\bar{u})(d\bar{e})$	(c)	(-2/3, 3) (-2/3, 3)	(0, 1) (0, 8)	(+2/3, 3) (+2/3, 3)	RPV [58–60] RPV [58–60]
4-ii-a	$(\bar{u}\bar{u})(d)(\bar{e})(d\bar{e})$		(+4/3, 3) (+4/3, 6)	(+5/3, 3) (+5/3, 3)	(+2/3, 3) (+2/3, 3)	only with $V_\rho$ see Sec. 4 (this work)
4-ii-b	$(\bar{u}\bar{u})(\bar{e})(d)(d\bar{e})$		(+4/3, 3) (+4/3, 6)	(+1/3, 3) (+1/3, 6)	(+2/3, 3) (+2/3, 3)	only with $V_\rho$
5-i	$(\bar{u}\bar{e})(d)(d)(\bar{u}\bar{e})$	(c)	(-1/3, 3) (-1/3, 3)	(0, 1) (0, 8)	(+1/3, 3) (+1/3, 3)	RPV [58–60] RPV [58–60]
5-ii-a	$(\bar{u}\bar{e})(\bar{u})(\bar{e})(dd)$		(-1/3, 3) (-1/3, 3)	(+1/3, 3) (+1/3, 6)	(-2/3, 3) (-2/3, 6)	only with $V'_\rho$
5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(dd)$		(-1/3, 3) (-1/3, 3)	(-4/3, 3) (-4/3, 3)	(-2/3, 3) (-2/3, 6)	only with $V'_\rho$

Colour 8

Colour 3

Colour 6

What can we learn from this table?

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5-ii-b	$(\bar{u}\bar{e})(\bar{e})(\bar{u})(d\bar{d})$		$(-1/3, 3)$	$(-4/3, 3)$	$(-2/3, 3)$		only with $V'_\rho$

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What can we learn from this table?

If 0n2b conflicts with cosmological obs.,

It could be a large  $d=9$  contribution

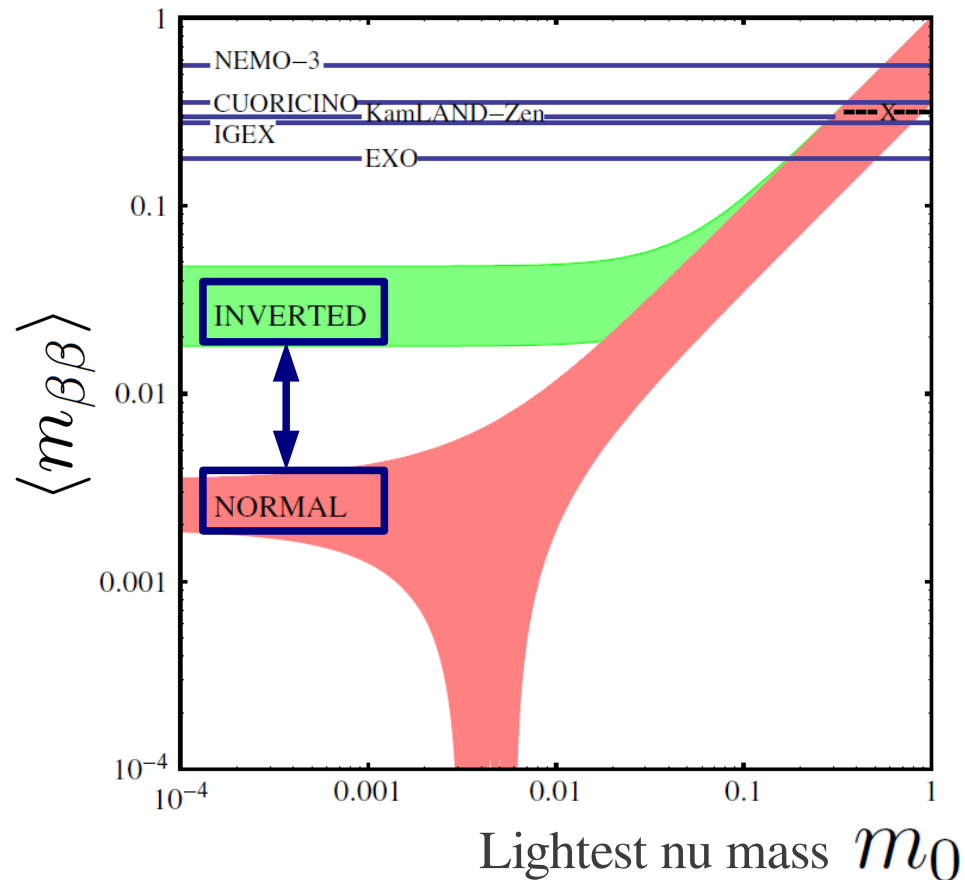
Such a large  $d=9$  contribution should leave the trace in LHC except for T-I-1-i (and T-II-1) that does not contain a coloured mediator

T-I-1-i can be examined at ILC! exotic interactions with electron!

My 2<sup>nd</sup> last message:

0n2b exps, cosmological obs, LHC and ILC are complementary!



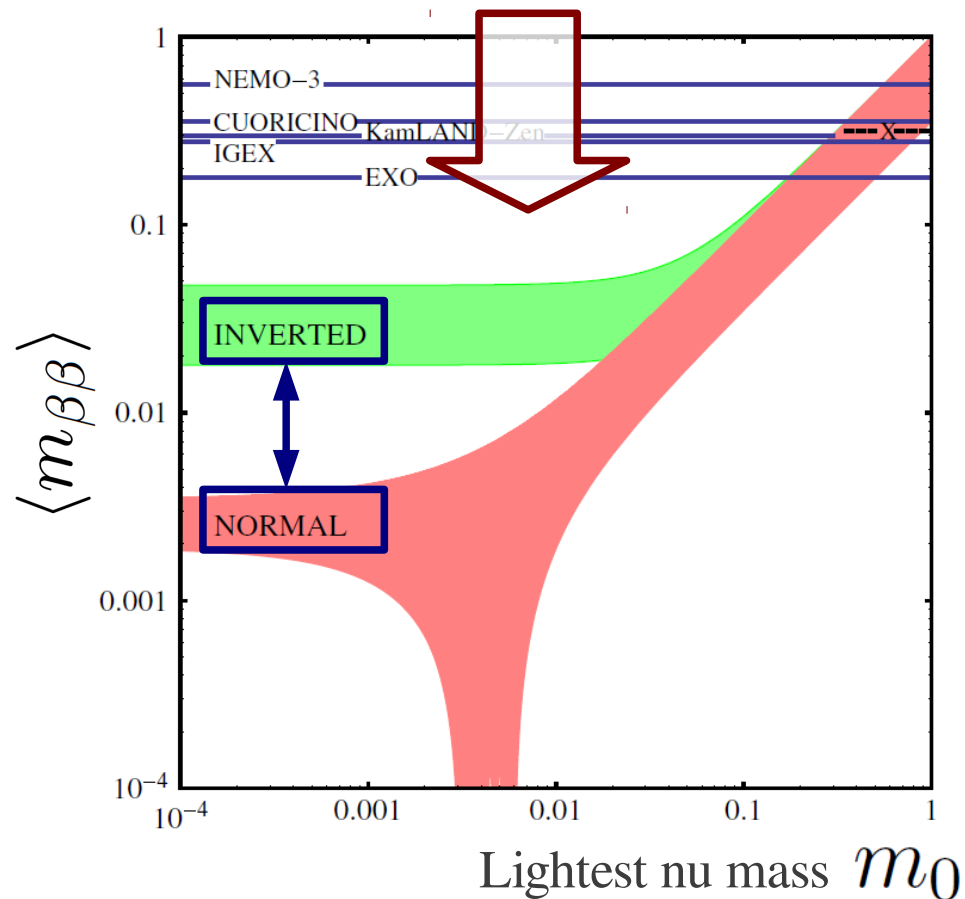


Standard 3nu parameter space

Neutrino mass search is  
the foremost front where

● Oscillation experiments,

face to the *Neutrino effective theory  
in the Universe*

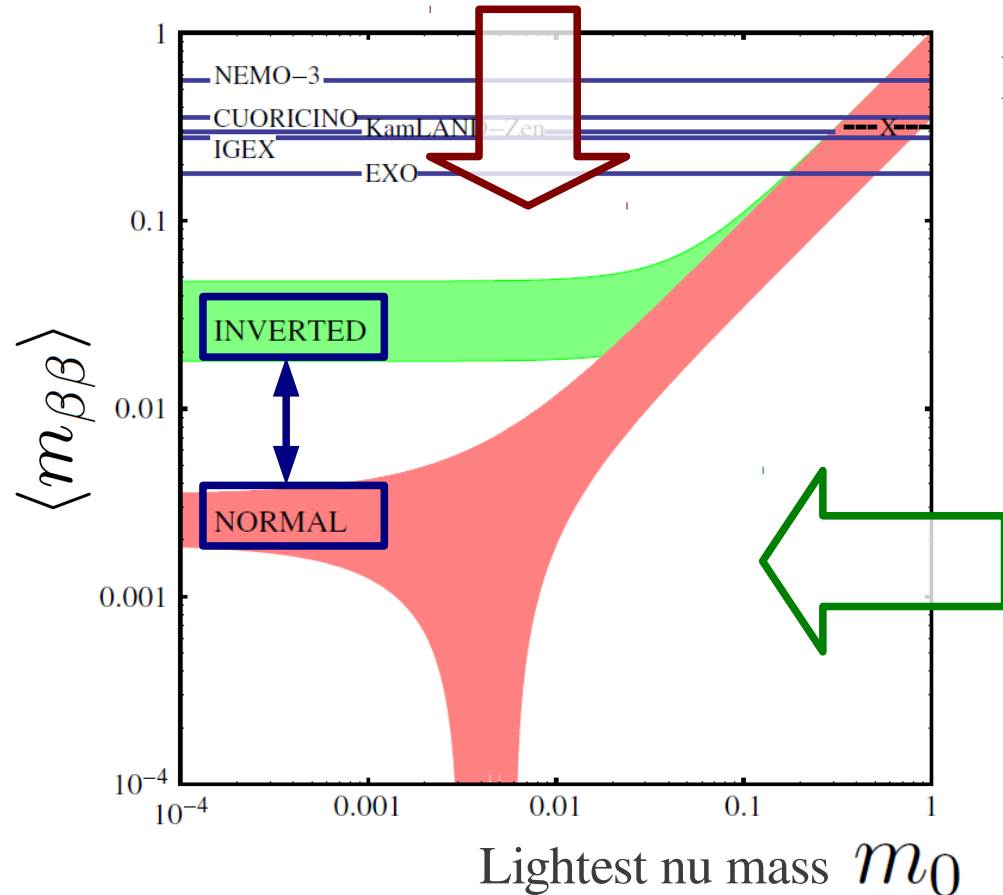


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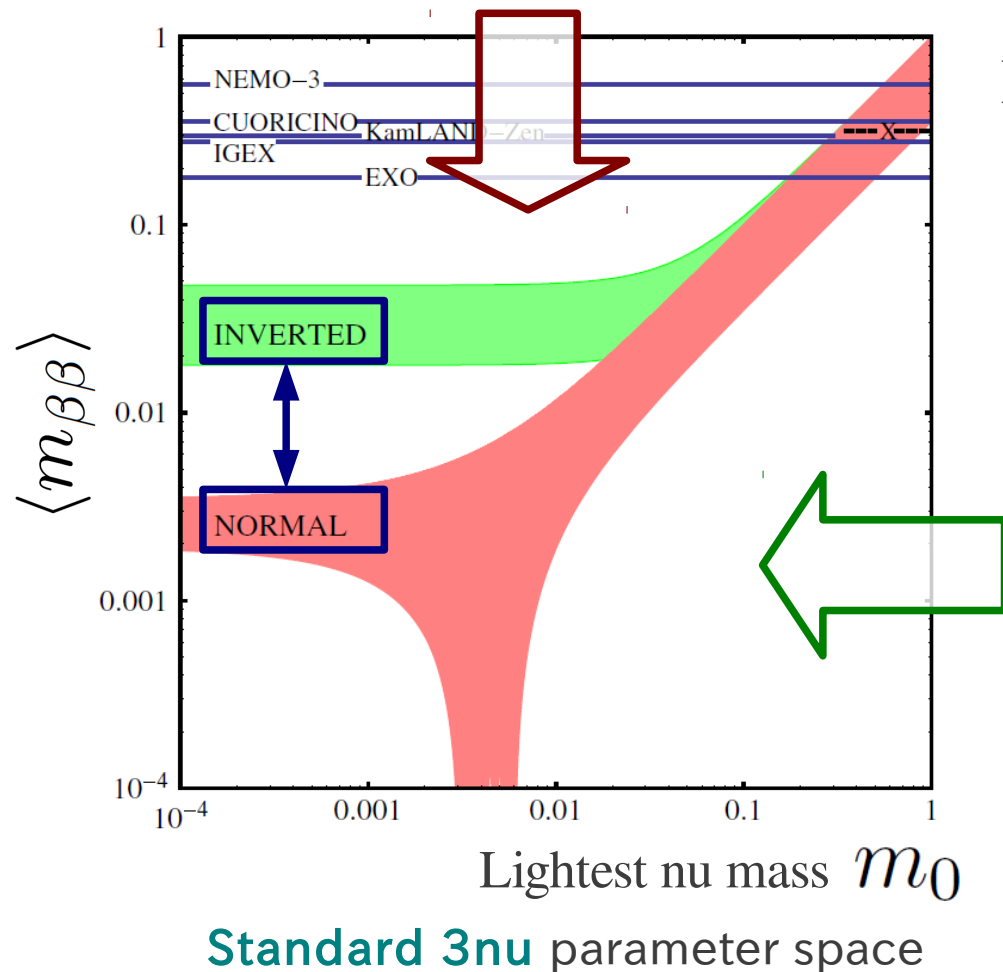


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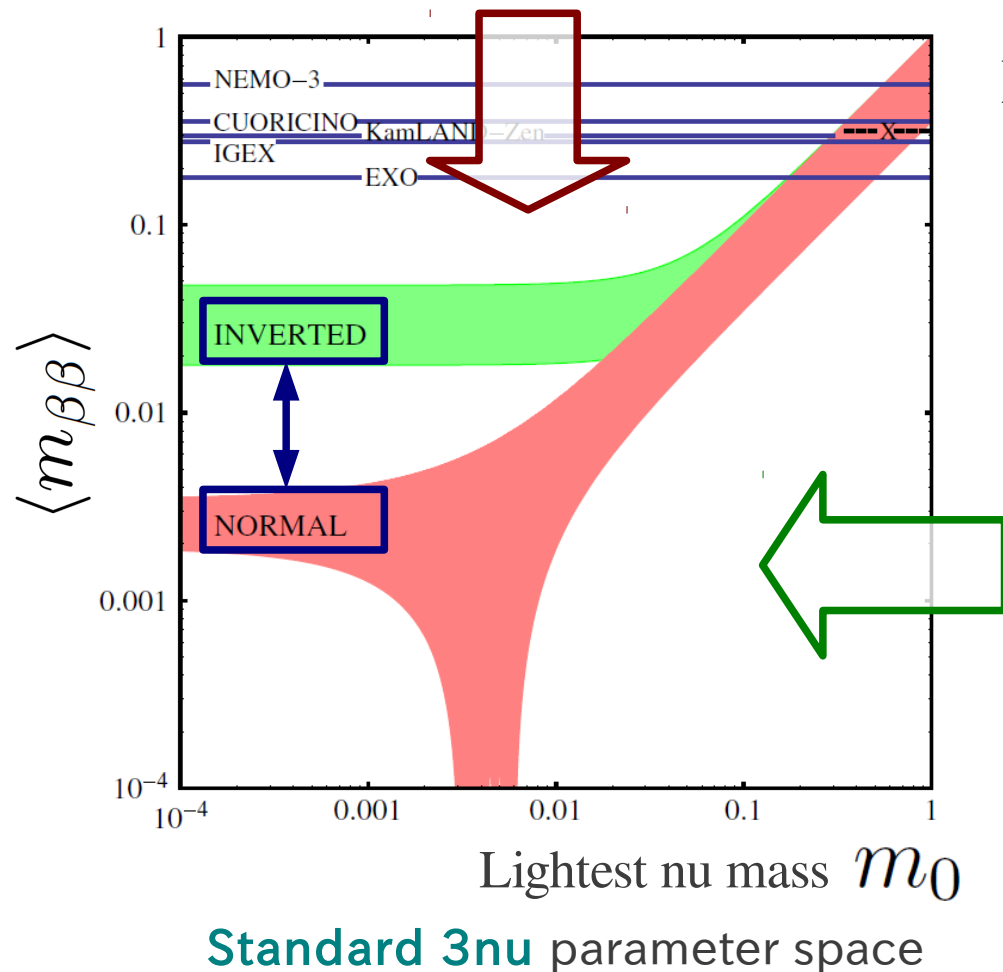
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If something unexpected will happen  
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In this talk we focus on the particle physics side. How about cosmological side?





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Cosmological side: Possible disturbance of neutrino mass bound?

Dark matter effective theory? and its high  $E$  completions?

# Outline

New Physics ( $d=9$ ) contributions in neutrinoless double beta decay ( $0\nu 2b$ )

## 1 *Motivation: Why $0\nu 2b$ ? Why $dim=9$ ops?*

$d=9$  ops  $\rightarrow$  half-life time of  $0\nu 2b$  processes

“How sensitive  $0\nu 2b$  experiments to the  $d=9$  ops?”

## 2 *What do the $d=9$ ops suggest to TeV scale physics?*

$d=9$  ops  $\rightarrow$  decompose them to the fundamental ints.

$\rightarrow$  list the TeV signatures of each completion

$\rightarrow$  The list helps us to discriminate the models

In progress  
Under discussion

## 3 *Seeking a relation to the models at the TeV scale*

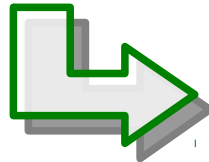
TeV scale models with LNV  $\rightarrow$  Models for radiative neutrino masses

Maybe, we have already known the mediators appear in the big table...

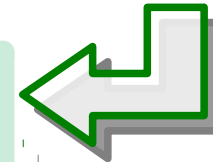
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**Radiative neutrino mass models  
with TeV ingredients**



In such models

Size of **two contributions** to  $0\nu 2b$  can be **comparable!**

Standard one

$$m_\nu \sim 0.1 \text{ eV}$$

dim=9

$$\Lambda_{\text{NP}} \sim 1 \text{ TeV}$$

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### Radiative neutrino mass models with TeV ingredients

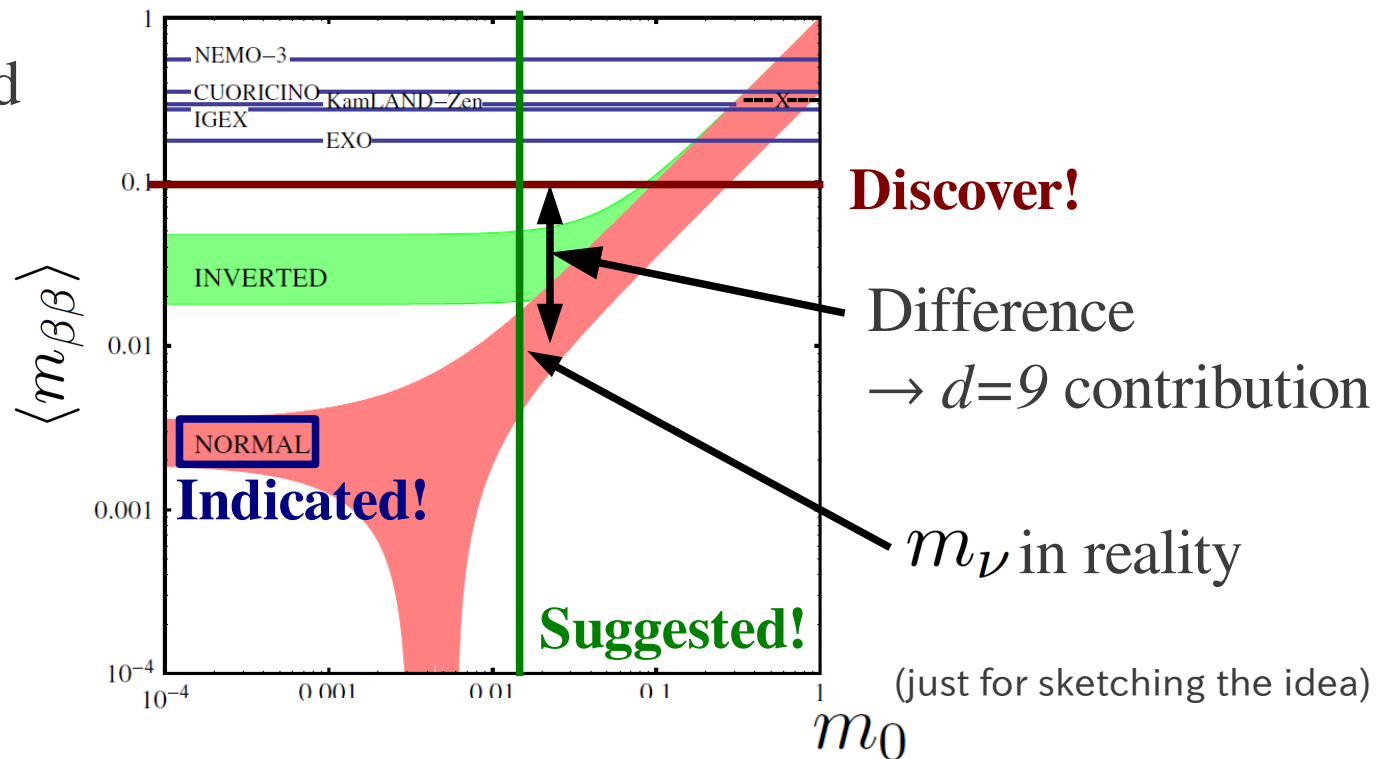
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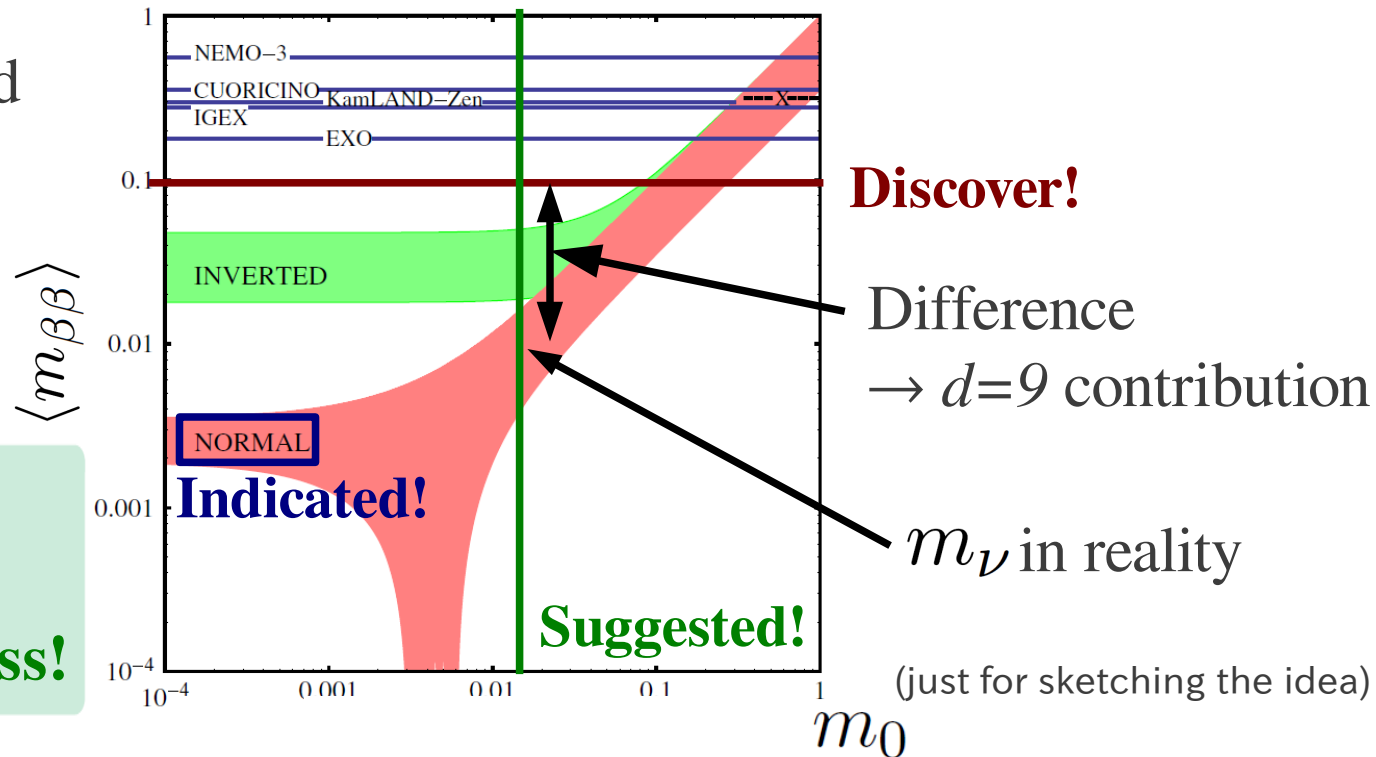
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With the info on this plane,  
we have a chance to know  
**the origin of neutrino mass!**

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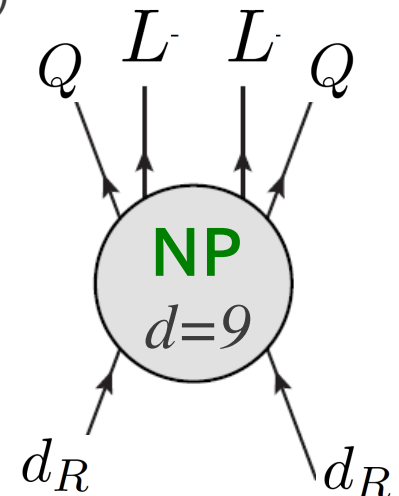
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Examples introduced in recent papers, based on Decomposition of  $LLQQd_Rd_R$

**Coloured Babu-Zee model** with  $LQ(3, 1, -1/3)$ ,  $DQ(6, 1, -2/3)$

Kohda Sugiyama Tsumura PLB718 (2013) 1436

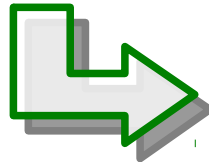
$$\mathcal{O}_{\text{eff}}^{0\nu 2\beta} =$$



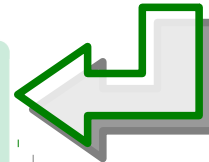
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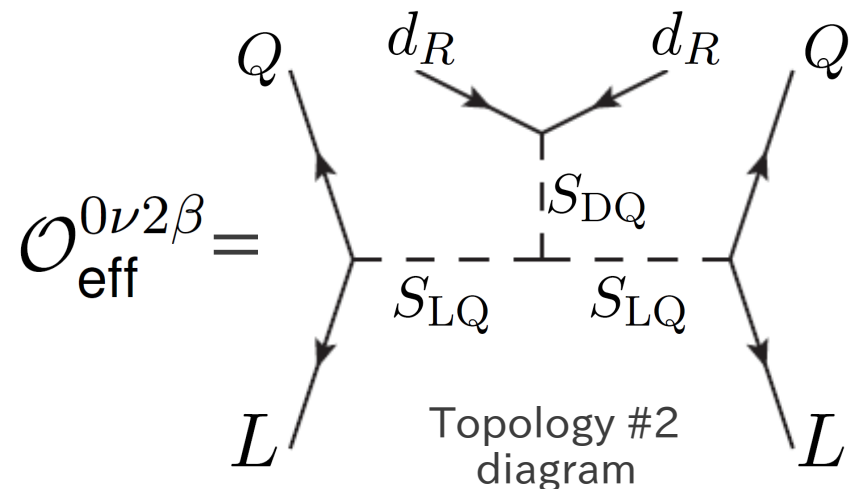
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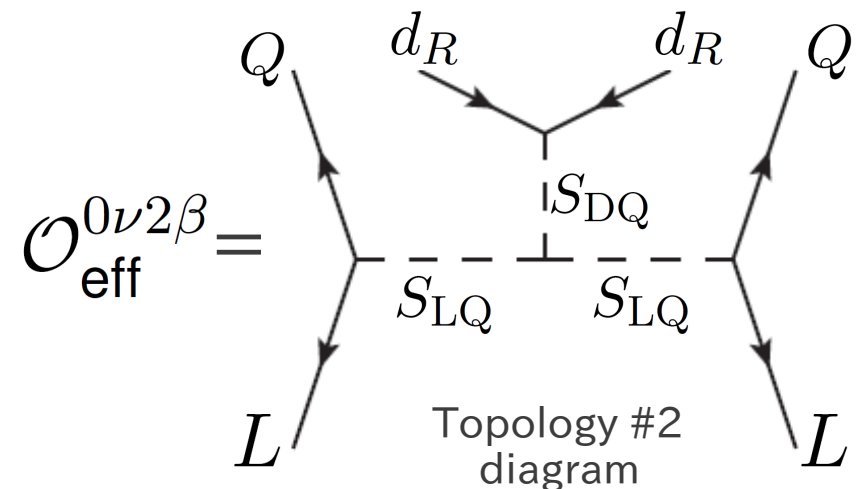
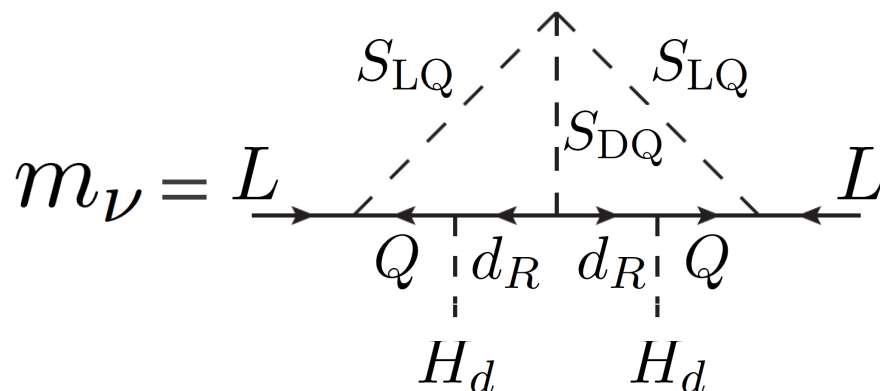
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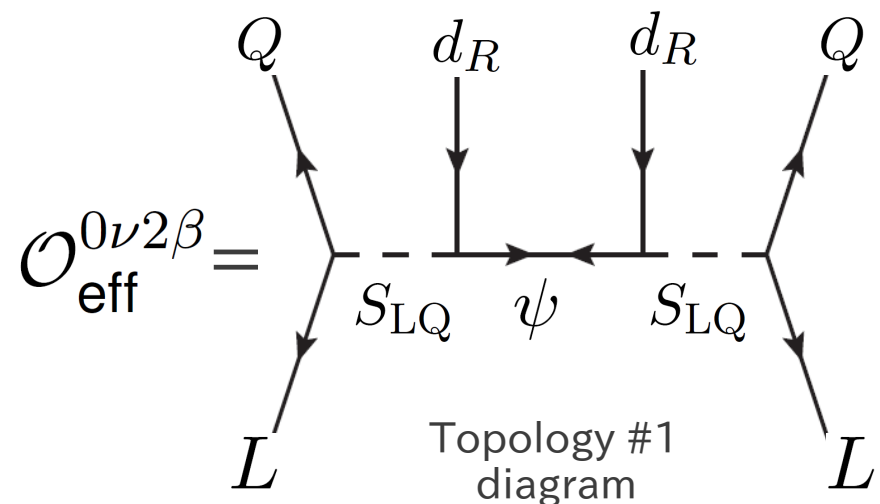
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**Two-loop mNu model** with  $LQ(3, 1, -1/3)$ , Majorana fermion  $(8, 1, 0)$

Angel Cai Rodd Schmidt Volkas 1308.0463



Dim=9 op is directly proportional to  $m_\nu$ , and its contribution to  $0\nu 2\beta$  seems to be large.

Maybe, we have already known the mediators appear in the big table...

- They have masses of the TeV scale
- $\#L$  must be violated in somewhere

**Radiative neutrino mass models  
with TeV ingredients**

In such models

Size of **two contributions** to  $0\nu 2\beta$  can be **comparable!**

Standard one

$$m_\nu \sim 0.1 \text{ eV}$$

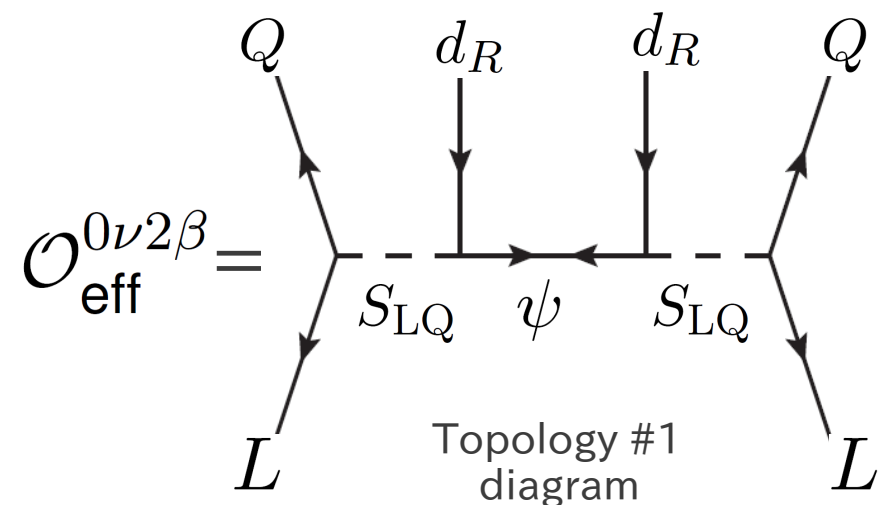
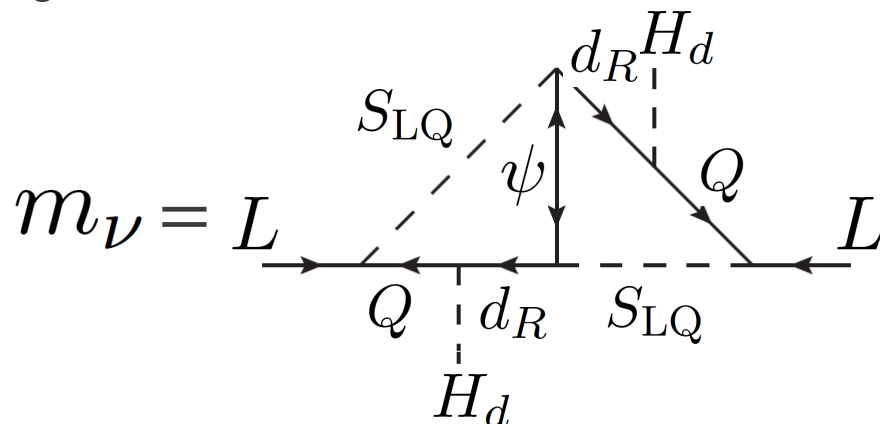
dim=9

$$\Lambda_{\text{NP}} \sim 1 \text{ TeV}$$

Examples introduced in recent papers, based on Decomposition of  $LLQQd_Rd_R$

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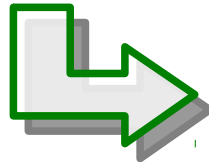
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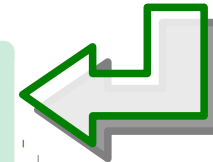
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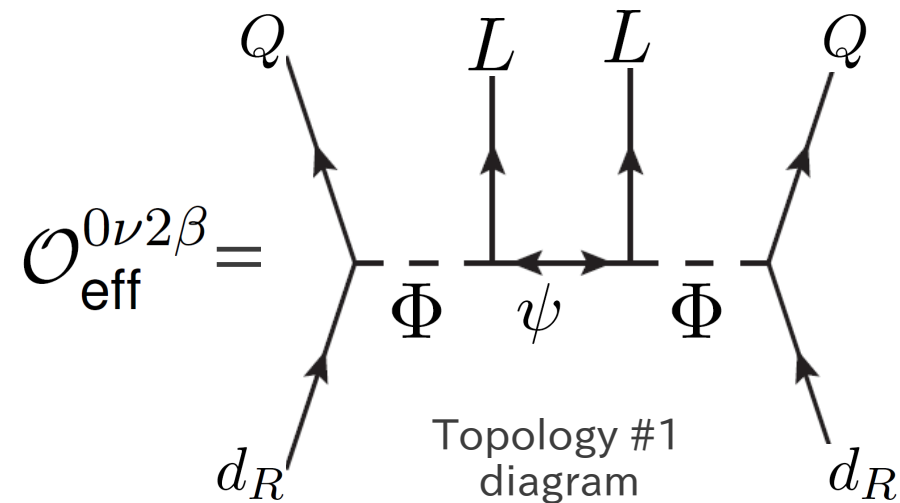
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**Colour-8 mNu model** with Scalar (8, 2, 1/2), Majorana fermion (8, 1, 0)

Choubey Duerr Mitra Rodejohann JHEP 1205 (2012) 017



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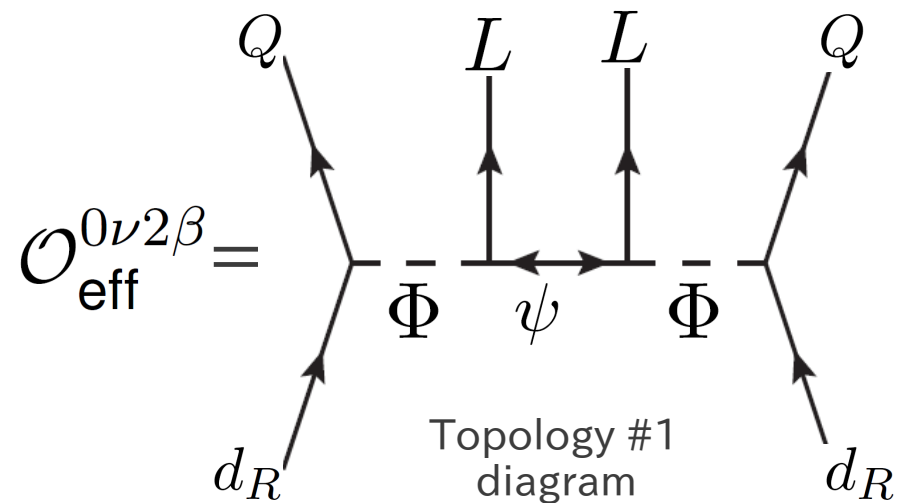
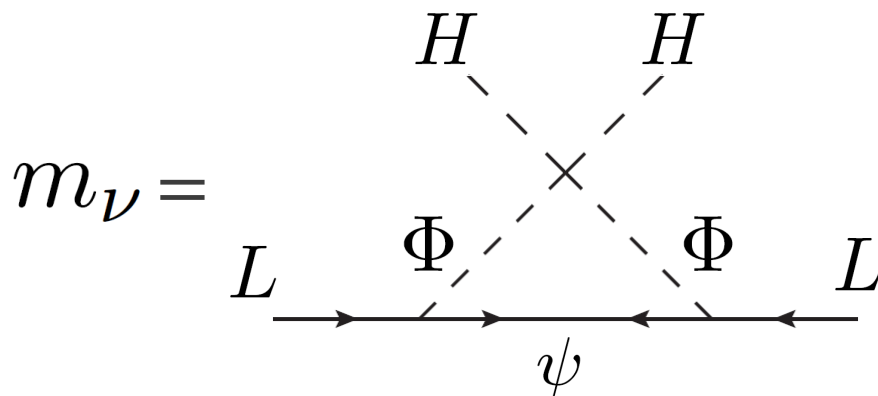
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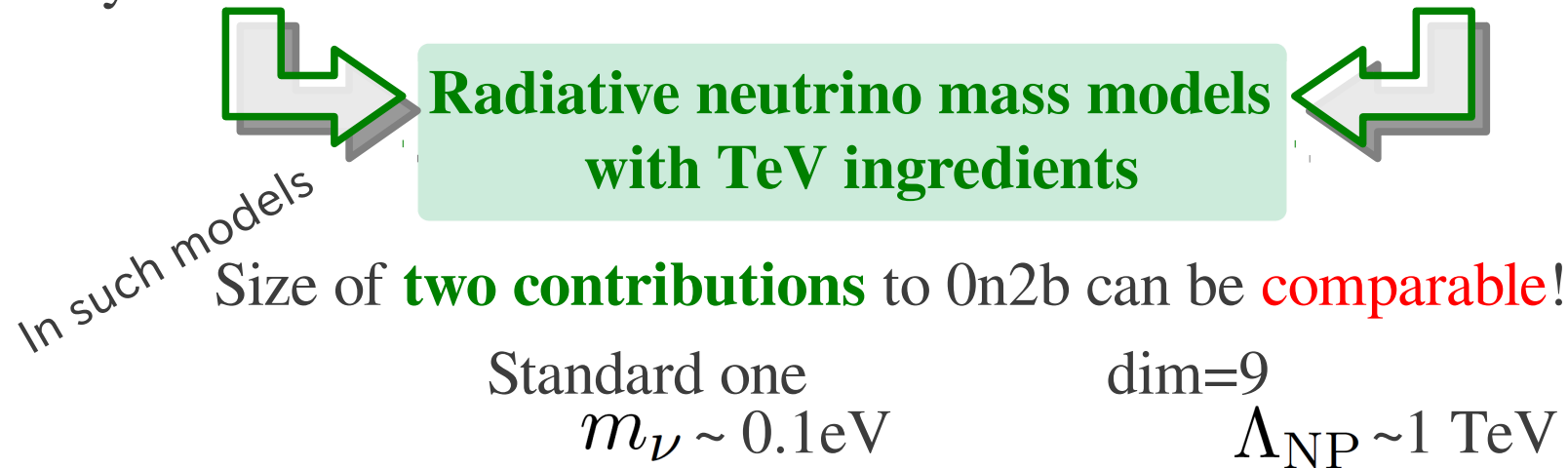
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Neutrino mass models based on the effective operator approach

Schechter Valle Phys. Rev. **D25** (1982) 2951

Babu Leung Nucl Phys **B619** (2001) 667

de Gouvea Jenkins Phys. Rev. **D77** (2008) 013008

del Aguila Aparici Bhattacharya Santamaria Wudka JHEP **1206** (2012) 146,  
JHEP **1205** (2012) 133

Angel Rodd Volkas Phys. Rev. **D87** (2013) 073007

Farzan Pascoli Schmidt JHEP **1303** (2013) 107

and more...

# Back up slides

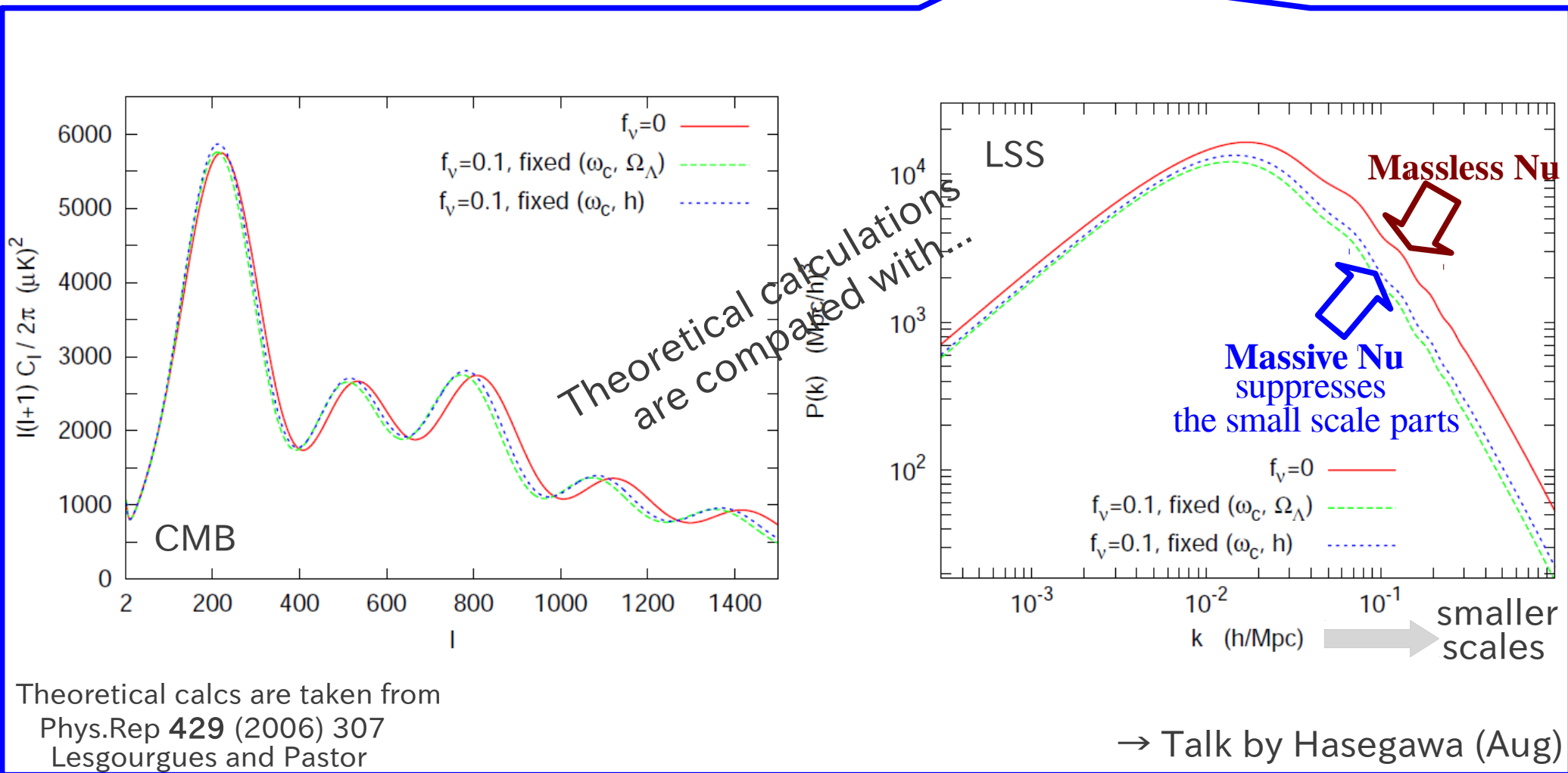
- 1 Neutrino mass bound from cosmological observations
- 2 LR symmetric model as a Decomposition of  $\dim=9$  op

- **0n2b exp** are sensitive to **Effective nu mass**

$$\langle m_{\beta\beta} \rangle \equiv \sum_{i=1}^3 (U_e^i)^2 m_i$$

- **Cosmological obs** constrain **Sum of nu masses**

$$\sum_{i=1}^3 m_i (\simeq 3m_0 \text{ if } m_0 \gtrsim 0.1 \text{ eV})$$





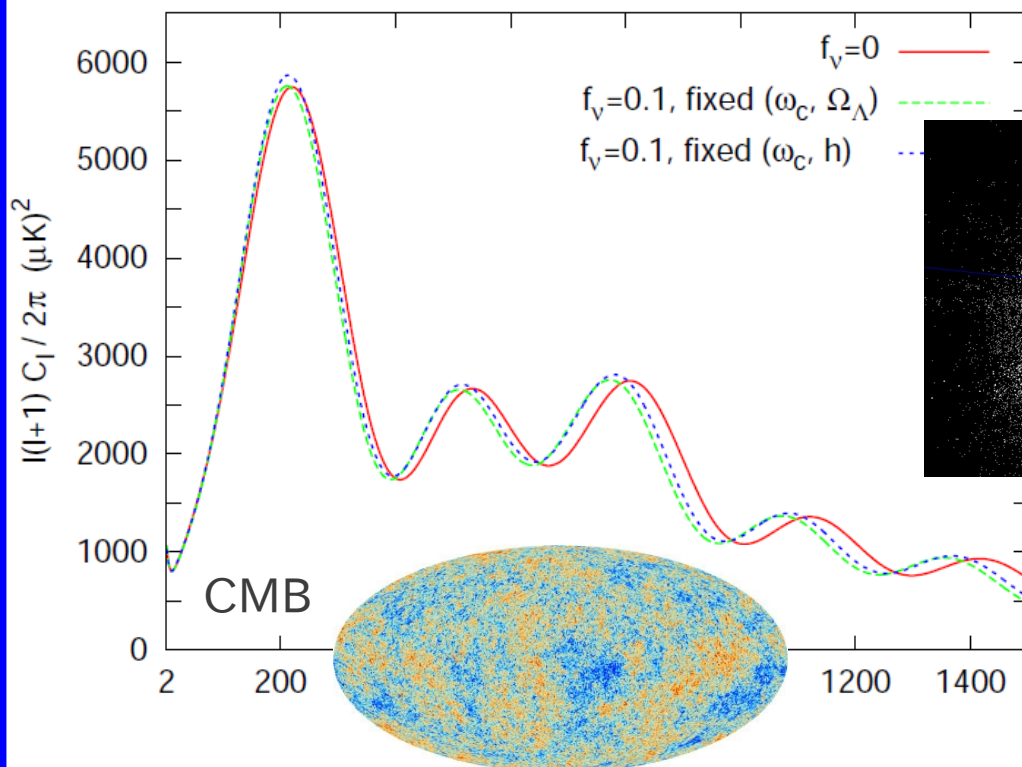
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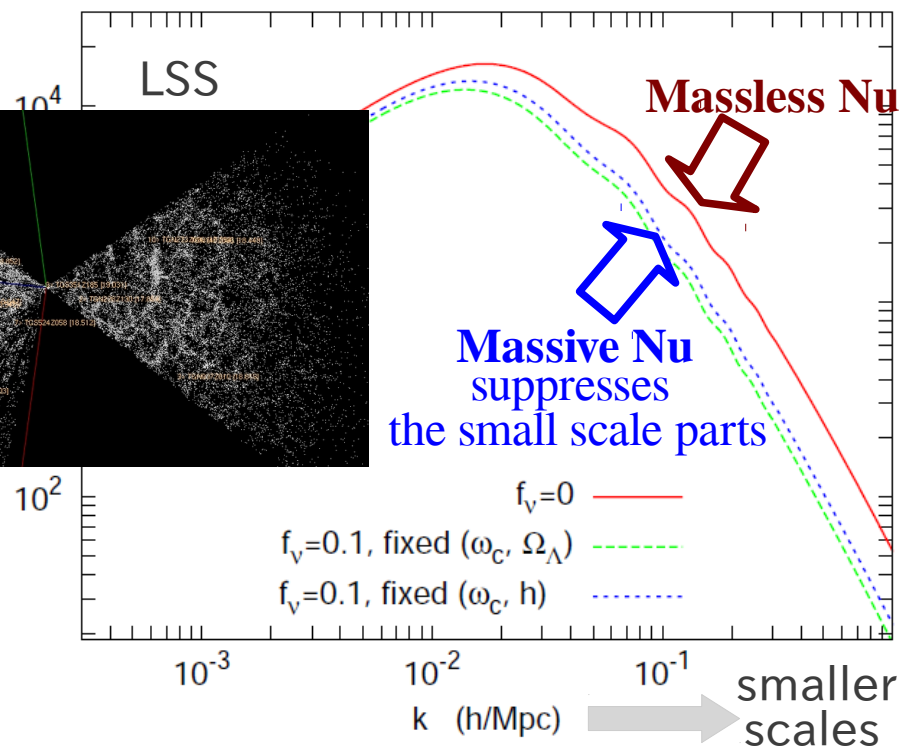
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Obs: Planck, WMAP-9year, and balloons



Obs: SDSS, 2dFGRS

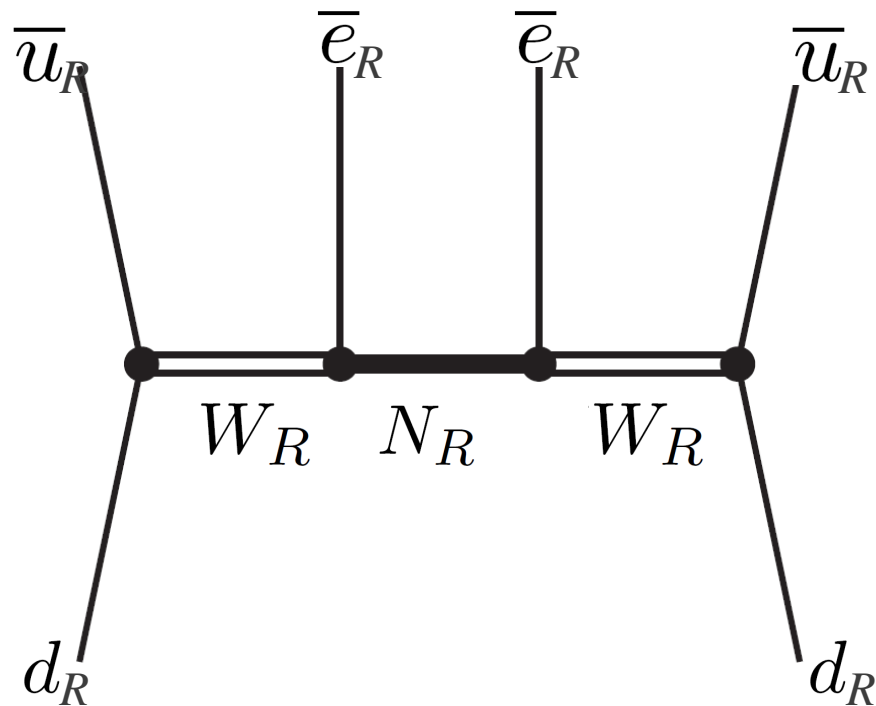


Theoretical calcs are taken from  
Phys.Rep **429** (2006) 307  
Lesgourgues and Pastor

→ Talk by Hasegawa (Aug)

- An example,  
Taking Topology #1  
let us decompose  $d=9$  op as

$$(\bar{u}d)(\bar{e})(\bar{e})(\bar{u}d)$$



Necessary mediators

$$V(+1, \mathbf{1}) \quad W_R$$

$$V'(-1, \mathbf{1}) \quad W_R$$

$$\psi(0, \mathbf{1}) \quad N_R$$

where  $(U(1)_{\text{em}}, SU(3)_c)$

***Left-right symmetric model***

All the outer fermions are right-handed

Bound from 0n2b

Riazuddin Marshak Mohapatra PRD24 (1981) 1310

$$M_{N_R} = M_{W_R} > 1.3 \text{ TeV } (g_L = g_R)$$

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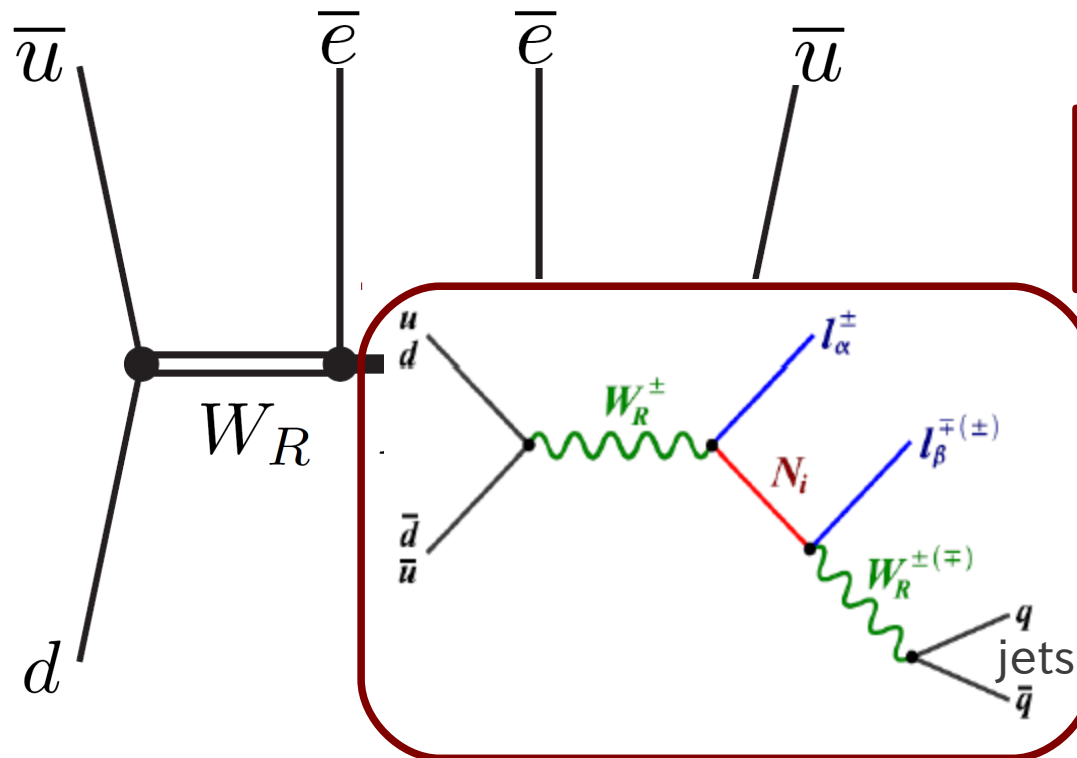
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$N_R$  and  $W_R$  collider search

Rizzo, Phys. Lett. B116 (1982) 23

Keung Senjanovic, Phys. Rev. Lett 50 (1983) 1427

ATLAS search for 2 leptons+jets: arXiv.1203.5420